# Computational Parallels Across Language Modules

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Yale Colloquium Sep 12, 2016

# The Talk in a Nutshell

### A Humble Goal

- A unified perspective on
  - phonology,
  - morphology,
  - syntax,

#### that ties together

- typology,
- cognition,
- learning.

But beware...

The ground of science [is] littered with the corpses of dead unified theories.

> **Freeman Dyson** Disturbing the Universe, p62



### Outline

### 1 The Received View: Highly Distinct Language Modules

2 Weak Parallelism: Syntax is Regular, Too

### 3 Strong Parallelism: Tier-Based Strict Locality

- Regularity is Too Permissive
- Tier-Based Strictly Local Phonology
- Tier-Based Strictly Local Morphology
- Tier-Based Strictly Local Syntax

## The Big Divide

- Phonology, morphology, and syntax are highly distinct.
  - different empirical phenomena
  - different cognitive properties
  - different theories
- There have been attempts at unification, but the resulting theories still look very different:
  - OT-syntax  $\Leftrightarrow$  phonological OT
  - Government Phonology  $\Leftrightarrow$  GB
  - ► Dependency Phonology ⇔ Dependency grammar
  - ► Distributed Morphology ⇔ standard Minimalism
- The standard view is still that there is little common ground.

In formal language theory, stringsets are classified according to their formal complexity

 $\mathsf{regular} < \mathsf{context}\text{-}\mathsf{free} < \mathsf{mildly} \ \mathsf{context}\text{-}\mathsf{sensitive} < \cdots$ 

Phonology

Morphology

Syntax

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# Implications of Mathematical Distinctness

Heinz and Idsardi (2011, 2013) highlight the implications:

- different typology center embedding, crossing dependencies
- different memory architecture flat & finite VS unbounded nested stacks
- different learning algorithms much harder for syntax





### An Incomplete Picture

- The argument that phonology, morphology generate simpler stringsets than syntax is mathematically correct.
- But syntax is not about strings!
- What happens if we think of syntax as generating trees?

## Minimalist Grammars



- Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- Operations: Merge and Move
- Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items

Chemistry	Syntax			
atoms	words			
electrons	features			
molecules	sentences			

## MG Syntax in Action



#### Phrase Structure Tree

### MG Syntax in Action





Phrase Structure Tree

**Derivation Tree** 

## The Central Role of Derivation Trees

 Derivation trees are rarely considered in generative syntax. (but see Epstein et al. 1998)

### satisfy Chomsky's structural desiderata:

- no linear order
- Iabel-free
- extension condition
- inclusiveness condition
- contain all information to produce phrase structure trees
   central data structure of Minimalist syntax

# Psychological Reality of Derivation Trees

Central role of derivation trees backed up by processing data:

- Derivation trees can be parsed top-down (Stabler 2013)
- Parsing models update Derivational Theory of Complexity, make correct processing predictions for
  - right < center embedding (Kobele et al. 2012)</p>
  - crossing < nested dependencies (Kobele et al. 2012)</li>
  - SC-RC < RC-SC (Graf and Marcinek 2014)</li>
  - SRC < ORC in English (Graf and Marcinek 2014)</li>
  - SRC < ORC in East-Asian (Graf et al. 2015)</li>
  - quantifier scope preferences (Pasternak 2016)

# Technical Fertility of Derivation Trees

Derivation trees made it easy for MGs to accommodate the full syntactic toolbox:

- sidewards movement (Stabler 2006; Graf 2013)
- affix hopping (Graf 2012b, 2013)
- clustering movement (Gärtner and Michaelis 2010)
- tucking in (Graf 2013)
- ATB movement (Kobele 2008)
- copy movement (Kobele 2006)
- extraposition (Hunter and Frank 2014)
- Late Merge (Kobele 2010; Graf 2014a)
- ► Agree (Kobele 2011; Graf 2012a)
- ▶ adjunction (Fowlie 2013; Graf 2014b; Hunter 2015)
- ► TAG-style adjunction (Graf 2012c)

# Even More MG Extensions

- ▶ local and global constraints (Kobele 2011; Graf 2012a, 2016a)
- transderivational constraints (Graf 2010c, 2013)
- Principle A and B (Graf and Abner 2012)
- GPSG-style feature percolation (Kobele 2008)
- idioms (Kobele 2012)
- grafts (multi-rooted multi-dominance trees) (Graf in progress)

#### Long Story Short

Derivation trees are a more useful and fertile data structure than phrase structure trees.

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# The Complexity of Minimalist Tree Languages

Another surprise: derivation trees are also **crucially simpler!** This holds even with all the extensions listed before.

- The set of derivation trees is a regular tree language. (Michaelis 2001; Kobele et al. 2007; Graf 2012a)
- The set of phrase structure trees is not. (Doner 1970; Thatcher 1967; Michaelis 2001)

#### Computational Parallelism Hypothesis (Weak)

- Phonology and morphology are regular over strings.
- Syntax is regular over derivation trees.

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Regular Syntax

### Different cognitive picture

	Complexity	Data Structure
Phonology	REG	strings
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Syntax	MCS	strings

Similar memory architecture (flat, finite) and structural inference mechanisms for all three modules

- 1 Can we leverage this for typology, language acquisition?
- 2 Is this just an accident?

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## Too Many Patterns are Regular

- Reminder: regular patterns at bottom of complexity hierarchy
- Problem
  - all phon/morph/syn patterns are regular,
  - not all regular patterns occur in natural languages
- Regularity is too loose an upper bound.

#### Example

- First-last consonant harmony
- Word with at least 3 suffixes must have exactly 5 prefixes
- Derivation contains even number of Move steps
- Principle A applies only if no wh-movement takes place

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### Subregular Languages

### Often forgotten: hierarchy of subregular languages

(McNaughton and Papert 1971; Rogers et al. 2010; Rogers and Pullum 2011; Heinz et al. 2011; Graf 2016b)



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### TSL: Tier-Based Strictly Local

- There are a variety of subregular classes to choose from.
- But recent research suggests that TSL is the right fit.

#### Tier-Based Strictly Local Languages

- All patterns described by locally bounded constraints.
- Non-local dependencies are local over tiers.
- Much weaker than regular but still powerful enough.

# Phonology as a TSL System

Tons of recent work by Jeffrey Heinz, Jane Chandlee, Adam Jardine, and others.

- Phonology as set of well-formed strings
   phonology = phonotactics
- Grammar is a finite set of hard, non-violable markedness constraints.
- Each constraint is represented by a finite collection of forbidden *n*-grams.





## Example: Local Constraints

<b>Process</b> Word-final devoicing	Constraint *[+voice]\$	Forbidden <i>n</i> -grams s\$, 0\$, f\$,
Intervocalic voicing	*V[-voice]V	asa, asi,, isa, isi,, afa, afi,, ifa, ifi,,
CV template	*\$V *CC *VV *C\$	\$a, \$i, … pp, pb, … bp, bb, … aa, ai, … , ia, ii, … p\$, b\$, …

# Tiers for Long-Distance Dependencies

- ▶ We can move to 3-grams, 4-grams, ... n-grams in order to regulate less local processes (e.g. umlaut, vowel harmony).
- ► Problem: Still limited to locality domain of size n ⇒ unbounded processes cannot be captured
- Solution: selected segments project dedicated tier

#### Tier-Based *n*-gram Grammar

- Tier-projection is determined by the shape of the segment, not by structural properties (e.g. feet).
- ► A string is well-formed iff no tier *T* contains an illicit *T*-*n*-gram.

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### Example: Sibilant Harmony

ConstraintForbidden tier\_1-n-grams\* $\int \cdots s$  $\int s$ 

Tier1contains all sibilantsTier0contains all segments

$Tier_1$ :	\$ 		J		S		\$ 
Tier <sub>0</sub> :	\$	e	ſ	i	S	i	\$
Tier <sub>1</sub> :	\$		ſ		ſ		\$
Tier <sub>0</sub> :	\$	е	ſ	i	∣ ∫	i	\$

## Example: Stress Assignment

Culminativity every word has exactly one primary stress

- Tier1contains segments with primary stressTier0contains all segments
- *n*-grams ś = and on **Tier**<sub>1</sub>


### A Non-TSL Pattern: Sour Grapes Harmony

Sour Grapes vowel harmony applies only if it can apply to the whole word (i.e. there is no blocker)

#### Why Sour Grapes isn't TSL

- All vowels V must be on the vowel harmony tier.
- The blocker B must be on the same tier in order to block it.
- But there is no bound on the number of vowels per tier.
- The tier thus may have the shape

···· **V V V** ···· **B** ····

- **B** can be arbitrarily far away from  $VVV \Rightarrow$  not a local relation
- But we need to know whether B is on the tier in order to determine the well-formedness of VVV.

### Complexity of Phonology

- All local phonological constraints are TSL.
- All segmental long-distance constraints are TSL.
  But my student Alëna Aksënova may have found a counterexample.
- Tone and stress constraints may go beyond TSL. (Graf 2010a,b; Jardine 2015)
- TSL avoids instances of OT overgeneration:
  - cannot generate sour-grapes or majority rules patterns
  - does not allow agreement by proxy
  - explains why consonant harmony is unbounded or transvocalic, but never transconsonantal (McMullin and Hansson 2015)

### **Cognitive Implications**

#### TSL languages learnable from positive data (Heinz et al. 2012; Jardine and Heinz 2016)

- ▶ UG: specifies upper bound on size of *n*-grams
- memorize which sequences have not been seen so far
- induce tier (more complex)
- still, learning input can be relatively small
- What cognitive resources are required?
  - Only memorization of the last n segments of a specific type
  - For most processes  $n \leq 3$ , and for all  $n \leq 7$
  - Fits within bounds of human working memory

# Interim Summary: Phonology

- Phonology is TSL (possibly with a few outliers).
- gives tighter bound on typology
- solves poverty of stimulus by greatly simplifying learning
- reduces cognitive resource requirements

#### A Tantalizing Possibility

- TSL is an appealing class.
- And it seems it isn't limited to phonology...

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### Tier-Based Strictly Local Morphology





- Join work with Alëna Aksënova and Sophie Moradi.
- It seems that morphology is also TSL. (Aksënova et al. 2016)
- Morphology  $\equiv$  Morphotactics of underlying forms
- ▶ We are unaware of any non-TSL patterns in this realm.
- Tight typology, explains gaps

#### Example: Circumfixation in Indonesian

- Indonesian has circumfixation with no upper bound on the distance between the two parts of the circumfix.
- (1) maha siswa<br/>big pupil(2) \*(ke-) maha siswa \*(-an)<br/>NMN- big pupil -NMN<br/>'student''student''student affairs'
  - Requirements: exactly one ke- and exactly one -an

<b>Tier</b> <sub>1</sub>	contains all NMN affixes	\$ an			ke	ke	\$
Tier <sub>0</sub>	contains all morphemes						
n-grams	\$an, ke\$, keke, anan	\$ an	m	S	ke	ke	\$

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# Example: Swahili vyo

# Swahili *vyo* is **either a prefix or a suffix**, depending on presence of negation. (Stump 2016)

- (3) a. a- vi- soma -vyo SBJ:CL.1- OBJ:CL.8- read -REL:CL.8 'reads'
  - b. a- si- **vyo-** vi- soma SBJ:CL.1- NEG- REL:CL.8- read -OBJ:CL.8 'doesn't read'

### Example: Swahili vyo [cont.]

- (4) a. \* a- vyo- vi- soma SBJ:CL.1- REL:CL.8- OBJ:CL.8- read
  - b. \* a- vyo- vi- soma -vyo SBJ:CL.1- REL:CL.8- OBJ:CL.8- read -REL:CL.8
  - c. \* a- si- vyo- vi- soma SBJ:CL.1- NEG- REL:CL.8- OBJ:CL.8- read -vyo REL:CL.8-
  - d. \* a- si- vi- soma -vyo SBJ:CL.1- NEG- OBJ:CL.8- read REL:CL.8-

# Example: Swahili vyo [cont.]

#### Generalizations About vyo

- may occur at most once
- must follow negation prefix si- if present
- ▶ is a prefix iff *si* is present

Tier <sub>1</sub>	contains <i>vyo</i> , <i>si</i> , and stem edges $\#$			
Tier <sub>0</sub>	contains all morphen	nes		
<i>n</i> -grams	vyovyo, vyo##vyo	"at most one <i>vyo</i> "		
	vyosi, vyo##si	" <i>vyo</i> follows <i>si</i> "		
	si##vyo, \$vyo##	" <i>vyo</i> is prefix iff <i>si</i> present"		

# Explaining Typological Gaps

Restriction to TSL can also explain some typological gaps.

#### General Strategy

- Attested patterns A and B are TSL.
- But combined pattern **A**+**B** is not attested.
- Show that A+B is not TSL.

# Example: Compounding Markers

- Russian has an infix -o- that may occur between parts of compounds.
- Turkish has a single suffix -si that occurs at end of compounds.
- (5) vod -o- voz -o- voz water -COMP- carry -COMP- carry 'carrier of water-carriers'
- (6) türk bahçe kapı -sı (\*-sı) turkish garden gate -COMP (\*-COMP)
   'Turkish garden gate'

#### New Universal

If a language allows unboundedly many compound affixes, they are **infixes**.

# Example: Compounding Markers [cont.]

Russian and Turkish are TSL.

Tier1COMP affix and stem edges #Russian n-gramsoo, \$o, o\$Turkish n-gramssisi, \$si, si#

- ▶ The combined pattern would yield Ruskish: stem<sup>n+1</sup>-si<sup>n</sup>
- This pattern is not regular and hence not TSL either.

### Interim Summary: Morphology

- While we know less about morphology than phonology at this point, it also seems to be TSL.
- Even complex patterns like Swahili vyo can be captured.
- At the same time, we get **new universals**:

Bounded Circumfixation No recursive process can be realized via circumfixation.

Non-proportionality The number of prefixes cannot be proportional to the number of stems or suffixes, *et vice versa*.

- We can reuse tools and techniques from TSL phonology, including learning algorithms.
- The cognitive resource requirements are also comparable.

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Phonology	REG	strings
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Syntax	MCS	strings

- Is syntax the odd one out after all?
- Hard to say in full generality, but Merge and Move are TSL. (Graf and Heinz 2016)

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#### Reminder: MG Derivation Trees





#### Phrase Structure Tree

**Derivation Tree** 

#### Tree *n*-gram Grammars

- ▶ We need to lift *n*-grams from strings to trees.
- ▶ Instead of strings of length *n*, use subtrees of depth *n*.
- Each subtree encodes a constraint on the derivation.



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#### Constraints on Move

#### Merge is a local process, regulated by tree *n*-grams. But what about Move?

Suppose our MG is in single movement normal form,

i.e. every phrase moves at most once.

Then movement is regulated by two constraints. (Graf 2012a)

#### Constraints on Movement

- Move Every head with a negative Move feature is dominated by a matching Move node.
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#### Move Constraints over Tiers

Original

- **Move** Every head with a negative Move feature is dominated by a matching Move node.
- **SMC** Every Move node is a closest dominating match for exactly one head.

#### Tier

Every lexical item has a **mother** labeled Move.

Exactly one of a Move node's **daughters** is a lexical item.

Tree <i>n</i> -gram Tem	plates			
	Move	SMC1	SMC2	
	\$	Move	Move	
		/^``\		
	$\geq 1 \text{ LI}$	no LI	$\geq 2$ Lls	





\$





\$





#### Example of III-Formed Derivation



SMC2

no LI SMC1

Move

 $\geq 1$  LI

Move

\$

g

\$

Move

no LI SMC1

Move

\$



 $\geq 1$  LI

Move

\$

no Ll SMC1

Move

\$




# Example of Well-Formed Derivation





S

# Example of Well-Formed Derivation





# Example of Well-Formed Derivation



Move

 $\geq 2 \overline{LI}$ 

SMC2

# Syntax is TSL

 Generalizing tiers from strings to derivations shows Merge and Move to be TSL.

caveat: single movement normal form

- It is unclear whether the MG extensions also fit into TSL.
- But we take an important step towards acquisition, solving poverty-of-stimulus!

#### Towards a New Learning Algorithm for Syntax

- Derivation trees without Move  $\approx$  dependency graphs
- Input: dependency graph, surface string
- Child must infer movement relations:
  - Look at string order to compute possible derivations with Move nodes (in single-movement normal form).
  - ▶ Keep track of well-formed tier *n*-grams seen so far.
  - ▶ Favor derivations that do not introduce new tier *n*-grams.

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# Remarks on Single Movement Normal Form

- Single Movement Normal Form seems unrealistic.
- But: does not rule out multiple movement steps, only says there is single feature trigger in derivation
- Intermediate landing sites can be part of structure built from the derivation tree.

#### A Conjecture on Movement Restrictions

- Conversion of an MG into single movement normal form causes large blow-up in size of lexicon.
- Blow-up varies a lot: from 0 to hundred times the original size
- ► The more fixed the position of movers, the smaller the blow-up ⇒ island constraints as a means to limit lexical blow-up?

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#### **TSL** Intuition

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- They are local over a very simple relativization domain.

Unified perspective on

- cognition
- acquisition
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# Future Work

There's tons of work that still needs to be done. Most pressing:

- fully autosegmental structures for phonology
- derivations for morphology
- mappings
- look beyond Move in syntax

# Join the Enterprise!

- typological universals/gaps
- grammar fragments and careful descriptions of phenomena
- TSL-analyses of phenomena
- counterexamples
- artificial language learning experiments
- processing experiments
- and of course: theorems and proofs

#### I wanna learn more...

- Computational Linguistics II lecture notes: lin637.thomasgraf.net
- Computational phonology seminar: lin626.thomasgraf.net
- Computational syntax seminar: next semester
- Check the references

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