Computational Lessons from and for Language

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The Gretchenfrage

What role can linguistics play in the computational sciences?
The Gretchenfrage

What role can linguistics play in the computational sciences?
Three Take Home Messages

1. Language is a fundamentally computational problem.
   cognitive turn, mental grammars, structure inference

2. Linguistics is a creator of computational results.
   subregular maps, finite-state decompositions

3. Linguistics is a consumer of computational results.
   tensor spaces, game theory, ...
Outline

1. Language as a Computational Problem

2. Results from Computational Linguistics
   - Some problems aren’t as complex as you might think
   - And complex problems are simple problems in disguise

3. Computational Problems in Linguistics
   - MSO-FSA conversion
   - Parallel parsing
   - Tensor space semantics
   - Game-Theoretic Pragmatics
There’s many views on language:

- cultural artifact
- a fixed system of preordained rules ("proper grammar")
- communication system
- system of signs

Cognitive Turn (Chomsky 1957, 1965)

Language is an aspect of human cognition.
Computational Questions

- What kind of representations are involved?
  strings, trees, graphs, hypergraphs, . . .

- How can they be manipulated?
  subtree substitution, graph transductions, . . .

- How can this domain knowledge be acquired from input data?
  Gold learning, PAC learning, MAT learning, . . .

- How do speakers use their knowledge about a language in real-time listening and comprehension?
  recursive descent parsing, CKY, Earley, . . .
If You Want to Know More...
Historical Role of Linguistics in Computational Sciences

- Foundations of formal language theory
  Chomsky (1956, 1959); Chomsky and Schützenberger (1963)

- Equivalence of CSGs and linear bounded automata
  Kuroda (1964)

- Initial motivation for tree transducers
  Rounds (1970)

- First parsing algorithms
  Yngve (1955)

- First string processing language (COMIT)
  Yngve (1958)
Lesson 1  Some problems are hard because the model is wrong.
Lesson 2  And some complex problems are just simple problems in disguise.
**Phonological Patterns**

**Phonology** system regulating the distribution of sounds in words

<table>
<thead>
<tr>
<th>Example</th>
<th>Description</th>
<th>Example</th>
<th>Language</th>
</tr>
</thead>
<tbody>
<tr>
<td>word-final devoicing</td>
<td>rat</td>
<td>*rad</td>
<td>German</td>
</tr>
<tr>
<td>intervocalic voicing</td>
<td>nevið</td>
<td>*nefið</td>
<td>Icelandic</td>
</tr>
<tr>
<td>vowel harmony</td>
<td>kauralla</td>
<td>*kaurella</td>
<td>Finnish</td>
</tr>
<tr>
<td>sibilant harmony</td>
<td>tsaanéez</td>
<td>*tʃaanéez</td>
<td>Navajo</td>
</tr>
<tr>
<td>umlaut</td>
<td>mömmu</td>
<td>*mammu</td>
<td>Icelandic</td>
</tr>
<tr>
<td>dissimilation</td>
<td>lunaris</td>
<td>*lunalis</td>
<td>Latin</td>
</tr>
</tbody>
</table>

**Computational Status Quo**

Every known phonological system defines a regular string language.
Finite-State Automata

A **finite-state automaton** (FSA) assigns every node in a string one of finitely many *states*, depending on

- the label of the node, and
- the state of the preceding node (if it exists).

The FSA accepts the string if the last state is a *final state*.

**Cognitive Intuition**

- States are a metaphor for memory configurations.
- Every symbol in the input induces a change from one memory configuration into another.
- Only finitely many memory configurations are needed. Thus the amount of working memory used by the automaton is finitely bounded.
Example: Sibilant Harmony

**Condition:** $\text{j}$ cannot be followed by $s$

**Memory:** 2 distinct states $\checkmark$ and $\text{j}$
Example: Sibilant Harmony

**Condition:** \( \text{ʃ} \) cannot be followed by \( s \)

**Memory:** 2 distinct states \( \checkmark \) and \( \text{ʃ} \)

\[
\begin{array}{c}
\text{start} \quad \checkmark \quad \text{ʃ} \quad \neg \text{ʃ} \\
\end{array}
\]

\[
\begin{array}{c}
\text{ʃ e g o f a} & \text{g e f o s a} \\
\end{array}
\]
**Example: Sibilant Harmony**

**Condition:** \( \emptyset \) cannot be followed by \( s \)  
**Memory:** 2 distinct states \( \checkmark \) and \( \emptyset \)
Example: Sibilant Harmony

**Condition:** ∫ cannot be followed by s

**Memory:** 2 distinct states ✓ and ∫

![Diagram showing the states and transitions for Sibilant Harmony example.]

- Start state: ✓
- Next state: ∫
- Transition: ∫ → ✓
- Transition: ✓ → ∫
- Transition: ∫ → s
- Transition: s → ∫

Example strings:

- ∫ ∫
- ∫ e g o ∫ a

Example output string:

- g e ∫ o s a
Example: Sibilant Harmony

**Condition:** $\int$ cannot be followed by $s$

**Memory:** 2 distinct states $✓$ and $\int$

![Diagram](attachment:image_url)

$\int\int\int$

$\int$ e g o $\int$ a

$g$ e $\int$ o s a
Example: Sibilant Harmony

**Condition:** $\int$ cannot be followed by s

**Memory:** 2 distinct states $\checkmark$ and $\int$

![Diagram showing the transition between states $\int$ and $\sim s$ starting from the initial state $\checkmark$.]
Example: Sibilant Harmony

**Condition:** \( \text{ʃ} \) cannot be followed by \( \text{s} \)

**Memory:** 2 distinct states \( \checkmark \) and \( \text{ʃ} \)

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![Diagram](attachment://diagram.png)

\( \text{ʃ} \) \( \text{ʃ} \) \( \text{ʃ} \) \( \text{ʃ} \) \( \text{ʃ} \) \( \text{ʃ} \)

\( \text{ʃ} \) \( \text{e} \) \( \text{g} \) \( \text{o} \) \( \text{ʃ} \) \( \text{a} \)

\( \text{g} \) \( \text{e} \) \( \text{ʃ} \) \( \text{o} \) \( \text{s} \) \( \text{a} \)
Example: Sibilant Harmony

**Condition:** \( \mathcal{J} \) cannot be followed by \( s \)

**Memory:** 2 distinct states \( \checkmark \) and \( \mathcal{J} \)

![Diagram of Sibilant Harmony](image)
**Example: Sibilant Harmony**

**Condition:** ∫ cannot be followed by s

**Memory:** 2 distinct states ✓ and ∫

```
∫ ∫ ∫ ∫ ∫ ∫ ∫
∫ e g o ∫ a
```

```
ge∫os∫a
```
Example: Sibilant Harmony

**Condition:** \( \mathcal{J} \) cannot be followed by \( s \)

**Memory:** 2 distinct states \( \checkmark \) and \( \mathcal{J} \)

\[
\begin{array}{c}
\mathcal{J} & \mathcal{J} & \mathcal{J} & \mathcal{J} & \mathcal{J} & \mathcal{J} \\
\mathcal{J} & e & g & o & \mathcal{J} & a
\end{array}
\]

\[
\begin{array}{c}
\checkmark & \sqrt{a} & \sqrt{g} & o & \sqrt{a}
\end{array}
\]
Example: Sibilant Harmony

**Condition**: \( \int \) cannot be followed by \( s \)

**Memory**: 2 distinct states \( \checkmark \) and \( \int \)
Example: Sibilant Harmony

**Condition:** ∫ cannot be followed by s

**Memory:** 2 distinct states ✓ and ∫
Example: Sibilant Harmony

**Condition:** \( \mathcal{J} \) cannot be followed by \( s \)

**Memory:** 2 distinct states: ✓ and \( \neg \mathcal{J} \)

\[
\begin{array}{c}
\text{start} \quad \leftarrow \quad \mathcal{J} \\
\mathcal{J} \quad \text{\( \neg \mathcal{J} \)} \\
\mathcal{J} \quad \text{\( \neg s \)} \\
\mathcal{J} \quad \text{\( \neg \mathcal{J} \)} \\
\end{array}
\]
Subregular Phonology

Regular languages are computationally appealing, but
- closure properties do not reflect typology
  union of two phonological systems is not a phonological system
- there is no known learning algorithm for the full class of regular languages

Subregular Hypothesis (Heinz 2010)

Phonological systems define subregular string languages.
Many subregular classes were established a long time, even though they have largely been ignored. (McNaughton and Pappert 1971)

Most of them aren’t suitable for phonology, so linguists had to find new subregular classes:

- strictly piecewise (Rogers et al. 2010)
- interval-based strictly piecewise (Graf under review)
- tier-based strictly local (Heinz et al. 2011)
Example: Sibilant Harmony is Tier-Based Strictly Local

- For every string, induce a substructure containing only s and ⌣
- Induced substructure may not contain the bigram ⌣s

```
∣ ∣ ∣
| | | |
e ∣ i ∣ i
```

```
∣ ∣ ∣
| | | |
e ∣ i ∣ s i
```
Advantages of the Subregular Classes

In contrast to regular languages, these new subregular classes

- have more suitable closure properties,
- are efficiently learnable in the limit from positive text, (Heinz et al. 2012)
- share a lattice-structured grammar space.

They also have applications outside of language, e.g. robotics. (Chandlee et al. 2012)

First Take-Home Message

If you’re currently working with regular languages, one of the weaker classes we have identified may suffice.
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one of the weaker classes we have identified may suffice.
Factorizing Syntax

Syntax system regulating the distribution of words in sentences

(1) Who did you say John likes?
(2) Who did you say that John likes?
(3) Who did you say likes John?
(4) * Who did you say that likes John?

Syntax is Very, Very Complex

When viewed as string languages, natural languages are parallel multiple context-free languages (PMCFL; Kobele 2006).

\[
\text{REG} \subset \text{DCFL} \subset \text{CFL} \subset \text{TAL} \subset \text{MCFL} \subset \text{PMCFL} \subset \text{CSL}
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REG ⊂ DCFL ⊂ CFL ⊂ TAL ⊂ MCFL ⊂ PMCFL ⊂ CSL
The Trouble with PMCFLs

PMCFs have many downsides:
- complex formalism, hard to reason about
- hard recognition problem (although PTIME)
- no useful learnability results

The Cognitive Conundrum

If PMCFs are an accurate model of natural language syntax, then how come humans
- learn syntax easily from little data, and
- can produce and understand sentences in real-time?
A Modular Solution

- Syntax is actually much simpler than it seems.
- The complexity arises from the interaction of two finite-state components:
  - **Derivations** a set of abstract structures generated by a regular tree grammar (≈ CFG)
  - **Interpretation** a macro tree transducer that constructs the pronounced strings from the derivations
- Since the interpretation is fixed across languages, syntax can be reduced to regular tree grammars/CFGs.
Example: Output Tree
Example: Much Simpler Derivation

```
Move
  |
Merge
  a
  Move
    |
    Merge
    b
    Move
    |
    Merge
    c
    Move
    |
    Merge
    a
    Move
    |
    Merge
    b
    Move
    |
    Merge
    c
    Merge
    a
    Merge
    b
    c
```
Transderivational constraints are optimization constraints: structure $X$ is well-formed only if there is no better choice $Y$.

These were believed to be intractable for syntax.

**But:** actually linear tree transductions on derivations $\Rightarrow$ computable in linear time! (Graf 2013)

**Second Take-Home Message**

- Decomposition/Modularization simplifies complex systems.
- Simpler representations allow for efficient implementations.
One of Many Application: Transderivational Constraints

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Dealing With Syntactic Constraints

Theorem (Graf 2011)

*Every syntactic constraint can be precompiled into the grammar.*

1. Every syntactic constraint can be expressed as a formula of **monadic second-order logic** (MSO).
2. Every MSO formula can be converted into an equivalent bottom-up tree automaton.
3. Every bottom-up tree automaton can be precompiled into the grammar.

**Question**

Is there a significant blow-up in the size of the grammar?
Dealing With Syntactic Constraints

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Every syntactic constraint can be precompiled into the grammar.

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Question

Is there a significant blow-up in the size of the grammar?
What we Already Know

- The size of the new grammar is **linearly** bounded by the size of the original grammar.
- But the factor grows **polynomially** in the size of the automaton.
- Each quantifier alternation in the MSO formula may induce an **exponential blow-up** in the size of the automaton.
- **But:** syntactic constraints do not need full MSO, first-order logic suffices.

Research Project

- What is the conversion complexity for (fragments of) first-order logic?
- What is the bound on the size of the automata?
Parallel Parsing

- Humans parse sentences in real-time (= faster than linear).
- Yet our current grammar formalisms display horrible serial parsing performance:
  - CFG: $O(n^3)$
  - TAG: $O(n^6)$
  - $k$-MCFG: $O(n^{3k})$

- But **parallel parsing algorithms improve speed** significantly for CFGs:

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- Can we reduce the number of processors and stay linear?
- Can we generalize these algorithms from CFGs?
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More Parsing

- CFG parsing can be treated as Boolean matrix multiplication.
- In theory this improves efficiency only marginally to $O(n^{2.7\ldots})$.
- But there’s a practical advantage: you can reuse very efficient code for matrix multiplication!

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- Are Boolean tensor spaces the analog for MCFG?
- Can we reuse tensor space algorithms?
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Tensor space semantics

- New idea: word meanings as vectors in tensor spaces
- But linguists care about how sentence meaning arises from combining word meanings.
- **Greg Kobele**: meaning composition in PTIME

**Example**

- every: \( \lambda f_{e,t} \lambda g_{e,t} \cdot \forall x[f(x) \to g(x)] \)
- boy: \( \lambda x_e. \text{boy}(x) \)
- slept: \( \lambda x_e. \text{slept}(x) \)

\[
\text{every boy slept} = \forall x[\text{boy}(x) \to \text{slept}(x)]
\]

**Research Project**

- What are the tensor space analogs of our logical combinators?
- Do they preserve PTIME complexity?
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Example

\[
\text{every } \lambda f_{\langle e, t \rangle} \lambda g_{\langle e, t \rangle} \cdot \forall x [f(x) \rightarrow g(x)] \\
\text{boy } \lambda x_e . \text{boy}(x) \\
\text{slept } \lambda x_e . \text{slept}(x) \\
\text{every boy slept } = \forall x [\text{boy}(x) \rightarrow \text{slept}(x)]
\]

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- What are the tensor space analogs of our logical combinators?
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**Pragmatics** study of intended (rather than literal) meaning

**Example**
- Can you pass the salt \(\neq\) physical capability to pass the salt
- I could care less = I don’t care at all

One successful model of pragmatics is bidirectional OT, which is equivalent to **signaling games**.

**Research Project**
- How are signaling games computed?
- How can we integrate them with parsing?
**Pragmatics** study of intended (rather than literal) meaning

**Example**
- Can you pass the salt ≠ physical capability to pass the salt
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One successful model of pragmatics is bidirectional OT, which is equivalent to **signaling games**.

**Research Project**
- How are signaling games computed?
- How can we integrate them with parsing?
The Bigger Picture: Symbiosis

- Computational questions in linguistics give rise to general-purpose methods, techniques and results.
- Linguistics also needs to import know-how from other computational fields to solve many challenges.


