# Constraints Emerge from Merge 

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## Take-Home Message

## Questions

- How do constraints fit into syntax?
- What are their properties?


## This Talk

- Constraints are closely related to operations.
- A formal perspective makes this connection explicit.
- Linking constraints to operations limits their power and makes new empirical predictions.


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## Outline

(1) The Status of Constraints in Linguistics
(2) Formal Concepts

- Minimalist Grammars
- Constraints as Logical Formulas
(3) Results
- Main Result: Constraints $\equiv$ Merge
- Corollary: Uniformity of Constraint Classes
- Linguistic Implications

4) Are MSO-Constraints Enough? A Look at Binding

- Syntactic Binding: No Semantics, No Discourse
- Computing Principle B
- English
- American Sign Language (ASL)
(5) Conclusion \& Outlook


## Constraints and Operations

The two essential tools of linguistics: Constraints and Operations

| GB | Minimalism | TAG |
| :---: | :---: | :---: |
| HPSG | EST | CCG |
| LFG | Gov. Phon. | SPE |
| OT | Harm. Serial. |  |

$\qquad$ $\rightarrow$ operations

## Some Naive Questions

- What distinguishes constraints from operations?
- Is one superior to the other?
(Kisseberth 1970; Brody 2002; Epstein and Seely 2002)
- How do they interact?
(Epstein et al. 1998; Bailyn 2010)
- Does it make a difference for empirical work? (Pullum and Scholz 2001, 2005)


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## Müller-Sternefeld Hierarchy of Constraints

- Representational (output filters/interface conditions) stated over phrase structure trees
- ECP: "Every trace is properly governed at LF."
- Full Interpretation: "No uninterpretable features at LF."
- Linearizability: "All leaves are linearly ordered at PF."
- Derivational stated over derivations
- Relativized Minimality: " $X$ moves to $Z$ only if there is no $Y$ closer to $Z$ that could have moved there."
- Transderivational (economy conditions; cf. OT) picks optimal tree out of set of competing candidates
- Shortest Derivation Principle: "Given a set of competing derivations, pick the one with the fewest instances of Move."

MS-Hierarchy (Müller and Sternefeld 2000; Müller 2005)
representational < derivational < transderivational

## Shortcomings of the MS-Hierarchy

- based on case studies of specific constraints
$\Rightarrow$ lack of generality
- no clear characterization of power of constraints
- Why do constraints exist in the first place?

What does this tell us about language?

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## Minimalist Grammars (MGs)

- formalization of Minimalist syntax without Agree/phases (Stabler 1997)
- many extensions to make them more faithful (Frey and Gärtner 2002; Graf 2012b; Kobele 2002, 2012; Stabler 2003, 2006, 2011, among others)
- original version suffices for our purposes


## Core Idea of MGs

- Operations: Merge and Move
- lexical items annotated with features
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## Merge: Example 1

## Assembling [DP the men]

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- Merge triggered by features of opposite polarities
- Label points to branch leading to projecting head
- Head must have a category feature ( $\mathrm{N}^{-}, \mathrm{D}^{-}, \mathrm{V}^{-}, \ldots$ )
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## Assembling [vp the men like which men]

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- the and men merged as before
- same steps for which men
- like selects which men
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## Merge: Example 2 [cont.]



## Move (Multi-Dominance Implementation)

Assembling "which men do the men like?"


- Merge do
- Move triggered by features of opposite polarity
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## Derivation Trees with Move



## MG Summary

An MG is given by a set of feature-annotated lexical items. It generates all (multi-dominance) trees that are CPs built from the available lexical items.

Example


Generated sentences: The men like the men. Which men do the men like. Which men do like the men.

## Formalizing Constraints

Constraint statement $c$ that must be satisfied in order for a tree to be well-formed
Logical Formula statement $\phi$ that must be satisfied in order for a structure to be a model of $\phi$
$\Rightarrow$ Constraints $\equiv$ Logical Formulas (Kracht 1995; Rogers 1998; Potts 2001; Pullum 2007)

## First-Order Logic for Trees (FO)

    \(\exists, \forall\)
    I(x)
    \(\triangleleft\)
    \(\approx\)
    variables $x, y, z, \ldots$
$\wedge, \vee,-, \rightarrow, \leftrightarrow$ and, or, not, implies, iff
there is, for all
$x$ has label /
dominance
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## Example: Stating Principle A

## Principle A (slightly simplified)

Every anaphor must be c-commanded by some DP within its binding domain.

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\begin{gathered}
\text { anaphor }(x) \leftrightarrow \operatorname{himself}(x) \vee \operatorname{herself}(x) \vee \operatorname{itself}(x) \\
\text { c-com }(x, y) \leftrightarrow \neg(x \approx y) \wedge \neg(x \triangleleft y) \wedge \forall z[z \triangleleft x \rightarrow z \triangleleft y]
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" $x$ is an anaphor iff $x$ is labeled himself
or $x$ is labeled herself or $x$ is labeled itself."

$$
\mathrm{c-com}(x, y) \leftrightarrow \neg(x \approx y) \wedge \neg(x \triangleleft y) \wedge \forall z[z \triangleleft x \rightarrow z \triangleleft y]
$$

"x c-commands $y$ iff
it is not the case that $x$ and $y$ are the same node, and it is not the case that $x$ dominates $y$, and every $z$ that dominates $x$ also dominates $y$."

## Set Quantification: Talking About Domains

Problem: domains are sets of nodes $\Rightarrow$ move beyond FO
Monadic Second-Order Logic for Trees (MSO)
Extension of FO with

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\begin{array}{ll}
X, Y, Z, \ldots & \text { set variables } X, Y, Z, \ldots \\
Y P(X) & \text { set } X \text { is a YP } \\
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## Principle A (slightly simplified)

Every anaphor must be c-commanded by some DP within its binding domain.

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\forall x[\operatorname{anaphor}(x) \rightarrow & \exists y[\mathrm{c}-\operatorname{com}(y, x) \wedge \mathrm{DP}(y) \wedge \\
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## Further Remarks on the Power of MSO

MSO provides good fit for syntactic constraints, but not perfect:

- can state many unnatural constraints (too strong)
- cannot state some natural constraints (too weak)


## Definable Unnatural Constraints

- Symmetric analog: "Every anaphor c-commands a DP",
- Unrelated properties: "The subject is plural if T is [+past]",
- Analogs from phonology: "The total number of nodes is even"


## Undefinable Natural Constraints

- "Subtrees A and B are identical"
$\Rightarrow$ problematic for ellipsis as deletion under (syntactic) identity
- "The meaning of subtree $A$ implies the meaning of $B$ "
$\Rightarrow$ problematic for semantic constraints in syntax


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## Computing MSO-Constraints

## MSO \& Tree Automata (Thatcher and Wright 1968; Doner 1970)

A constraint is MSO-definable iff it can be computed by a (finite-state) tree automaton.

A tree automaton

- assigns each node in a tree one of finitely many states, and
- accepts the tree iff its root is assigned a final state.



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## Section Summary

## Minimalist Syntax

- Formalized in terms of MGs
- Operations: Merge and Move (Agree omitted for convenience)
- Triggered by checking features of opposite polarities


## Constraints

- Constraints $\equiv$ MSO formulas $\equiv$ tree automata
- MSO can talk about both nodes and sets of nodes $\Rightarrow$ expressive enough for syntax
- Tree automata compute constraints in a local way using finitely bounded number of states ( $\approx$ working memory) $\Rightarrow$ cognitive plausibility


## Outline

(1) The Status of Constraints in Linguistics
(2) Formal Concepts

- Minimalist Grammars
- Constraints as Logical Formulas
(3) Results
- Main Result: Constraints $\equiv$ Merge
- Corollary: Uniformity of Constraint Classes
- Linguistic Implications
(4) Are MSO-Constraints Enough? A Look at Binding
- Syntactic Binding: No Semantics, No Discourse
- Computing Principle B
- English
- American Sign Language (ASL)
(5) Conclusion \& Outlook


## The Central Result

## MSO-Constraints $\equiv$ Merge (Graf 2011; Kobele 2011)

A constraint $C$ can be expressed by an MG iff $C$ is MSO-definable.

## Proof idea

- convert constraint $C$ into tree automaton $A$
- incorporate states of $A$ into feature calculus $\Rightarrow$ "refined" grammar expresses $C$ via Merge



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## Uniformity of Constraint Classes

Reminder: Müller-Sternefeld Hierarchy of Constraints representational < derivational < transderivational

## Formal Result: Uniformity of MSO-Constraints

For every MG

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\text { representational } \equiv \text { derivational } \equiv \text { transderivational }(\equiv \text { local })
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(Graf 2010, 2011, 2012a, b; Kobele 2011)

## Recap: What Just Happened?

- Monadic Second-Order logic as description language:
- powerful enough for stating syntactic constraints
- computable with finite working-memory
- Every MSO-constraint expressible purely through Merge Metaphor: Put memory states into category features
- Corollary: constraint types conflate into one


## The New Perspective on Constraints

- Existence of MSO-definable constraints unsurprising given power of Merge
- But are there really only MSO-constraints in syntax? What would the implications be?


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## Implications for Processing

- derivational $\equiv$ local
solves problem of parsing long-distance dependencies
in a local, incremental manner (cf. Alcocer and Phillips 2012)
- derivational $\equiv$ representational
allows parsing derivations rather than phrase structure trees
$\Rightarrow$ increased performance (Stabler 2012)
correctly predicts processing difficulties (Kobele et al. 2012)


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## Syntactic Binding: No Semantics

- Canonical Binding Theory:
is sentence grammatical with respect to specific reading?
- requires storing referent for each pronoun
- number of pronouns per sentence unbounded
$\Rightarrow$ no upper bound on number of referents
$\Rightarrow$ needs unbounded amount of working memory


## Syntactic Binding (preliminary)

Does a given sentence have some grammatical reading?

## Syntactic Binding: No Semantics

- Canonical Binding Theory: is sentence grammatical with respect to specific reading?
- requires storing referent for each pronoun
- number of pronouns per sentence unbounded
$\Rightarrow$ no upper bound on number of referents
$\Rightarrow$ needs unbounded amount of working memory


## Syntactic Binding (preliminary)

Does a given sentence have some grammatical reading?

## Syntactic Binding: No Discourse

- Discourse-mechanisms arguably not part of syntax $\Rightarrow$ syntax only regulates pronouns that must be syntactically bound (cf. aapaṇ in Marathi; Kiparsky 2002)
- Technical assumption

English has discourse-bound $\operatorname{him}_{d}$ and syntactically bound $h_{i m}$; only the latter is of interest here

## Syntactic Binding (final)

Is there some syntactically grammatical reading?

## Example

(1) a. Every patient said that $\mathrm{he}_{d}$ should sedate him ${ }_{s}$.
b. * Every patient said that he $\mathrm{e}_{s}$ should sedate him ${ }_{s}$.
c. Every patient told some doctor that he ${ }_{s}$ should sedate hims.

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c. Every patient told some doctor that he ${ }_{s}$ should sedate hims. $_{\text {s }}$.

## Principle A is Easy

- already saw how Principle A can be expressed in MSO $\Rightarrow$ SE/SELF anaphors no problem
- What about long distance reflexives?
- Icelandic type: usually allows local binding $\Rightarrow$ like SE/SELF
(2) Jón ${ }_{i}$ segir að María ${ }_{j}$ elski $\quad \operatorname{sig}_{i / j}$. Jon says that Maria loves.subj SE
'Jon says that Maria loves him/herself.'
- Swedish type: no local binding allowed $\Rightarrow$ like pronouns
(3) Generalen $_{i}$ tvingade översten ${ }_{j} \quad \mathrm{PRO}_{j}$ att hjälpa General.the forced colonel.the PRO to help $\operatorname{sig}_{i / * j}$.
SE
'The general forced the colonel to help him(*self).'


## Principle B: Limited Obviation

While Principle A is easy, Principle B is difficult because of its obviation requirement ( $=$ no local binding).

Syntactic Binding and MSO
Syntactic Binding is MSO-definable iff Limited Obviation holds.

## Limited Obviation

For every binding domain, its syntactically bound pronouns need at most a total of $n$ antecedents to yield a grammatical reading.

## So, what does that mean?

If a binding domain contains more than $n$ bound pronouns,
those additional pronouns can be coreferent with
pronouns in the same domain $\Rightarrow$ Principle B exceptions

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## How would one Falsify Limited Obviation?

- All binding proposals agree that there is some domain within which pronouns may not be syntactically bound $\approx$ binding/obviation domain
- binding domain $\leq \mathrm{CP}$
- Within a single CP, there are three ways of introducing an unbounded number of pronominal DPs:
- adjuncts
- nested TPs/vPs, VPs, and DPs
- coordination
- Limited Obviation is violated only if the pronouns in these configurations all obviate each other (i.e. are mandatorily disjoint in reference).


## Adjuncts

Pronouns contained by adjuncts usually lack obviation.
(4) Every/No/Some woman put the box down in front of her.

But even when obviation can be observed, pronouns contained by distinct adjuncts do not obviate each other.
(5) a. * Every/No/Some priest sacrificed a goat for him.
b. Every/No/Some Egyptian goddess asked of some priest that he sacrifice a goat for her in honor of her.

Hence adjuncts increase the required number of antecedents only by a limited amount.

## Nested TPs/VPs

- Nested TPs/vPs

In English, TPs establish new obviation domains
(although overlap is possible for Spec,TP).
(6) a. * Every/No/Some patient said that he wants him to sedate him.
b. Every/No/Some patient told some doctor that he wants him (to convince him) to sedate him.

- Nested VPs

Nested VPs, if they exist at all in English, behave like nested TPs.
(7) a. * Every/No/Some patient said that he made him operate on him.
b. Every/No/Some doctor told some patient that he made him (watch him) operate on him.

## Nested DPs with Possessors

Depending on your choice of binding theory, one of the two holds:

- possessed DPs establish a new obviation domain
- pronouns inside possessed DPs are not obviative Either way Limited Obviation is satisfied.
(8) a. Every/No/Some politician liked the photographer's picture of him.
b. Every/No/Some politician complained about [the reporter's article on him and [the photographer's picture of him]].


## Nested DPs without Possessors

There is no obviation effect with non-possessed DPs.
(9) a. Every/No/Some post-modern artist must paint at least one [picture of [him and a picture of him]].
b. Every/No/Some client wanted to see a [presentation of [a presentation to him] to him].

## Coordination

Coordination involving bound pronouns is ungrammatical if the two pronouns are identical.
(10) a. Every/No/Some football player told every/no/some cheerleader that the coach wants to see him and her in the office.
b. * Every/No/Some football player told every/no/some masseur that the coach wants to see him and him in the office.

Since every language has only a finite number of distinct pronouns, coordination can only introduce a bounded number of pronouns that obviate each other.

## A Counterexample in ASL? (Graf and Abner 2012)

Coordination of bound pronouns is grammatical in ASL.
(11) ALL $_{\mathrm{i}}$ WRESTLER $_{\mathrm{i}}$ INFORM $_{\mathrm{j}}$ SOMEONE $_{\mathrm{j}}$ SWIMMER $_{\mathrm{j}}$ THAT $\mathrm{IX}_{\mathrm{i} / \mathrm{j}} \mathrm{IX}_{\mathrm{j} / \mathrm{i}}$ WILL RIDE-IN-VEHICLE LIMO GO-TO DANCE Every wrestler ${ }_{i}$ told some swimmer ${ }_{j}$ that him $_{i / j}$ and him $_{j / i}$ would ride in a limo to the dance.
(12) EACH $_{\mathrm{i}}$ WRESTLER $_{\mathrm{i}}$ TELL $_{\mathrm{j}}$ SOMEONE $_{\mathrm{j}}$ SWIMMER $_{\mathrm{j}}$ THAT SOMEONE $_{k}$ FOOTBALL $_{k}$ PLAYER $_{k}$ ASK CAN IX $_{\mathrm{i}} \mathrm{IX}_{\mathrm{j}} \mathrm{IX}_{\mathrm{k}}$ THREE-HUMANS-GO-TO DANCE (TOGETHER)
Each wrestler ${ }_{i}$ told some swimmer ${ }_{j}$ that some football player $_{k}$ asked if $\mathrm{him}_{i}$ and $\mathrm{him}_{j}$ and $\mathrm{him}_{k}$ could go to the dance together.

## Binding in ASL

- Every DP can be assigned a locus in space.
- Pronominal binding is realized by pointing at the locus which a DP has been assigned to (transcribed as IX).


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## The Role of Deixis

Pointing at referents in space resembles deictic pronouns in English. And deictic pronouns can easily be coordinated.
(13) Every/No/Some football player told every/some/no masseur that the coach wants to see him deictic and him $_{\text {deictic }}$ in his office.

Since Limited Obviation only applies to syntactic binding, (13) does not constitute a counterexample.

## The Big Question

Are the coordinated pronouns in ASL syntactically bound?

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## Non-empty Domain Restrictions

While pronouns can be discourse-bound by quantifiers in English, the extension of the quantified DP must be non-empty.
(14) a. Every player is handed a card. He then has to role a dice.
b. \# No player is handed a card. He then has to role a dice.

A similar pattern emerges for pronouns in ASL.
(15) EACH POLITICS PERSON ${ }_{i}$ TELL-STORY (IX ${ }_{i}$ ) WANT WIN Each politician ${ }_{i}$ said he ${ }_{i}$ wants to win.
(16) NO POLITICS PERSON ${ }_{\mathrm{i}}$ TELL-STORY ( ${ }^{*} \mathrm{IX}_{\mathrm{i}}$ ) WANT WIN No politician ${ }_{i}$ said he $e_{i}$ wants to win.

## Section Summary

Are MSO-definable constraints sufficient?
Probably yes, if semantics isn't involved:

- Constraint results only hold for syntax
$\Rightarrow$ Syntactic fragment of binding theory
- No discourse binding, no evaluation of specific readings
- Even then a limit on the number of required antecedents per binding domain is mandatory for MSO-computability $\Rightarrow$ Limited Obviation
- Satisfied in English and (probably) ASL
- A new descriptive universal for binding theory?


## Conclusion

- Questions
- Why do constraints exist at all?
- What kinds of constraints are there?
- How powerful are they?
- How do they fit into syntax?
- What are the empirical implications?
- Formal Answer
- Constraints are a natural by-product of Merge.
- The MG-expressible constraints are exactly those that can be computed with a finitely bounded amount of working memory.
- Within this class, all subtypes are interchangeable.
- Implications
- offers new solutions to processing problems
- prompts new descriptive universal for pronominal binding


## Outlook



## Outlook



## Outlook



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## Compiling States into Features



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## Representational $\equiv$ Derivational

MSO over Representations

$$
\begin{gathered}
\wedge, \vee, \neg, \rightarrow \\
\exists, \forall
\end{gathered}
$$

$$
\equiv
$$

standard dominance $\triangleleft$

## MSO over Derivations

$$
\wedge, \vee, \neg, \rightarrow
$$

$$
\exists, \forall
$$

$$
\equiv
$$

derivational dominance

- $x \triangleleft y$ iff $\phi(x, y)$, where $\phi$ uses $\triangleleft$ but not $\triangleleft$
$\Rightarrow$ replacing each occurrence of $x \triangleleft y$ by $\phi(x, y)$
in representational constraint $C$ yields derivational $C^{\prime}$
- $x \triangleleft y$ iff $\psi(x, y)$, where $\psi$ uses $\triangleleft$ but not $\triangleleft$
$\Rightarrow$ replacing each occurrence of $x \longleftarrow y$ by $\psi(x, y)$
in derivational constraint $C$ yields representational $C^{\prime}$


## Derivational $\equiv$ Transderivational

## A Different Perspective on Transderivationality

Transderivational constraints do not filter out suboptimal trees. They rewrite suboptimal trees into optimal ones.

- Rewrite procedure carried out by linear tree transducer
- Given a set of Minimalist derivations as inputs, transducer produces set of outputs that can be computed by a tree automaton
- Compile said automaton into the features as usual


## (Dis)Advantages of Constraint Classes

Are constraints redundant? Should we just use feature checking?

- Shortcomings of Local Constraints less succinct, often incomprehensible, hide generalizations
- Shortcomings of Derivational Constraints some constraints are significantly more complicated when stated over derivations (e.g. ECP)
- Advantages of Transderivational Constraints can state generalizations across grammars that are not expressible with derivational/representational constraints


## Methodological Moral of the Story

Even though the constraint classes have the same power, they each have their own advantages and disadvantages.
$\Rightarrow$ Use the type of constraint that is best suited to the task!

## A Purely Transderivational Generalization

## Shortest Derivation Principle

Given a set of competing derivations, pick the one with the fewest instances of Move.

## Toy Grammar 1

- At least one DP moves out of VP.
- Two options:
- Move to SpecYP, and YP then moves to SpecZP (roll-up)
- Move directly to SpecZP (one-fell-swoop)
- Result: Exactly one DP must move from VP to SpecZP.


## Toy Grammar 2

- At most one DP moves out of VP, directly into SpecZP.
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## Implications for Acquisition

- "cognitive load explanations" for acquisition delays of Principle B and Focus Projection (Grodzinsky and Reinhart 1993; Szendrői 2004)
- Certain processes involve transderivational constraints.
- Comparing multiple trees too computationally demanding for young children
$\Rightarrow$ delay in acquisition due to insufficient working memory
- Implausible explanation if transderivational $\equiv$ derivational (no extra processing load)
- Recent findings: Principle B delay an artifact of experimental setup
(Papafragou and Musolino 2003; Papafragou and Tantalou 2004; Elbourne 2005; Conroy et al. 2009)
- Same problem with Focus experiment?

A pilot study is in preparation.

## Two Common Questions on ASL Binding

## What about other obviation domains in ASL?

Coordination and nested VP/TP domains provide the only true ASL parallel to their English counterparts, the latter of which also introduce new binding domains in ASL. Nested DP structures are not well-attested in the language and comparable adjunct structures are expressed in ASL through the use of complex locative and classifier morphology.

Could spatial reference just be an elaborate case or gender system?
Then the grammatical coordination examples parallel the coordination of him and her in English and are not a problem for Limited Obviation. However, there is no sense in which spatial loci are inherently associated with (pro)nominals in ASL, as is typical of gender systems, nor are spatial loci reliably assigned in specific syntactic environments, as is typical of case systems.

## More on Coordination in English

Some speakers accept (17) as grammatical.
(17) ?? Every/No/Some football player told every/no/some masseur that the coach wants him to run six laps and him to prepare the massage room.

If this pattern is a productive instance of coordinating syntactically bound pronouns, it would falsify Limited Obviation.
But just like in ASL, the binding mechanism at play here arguably isn't (purely) syntactic in nature.

- Most speakers need to put (contrastive) stress on the respective pronouns.
- No seems to be disprefered compared to every and some.
- There is no c-command requirement (even in configurations where QR is bounded).


## More on Coordination in English [cont.]

(18) a. A coach of every/some football player told a receptionist of every/some masseur that the team's president wants him to get a massage and him to give it.
b. An agent of every/some actress told a bodyguard of every/some first lady that he wants her to do a movie about Jackie Kennedy and her to be on the set as a consultant.
c. An interview that every/some football player liked included a quib, which every/some masseur had related to the reporter at some point, that the coach always ordered him to run six laps and him to prepare the massage chair.

