# The Syntactic Algebra of Adjuncts

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#### The Talk in a Nutshell

Neo-Davidsonian semantics: adjuncts are interpreted as conjuncts

- (1) a. John danced beautifully.
  - b.  $\exists e[\operatorname{dance}(e, \operatorname{john}) \land \operatorname{beautiful}(e)]$

#### Take-Home Message

- Adjuncts behave syntacticially like logical and, too.
- Properties of adjuncts give rise to grammaticality inferences.
- Adjunct Island Constraint and parasitic gaps follow from these inferences.

### Outline

- A Theory-Neutral Definition of Adjuncts
- Adjuncts and Grammaticality Inferences
  - Characterizing Adjunct Languages
  - Adjunct Algebras
- 3 Empirical Implications
  - Deriving the AIC
  - Parasitic Gaps
  - Some Open Problems
- Conclusion

## Adjuncts in the Literature

#### Adjuncts . . .

- have no special operational status (CG; Cinque 1999),
- are pair-merged (Chomsky 1995),
- are late-merged (Stepanov 2001),
- are inserted but not merged immediately (Hunter 2012),
- involve asymmetric feature checking (Frey and Gärtner 2002),

**Empirical Implications** 

#### Problem

Can we abstract away from these details? Properties that hold of every conceivable implementation?

# Two Surface Properties of Adjuncts

### Optionality

**Defining Adjuncts** 

Adjuncts can be omitted.

(Obviously) I will (easily) ace this ((very) challenging) exam (because I (really) am that smart).

#### Independence

Independently well-formed adjuncts can be combined.

- (3) a. Obviously I will ace this exam.
  - b. I will easily ace this exam.
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Phrase marker a is an **Adjunct** iff it is optional and independent.

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What do these properties tell us about grammars with Adjuncts? What is the general shape of the **generated language?** 

Let s and t be (multi-dominance) trees.

Then t is an **Adjunct extension** of s for grammar G (s < t) iff t is the result of inserting one or more Adjuncts of G in s.

- Obviously I will ace this exam < G
  - Obviously I will easily ace this exam
- I will ace this exam  $<_G$  Obviously I will easily ace this exam
- Obviously I will ace this exam  $\not \subset_G$  I will easily ace this exam
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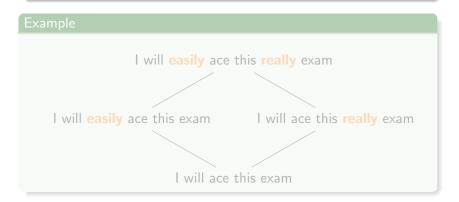
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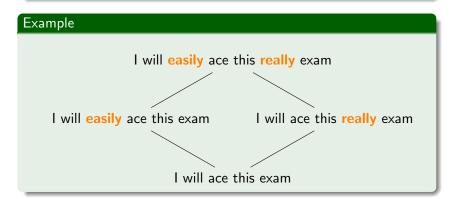
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#### Theorem (Optionality Closure)



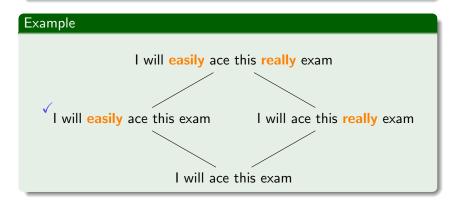
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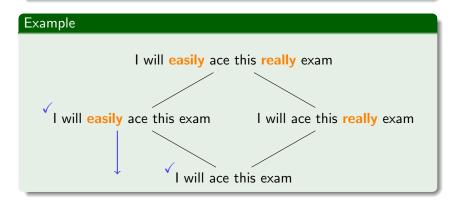
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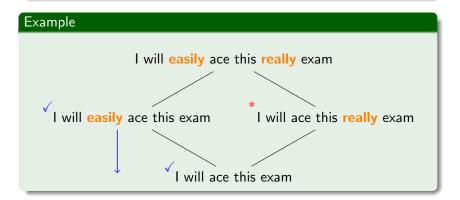
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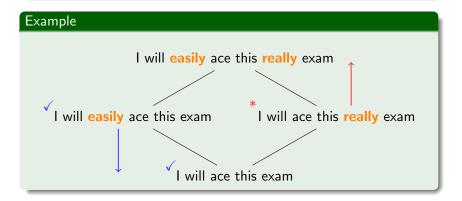
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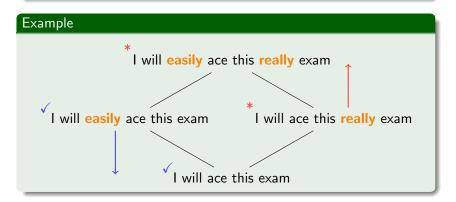
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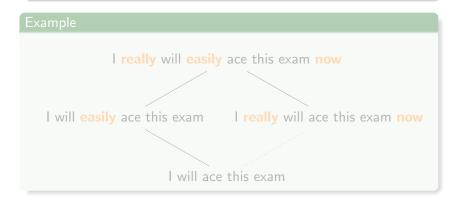
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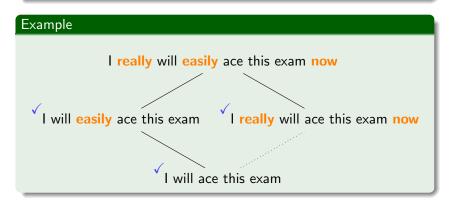
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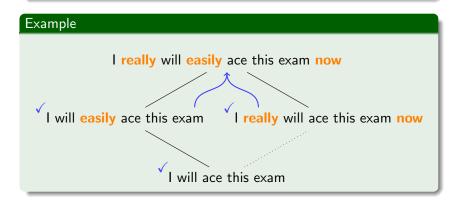
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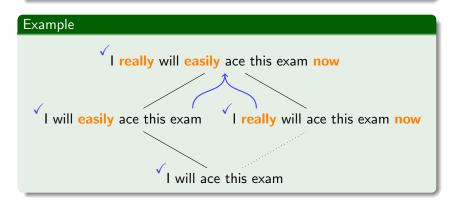
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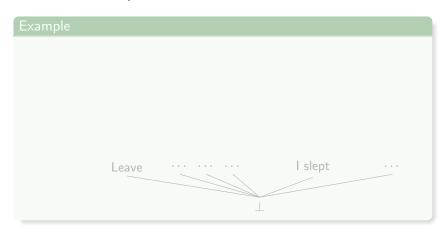
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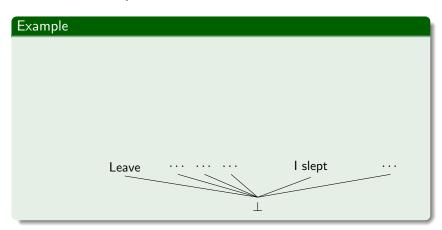
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- Order the set of all possible (not necessarily grammatical) trees by G's Adjunct extension relation.
- Add a dummy element  $\perp$  at the bottom.

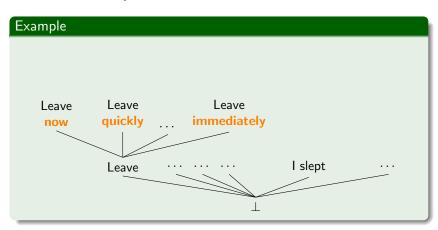


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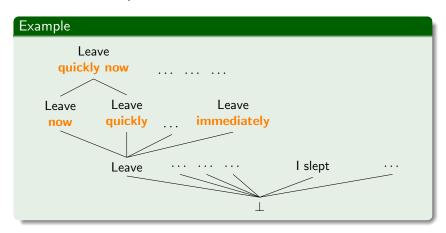


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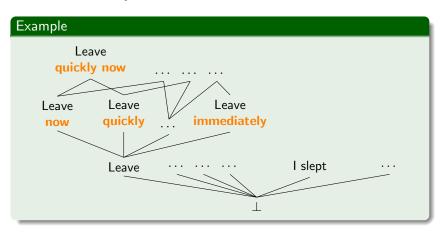
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## Adjunct Languages are Collections of Ideals

#### Definition (Ideal)

A non-empty subset S of a poset  $\langle A, \leq \rangle$  is an **ideal** iff

- for every  $x \in S$ ,  $y \le x$  implies  $y \in S$ , and
- for all  $x, y \in S$  there is some  $z \in S$  such that x < z and y < z.

#### $\mathsf{Theorem}$

**Defining Adjuncts** 

The tree language generated by grammar G is a collection of ideals over the Adjunct Algebra induced by G (modulo  $\perp$ ).

## Interim Summary

Any implementation of Adjunction that captures Optionality and Independence yields a grammar formalism where

- ullet grammaticality is downward entailing with respect to  $<_G$ ,
- ullet ungrammaticality is upward entailing with respect to  $<_G$ ,
- V grammaticality is preserved under "fusion".

#### Parallels to Logical And

- Grammaticality is Downward Entailing  $a \wedge b = 1$  implies a = 1
- Ungrammaticality is Upward Entailing a = 0 implies  $a \wedge b = 0$
- Grammaticality is Preserved Under "Fusion"  $a \wedge b = 1$  and  $a \wedge c = 1$  jointly imply  $a \wedge b \wedge c = 1$

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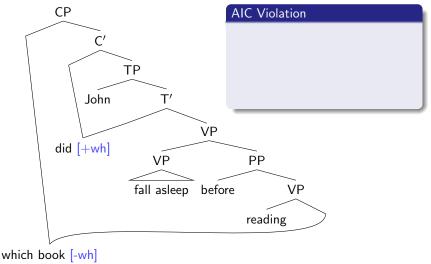
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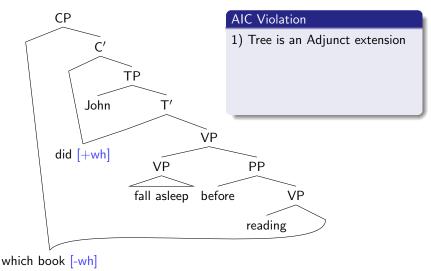
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The AIC follows from optionality closure and feature checking.



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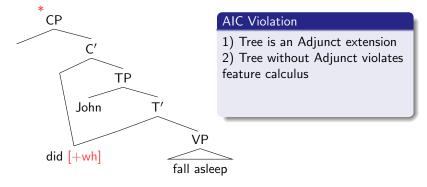
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# Deriving the AIC

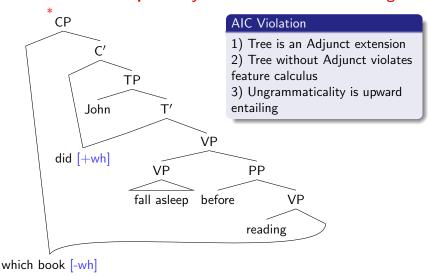
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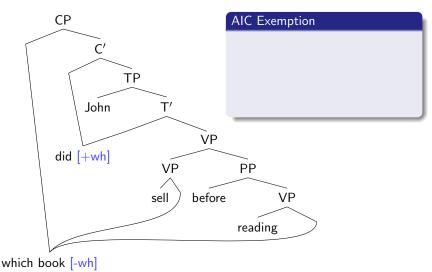


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PGs piggyback on a mandatory feature checker.

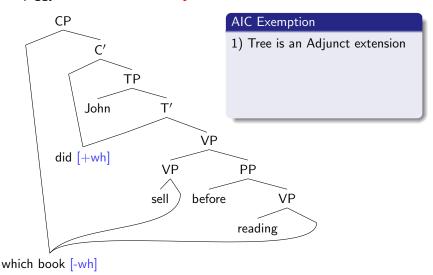


**Empirical Implications** 

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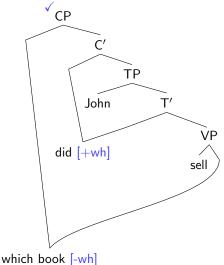
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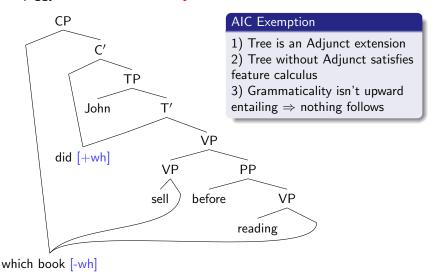


#### **AIC Exemption**

- 1) Tree is an Adjunct extension
- 2) Tree without Adjunct satisfies feature calculus

**Defining Adjuncts** 

PGs piggyback on a mandatory feature checker.



## Why Parasitic Gaps are Idempotent

Multiple PGs may piggyback on a single mover.

Which movie did John whilst mocking throw in the trash after watching?

#### Follows from independence closure

- a. Which movie did John whilst mocking throw in the (5) trash?
  - b. Which movie did John throw in the trash after watching?

## Not All adjuncts are Adjuncts

**Defining Adjuncts** 

Some adjuncts can be extracted from (Truswell 2007):

(6) Which car did John drive Mary crazy trying to fix?

Truswell's event-based generalization  $\approx$ non-island adjuncts more tightly integrated semantically

	sem-argument	sem-adjunct
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#### V2 in German

- (7)a. Gestern hat der Hans die Maria geküsst. vesterday has the Hans the Maria kissed 'Yesterday, John kissed Mary.'
  - b. Hat der Hans die Maria geküsst? has the Hans the Maria kissed 'Did John kiss Mary?'
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#### Possible Answers

- V2 is post-syntactic and thus irrelevant for Optionality.
- V1 is grammatical, but restricted by discourse factors (e.g. telling jokes).

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#### Summary

- Adjuncts characterized by Optionality and Independence
- enforces certain grammatical inferences
  - ↓ grammaticality is preserved under Adjunct removal
  - † ungrammaticality is preserved under Adjunct insertion
  - V grammaticality is preserved under Adjunct combination
  - ⇒ AIC falls out naturally, yet allow for parasitic gaps

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## Constraints through Operations

Constraints and operations are **closely connected**.

#### Theorem (Graf 2011; Kobele 2011)

A constraint can be expressed via Merge iff it can be computed using only a finitely bounded amount of working memory.

- Intuition: Use feature calculus to emulate how information flows through the tree during computation
- Doable for almost all constraints from the syntactic literature
- Relies on symmetry of c-selection (category features & selection features)

head-argument relation ≡ information pipeline

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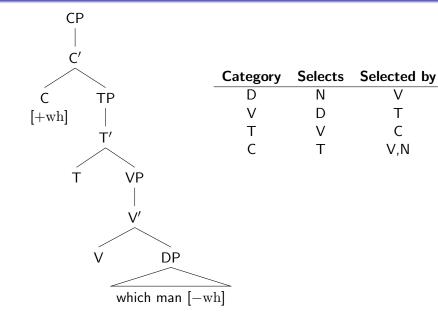
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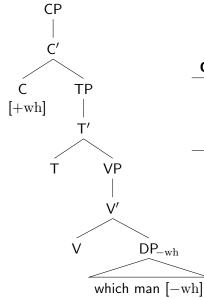
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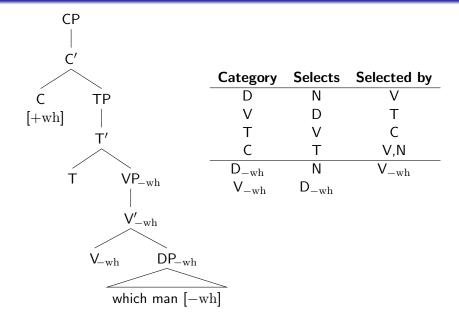
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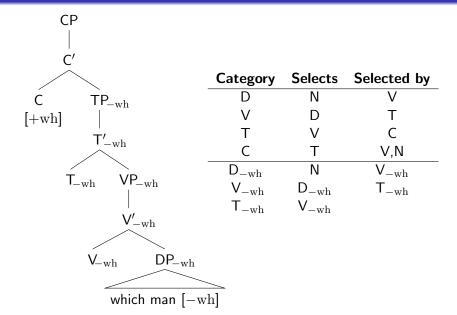
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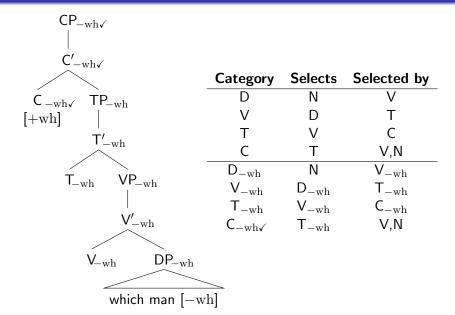


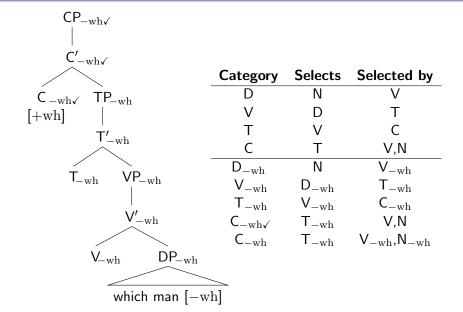


Category	Selects	Selected by
D	N	V
V	D	T
Т	V	C
C	T	V,N
$\overline{D_{-\mathrm{wh}}}$	N	









## Adjuncts: The Price of Freedom

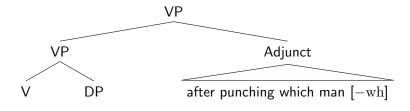
- Adjuncts very free due to Optionality and Independence
- Freedom reflected in feature calculus, limits information flow
   feature calculus cannot emulate all constraints correctly

#### Semi-Permeability

- Information flow into Adjuncts reliable
  - ⇒ Adjuncts can put restrictions on shape of tree (cf. parasitic gaps)
- Information flow out of Adjuncts unreliable
  - ⇒ Adjuncts cannot be depended on

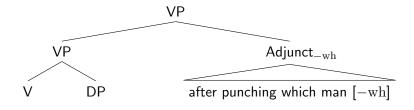
#### Adjunct ≡ black hole

#### Adjunction as Asymmetric Selection



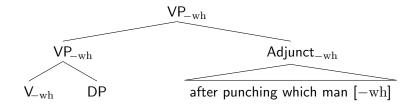
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Adjunct	V	_
V	D	Т

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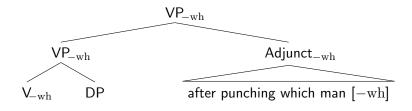
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V	D	T
Adjunct_wh	V	

#### Adjunction as Asymmetric Selection



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$\overline{Adjunct_{-\mathrm{wh}}}$	$V_{-\mathrm{wh}}$	
$V_{-\mathrm{wh}}$	D	$T_{-\mathrm{wh}}$

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$V_{-\mathrm{wh}}$	D	$T_{-\mathrm{wh}}$