

Graph Transductions and Typological Gaps in Morphological Paradigms

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Prelude: So Many Boring Problems

- ▶ Theoretical linguists obsess about many problems that are boring to mathematical linguists.

Example: Person Case Constraint (PCC; Bonet 1994)

The well-formedness of clitic combinations is contingent on their person specification.

- (1) Roger *le/*me* *leur* a présenté.
Roger 3SG.ACC/1SG.ACC 3PL.DAT has shown
'Roger has shown me/him to them.'

- ▶ The existence of the **PCC is unremarkable**.
 - ▶ captured by bigram model (very simple)
 - ▶ small problem space \Rightarrow no learnability issues

Take-Home Message: Boring = Interesting At Close-Up

- ▶ Boring problems are interesting once we take a closer look.

Why the PCC is Interesting

- ▶ Out of 64 conceivable PCC variants, only 4 are attested.
 - ▶ The attested PCCs form a mathematically natural class.
 - ▶ And the mathematical account extends to seemingly unrelated phenomena in morphosyntax.
-
- ▶ **Moral:** We should **study all linguistic phenomena**, not just the usual suspects.

Technical Insight: Base Orders & Graph Transductions

Morphosyntactic phenomena can be given a natural explanation via **three components**:

- 1 an independently motivated base hierarchy
person, number, adjectival gradation, . . .
- 2 maximally simple graph transductions to modify this hierarchy
- 3 a simple interpretation of the output graphs

Outline

- 1 The *ABA Generalization & Monotonicity
- 2 *ABA Revisited: Graph-Theoretic Approach
 - Application to Pronoun Syncretism
 - Beyond 3-Cell Systems
- 3 Person Case Constraint
- 4 Subregularity of Weakly Non-Inverting Graph Mappings

A Case Study: *ABA in Morphological Paradigms

Syncretism multiple forms built from same base

*ABA Generalization (Bobaljik 2012)

Two paradigmatic cells cannot be syncretic to the exclusion of any intervening cell.

Example: Adjectival Gradation

- (2) a. smart, smarter, smartest (AAA)
- b. good, better, best (ABB)
- c. * good, better, goodest (ABA)

*ABA Across Morphological Paradigms

Example: Pronoun Syncretism (Harbour 2015, 2016)

- | | | | |
|-----|----|------------------------|-----------|
| (3) | a. | mi, ni, ehi (ABC) | Jarawa |
| | b. | n!aa, n!uu, n!uu (ABB) | Damin |
| | c. | ne, ne, e (AAB) | Winnebago |
| | d. | * I, you, I (ABA) | |

Example: Case Syncretism in Russian (Caha 2009)

Case	window.Sg	teacher.Pl	100
Nom	okn-o	ucitel-ja	st-o
Acc	okn-o	ucitel-ej	st-o
Gen	okn-a	ucitel-ej	st-a
Dat	okn-u	ucitel-jam	st-a
Inst	okn-om	ucitel-ami	st-a

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*ABA: A First Account

- ▶ A mapping that produces ABA violates **monotonicity**.

Monotonicity for Pronoun Syncretism

- ▶ Suppose $3 < 2 < 1$ (Zwicky 1977)
- ▶ A function f is **monotonic** iff $x \leq y$ implies $f(x) \leq f(y)$.
- ▶ No monotonic function from $\{1, 2, 3\}$ to $\{A, B, C\}$ can produce ABA!
- ▶ This holds irrespective of the ordering of $\{A, B, C\}$.

Illustrating Monotonicity

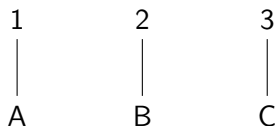
Monotonicity is similar to No Crossing Branches constraint in autosegmental phonology. (Goldsmith 1976)

1	2	3
A	B	C

Patterns:

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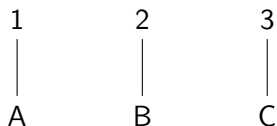
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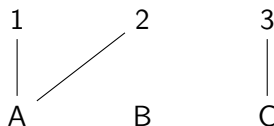
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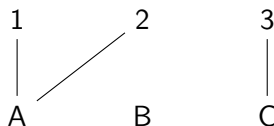
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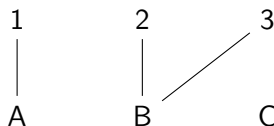
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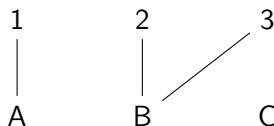
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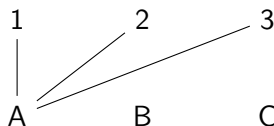
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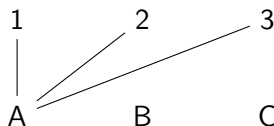
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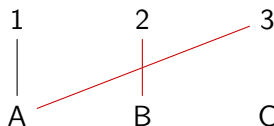
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Why Monotonicity?

- ▶ Why should spell-out functions be monotonic?
- ▶ **Idea:** Monotonicity matters in other areas.
 - ▶ NPI licensing in downward entailing contexts
 - ▶ Direction-preserving nature of movement in MGs
- ▶ **But:** Those are just-so stories.
 - ▶ Downward entailingness is neither necessary nor sufficient.
 - ▶ Various MG movement types are not direction-preserving.
- ▶ Maybe monotonicity is not the best characterization...

A More General View: Graph Structure Preservation

The General Idea

- ▶ *ABA is about structure preservation.
- ▶ Syncretism is modification of a base graph.
- ▶ Modification must not contradict orderings of base graph.

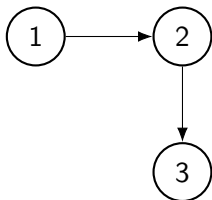
Definition (Weakly Non-Inverting Graph Mappings)

- ▶ Given input graph G and output graph G'
 - ▶ $x \triangleleft y$ iff y is reachable from x in G ,
 - ▶ $x \blacktriangleleft y$ iff y is reachable from x in G' .
- ▶ A mapping from G to G' is **weakly non-inverting** iff
$$x \triangleleft y \wedge y \blacktriangleleft x \rightarrow x \blacktriangleleft y$$

Weakly Non-Inverting Graph Mappings

- ▶ Since we want graphs to encode hierarchies, they must be *weakly connected*: ignoring the direction of arrows, all nodes are mutually reachable.
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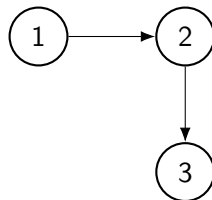
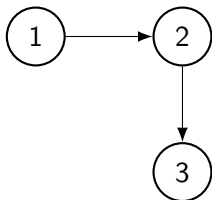
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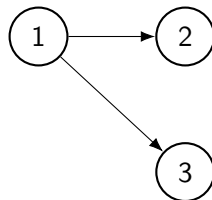
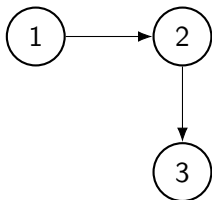
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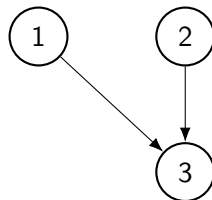
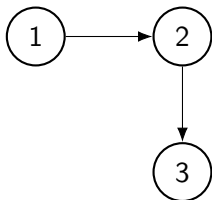
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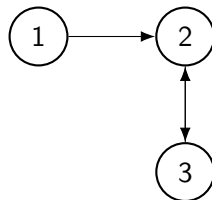
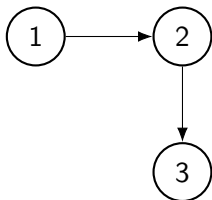
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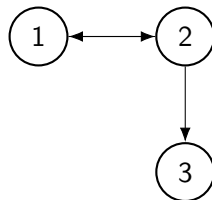
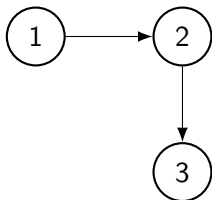
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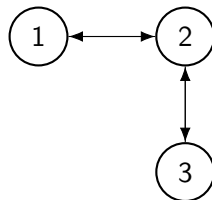
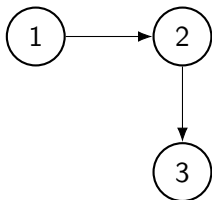
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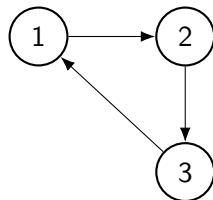
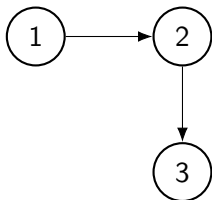
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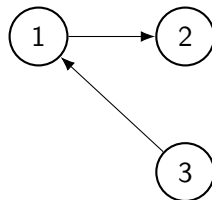
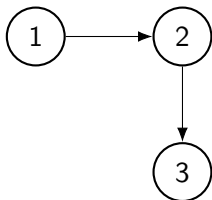
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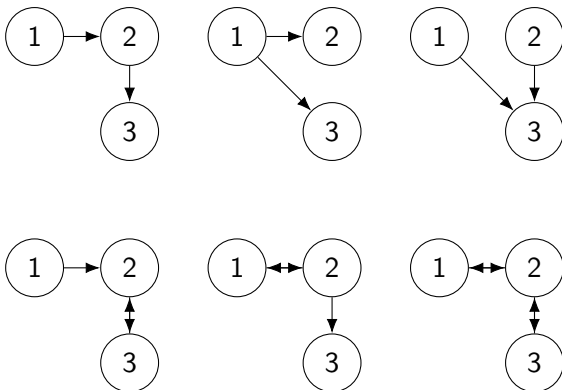
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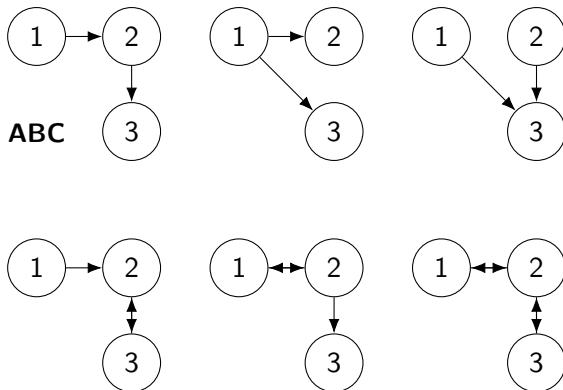
Graphs and Syncretism

- ▶ Suppose two cells may be syncretic iff they are mutually reachable in a graph.
- ▶ Then the previous set of graphs describes the **class of attested syncretisms**.



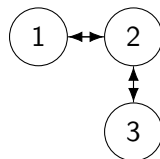
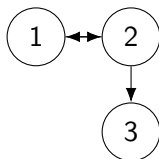
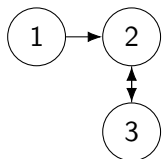
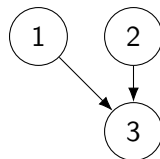
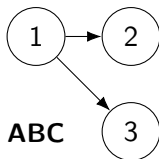
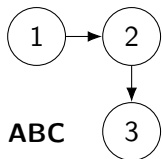
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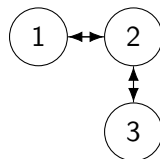
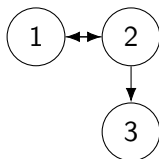
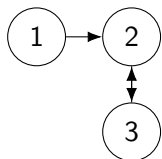
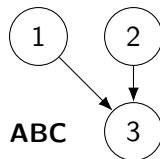
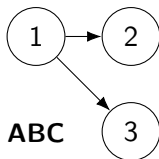
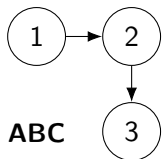
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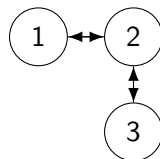
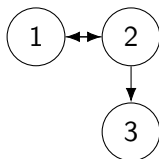
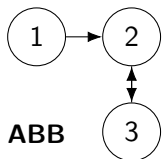
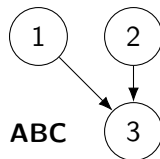
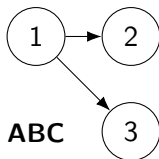
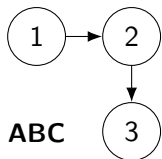
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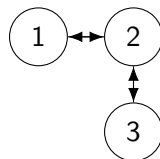
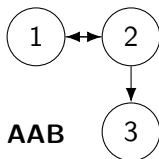
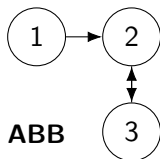
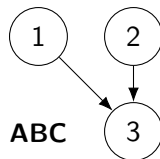
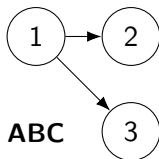
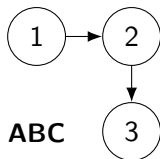
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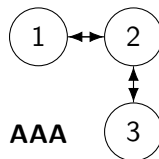
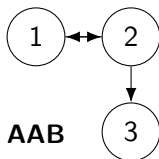
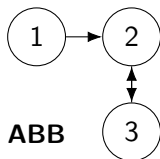
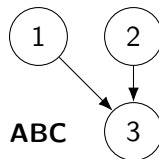
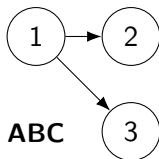
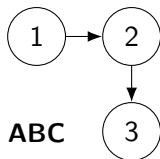
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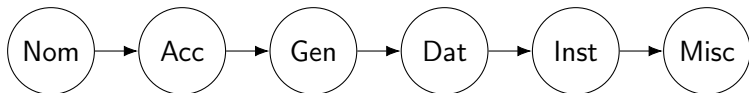


Scaling to Larger Systems

- ▶ The previous account works for any 3-cell paradigm.
- ▶ Some morphosyntactic phenomena have many different cells.
case syncretism, noun stem allomorphy
- ▶ For those, weakly non-inverting maps **incorrectly allow ABA!**

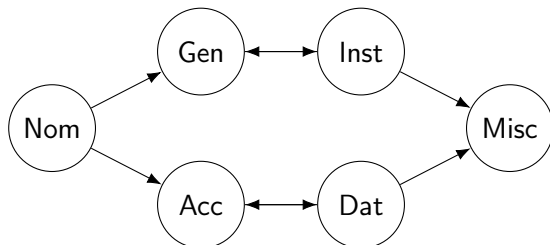
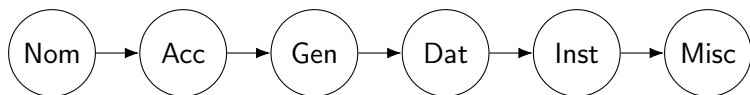
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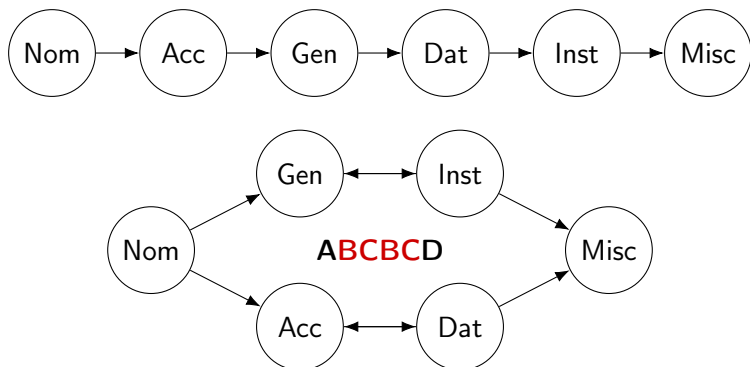
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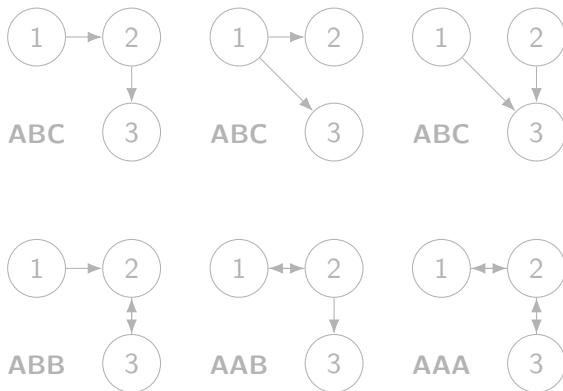


The Fix: A Stronger Connectivity Requirement

- ▶ Weakly non-inverting maps still obey *ABA if output graphs must be **connected**:

$$\forall x, y [x \blacktriangleleft y \vee y \blacktriangleleft x]$$

- ▶ We can also assume this for 3-cell paradigms.

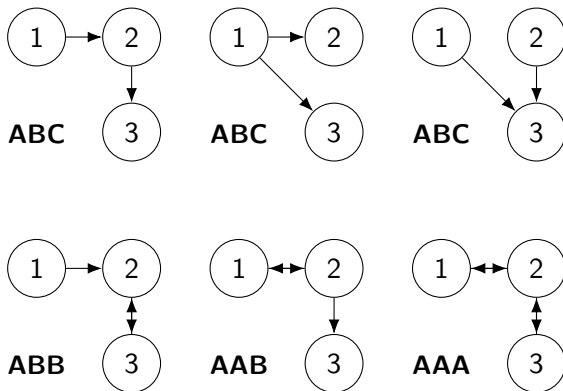


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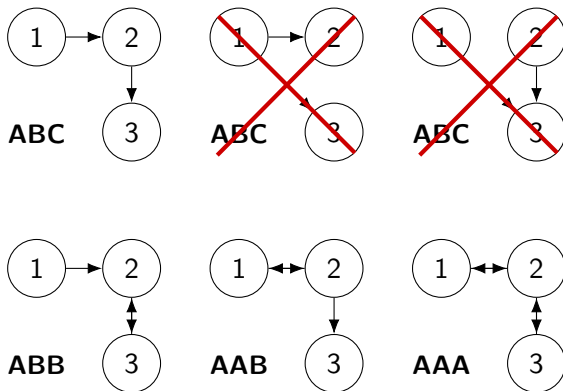


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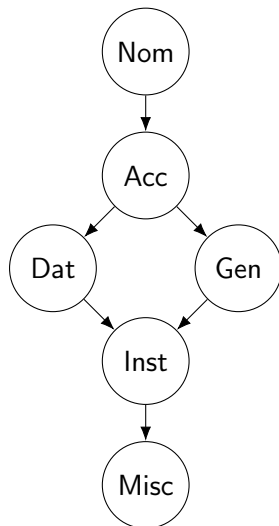
A Note on Case Syncretism

- ▶ Attested syncretisms of **Acc & Dat** and **Acc & Gen** in Icelandic (Harðarson 2016)

Example

- ▶ drottning- \emptyset /-u/-ar/-u 'daughter'
- ▶ arm-ar/-a/-a/-um 'arm'

- ▶ Modified case hierarchy as base (Blake 2001)
- ▶ **Prediction:** some language has Acc & Dat and Gen & Inst, or Acc & Gen and Dat & Inst



Interim Summary

- ▶ Weakly non-inverting graph mappings preserve aspects of the base order.
- ▶ This structure preservation derives the *ABA generalization.
- ▶ Some ad hoc stipulations are still needed in certain cases.
- ▶ Those reflect aspects of the grammatical machinery, which the graph-theoretic view abstracts away from.

Phenomenon	Target graph	Constraints
Pronoun allomorphy	(weakly) connected	none
Adjectival gradation	(weakly) connected	$2 \blacktriangleleft 1 \rightarrow 3 \blacktriangleleft 1$
Case syncretism	connected	none
Noun stem suppletion	connected	$\exists z[z \blacktriangleleft x] \rightarrow (x \blacktriangleleft y \leftrightarrow y \blacktriangleleft x)$

The Graph-Theoretic View of the Person Case Constraint

- ▶ There are **four attested variants** of the PCC:

S(trong)-PCC DO must be 3.

(Bonet 1994)

U(ltrastrong)-PCC DO is less prominent than IO,
where 3 is less prominent than 2,
and 2 is less prominent than 1.

(Nevins 2007)

W(eak)-PCC 3IO combines only with 3DO.

(Bonet 1994)

M(e first)-PCC If IO is 2 or 3, then DO is not 1.

(Nevins 2007)

- ▶ But symmetric variants have been discovered.
(Stegovec 2016)
- ▶ This looks like a mess!

A More Systematic Perspective (Walkow 2012)

$IO\downarrow/DO\rightarrow$	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	*	NA

U-PCC

$IO\downarrow/DO\rightarrow$	1	2	3
1	NA	*	✓
2	*	NA	✓
3	*	*	NA

S-PCC

$IO\downarrow/DO\rightarrow$	1	2	3
1	NA	✓	✓
2	✓	NA	✓
3	*	*	NA

W-PCC

$IO\downarrow/DO\rightarrow$	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	✓	NA

M1-PCC

Graph-Theoretic Unification

Generalized PCC

y must not be
reachable from x .

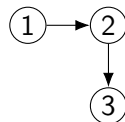
Standard PCCs:

$y = IO$, $x = DO$

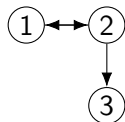
Symmetric PCCs:

$y = DO$, $x = IO$

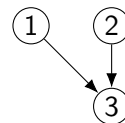
U	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	*	NA



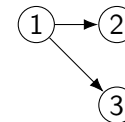
S	1	2	3
1	NA	*	✓
2	*	NA	✓
3	*	*	NA



W	1	2	3
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2	✓	NA	✓
3	*	*	NA

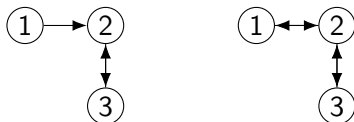


M1	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	✓	NA



Extending the PCC

- ▶ What about the other two graphs?



- ▶ The first is currently unattested.
- ▶ The second blocks all clitic combinations, as in Cairene Arabic. (Shlonsky 1997:207, Walkow p.c.)
- ▶ So 5 out of 6 graphs are attested PCCs.

Summary of Relevant Graph Classes

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PCC	w-connected	$3 \blacktriangleleft 2 \rightarrow 3 \blacktriangleleft 1$

- ▶ This is a fairly natural characterization.
- ▶ Generative accounts are too fine-grained, only mathematics allows for this unification.

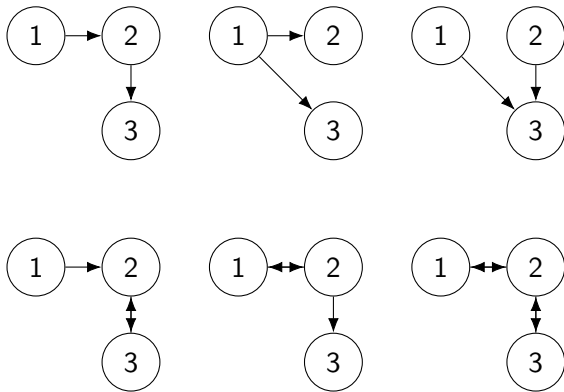
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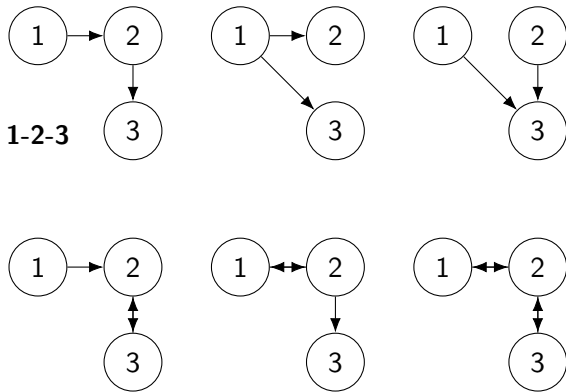
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- ▶ From a certain perspective, being weakly non-inverting is computationally simple.
- ▶ All the required graphs can be represented as strings.



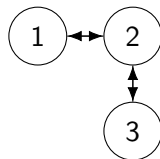
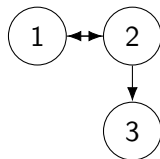
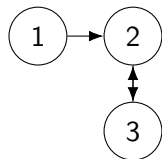
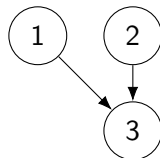
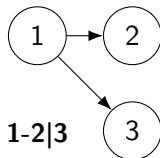
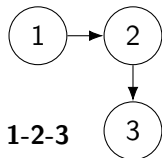
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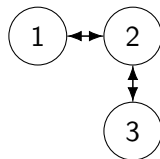
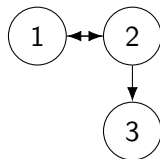
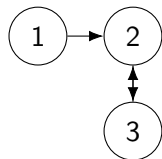
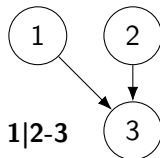
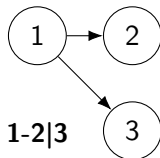
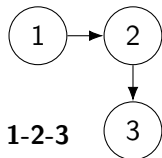
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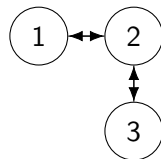
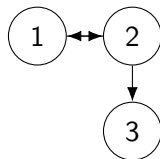
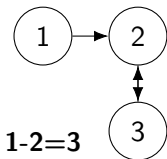
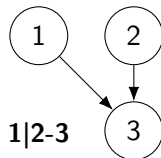
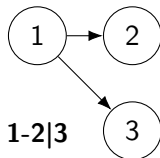
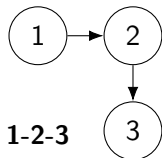
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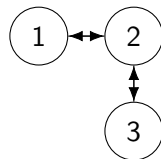
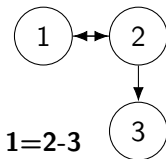
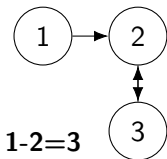
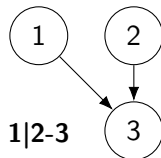
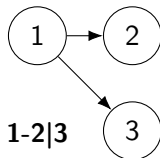
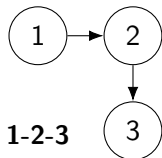
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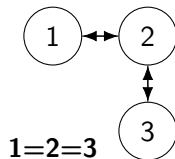
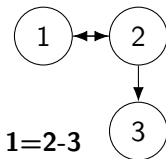
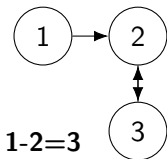
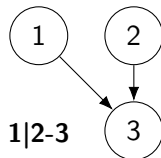
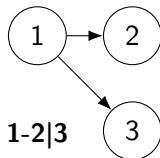
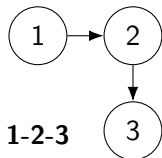
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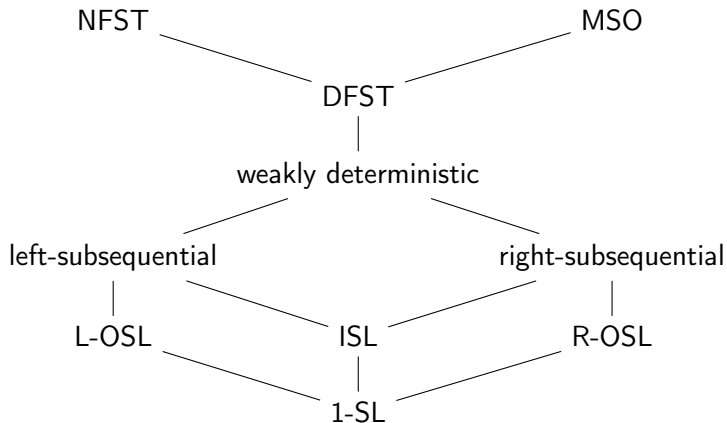
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Subregular String Mappings

For weak mappings, we look at **subregular string transductions**.



1-SL Mappings

- ▶ 1-SL relations/maps = state-free N/DFST transductions
- ▶ This is sufficient to compute weakly non-inverting maps over the string representations.



- ▶ Switching the order of **ab** requires memorizing **a** \Rightarrow not 1-SL

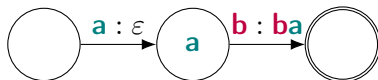


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Extrapolating to Graph Mappings

- ▶ Of course 1-SL could reverse direction with a symbol for inverse order (\leftarrow) in the string representations.
- ▶ But strings capture the idea that **reversal is costly**, cf.:
 - ▶ impossibility of local rotations with LBUTTs
 - ▶ markedness of metathesis in phonology
- ▶ Current graph transductions don't capture this, deleting and adding edges is cheap.
- ▶ Maybe we need a different view of graph transductions, or a more restricted transduction class (DAG, tree, string).
- ▶ **Bottom line:** class of attested patterns should reduce to computational simplicity

Conclusion

- ▶ Graphs generalize across domains of morphosyntax
 - ▶ Base hierarchy
 - ▶ Maximally simple transduction (1-SL)
- ▶ Approach could be about markedness rather than well-formedness (weaker typological claim)
- ▶ **But:** a lot of work still to be done
Gender Case Constraint, inverse marking, resolved agreement, . . .

Two General Points

- ▶ More work on subregular graph transductions, please!
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