

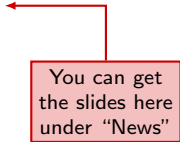
The (Surprising) Simplicity of Syntax

Derivation trees, subregular complexity, and
what it implies for language and cognition

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Penn ILST Seminar
November 26, 2018



You can get
the slides here
under "News"

A Mathematical Distinctness Theorem

- ▶ From a computational perspective, there is a split between “P-side” and “S-side”.

regular < context-free < mildly context-sensitive < ...

Phonology

Morphology

Syntax

- ▶ Matches linguistic practice (despite attempts at unification, e.g. DM)
- ▶ Why is syntax the outlier?

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↑ Kaplan and Kay (1994)

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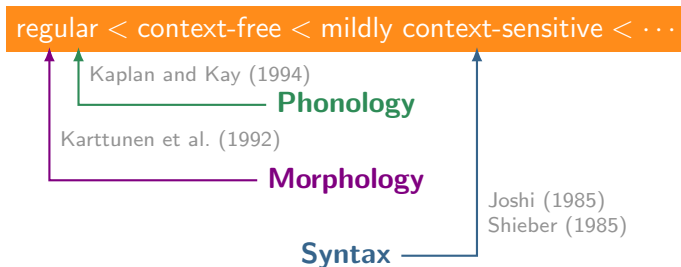
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An Alternative: Simple Syntax

- ▶ The postulated split is misleading.
- ▶ If we probe deeper, we find that
 - ▶ syntax is just as simple,
 - ▶ phonology, morphology, and syntax are weaker than regular \Rightarrow **subregular**
 - ▶ relativized locality plays a major role,
 - ▶ and is approximated by the formal class **TSL**.
- ▶ This has repercussions for
 - ▶ cognitive architecture of language,
 - ▶ learning,
 - ▶ processing.

Outline

- 1** Locality and Tiers in Phonology
 - Tier-Based Strictly Local (TSL)
 - The Cognitive Picture

- 2** c-Command Constraints in Syntax
 - c-Strings
 - The Cognitive Picture

- 3** Syntax
 - Minimalist Grammars
 - Merge is TSL
 - Move is TSL

The Subregular Program

- ▶ **Received view:** class of regular (= finite-state) string languages maximally complex
- ▶ **Subregular hierarchy:** even weaker/simpler subclasses
- ▶ The **tier-based strictly local (TSL)** languages have emerged as particularly important.



**Jeff
Heinz**



**Jane
Chandlee**



**Adam
Jardine**



**Kevin
McMullin**

Example: Word-Final Devoicing

- ▶ Captured by forbidding voiced segments at the end of a word
- ▶ **German:** Don't have **z**\$ or **v**\$ or **d**\$ (where \$ = word edge).

Example: German

*\$ r a **d** \$

***z**\$
***v**\$
***d**\$

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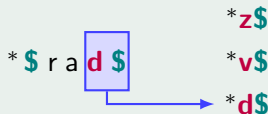
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 - ▶ $[-\text{voice}] = \{s, f\}$
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A Problem: Samala Sibilant Harmony

- ▶ If multiple sibilants occur in the same word, they must all be +anterior (**s,z**) or –anterior (**ʃ,ʒ**).
- ▶ In other words: Don't mix **purple** and **teal**.

***s**ʃ ***s**ʒ ***z**ʃ ***z**ʒ
 *ʃ**s** *ʒ**s** *ʃ**z** *ʒ**z**

- ▶ **But:** Sibilants can be arbitrarily far away from each other!

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Making Long-Distance Dependencies Local

- ▶ Let's take a clue from phonology:
create locality with **tiers**.
(Goldsmith 1985; Heinz et al. 2011)
- ▶ Enforce constraints on tier,
rather than string



Jeff Heinz

Example: Samala Revisited

1 Project sibilant tier

2 *sʃ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz

*\$ha s xintilawa ʃ\$

\$ha ʃ xintilawa ʃ\$

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\$	s		ʃ	\$	
*\$	h	a	s	x	i
			n	t	i
			l	a	w
			a	ʃ	\$

\$	h	a	ʃ	x	i	n	t	i	l	a	w	a	ʃ	\$
----	---	---	---	---	---	---	---	---	---	---	---	---	---	----

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\$	s		ʃ	\$
*\$	h a s	x i n t i l a w a	ʃ	\$

\$	ʃ		ʃ	\$
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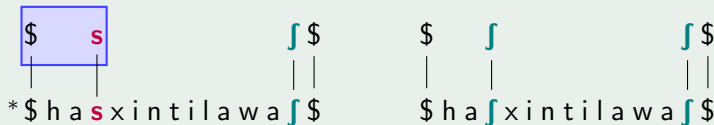


Jeff Heinz

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\$ s ʃ \$
| |
*\$ h a s x i n t i l a w a ʃ \$

\$ ʃ ʃ \$
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7

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Diagram illustrating the state of the stack after the third push operation:

Stack (top to bottom): \$, \$, \$

Input string: * \$ h a s x i n t i l a w a \$

The stack contains three '\$' symbols. The input string is "saxintilawa" with a '*' at the beginning and a '\$' at the end. The 's' in the input string is highlighted in red, corresponding to the red 's' in the stack above it.

Making Long-Distance Dependencies Local

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What may Project?

Tier projection controlled by

- 1 label of segment
- 2 local context
- 3 symbols already on tier

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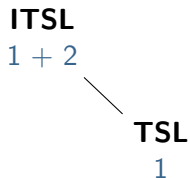
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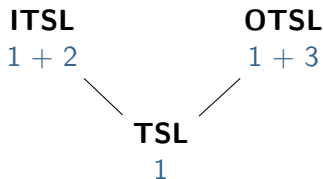
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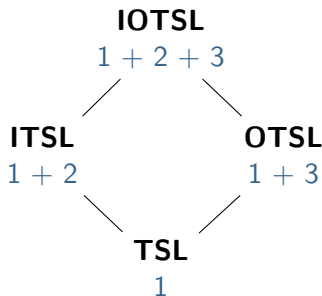
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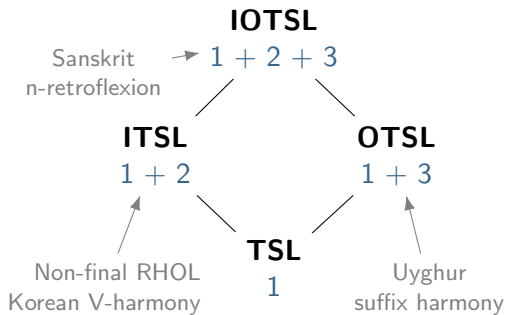
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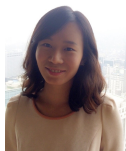
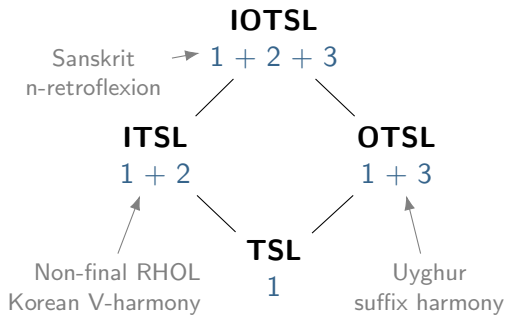
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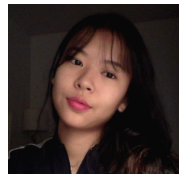
**Hyunah
Baek**



**Aniello
De Santo**



**Connor
Mayer**



**Suji
Yang**

TSL Across Language Modules

- ▶ Phonological dependencies fall within the TSL region.
- ▶ Morphological dependencies do, too.
(Aksënova et al. 2016; Aksënova and De Santo 2017; Chandlee 2017)
- ▶ Phonology and morphology are **computationally similar**.



**Alëna
Aksënova**

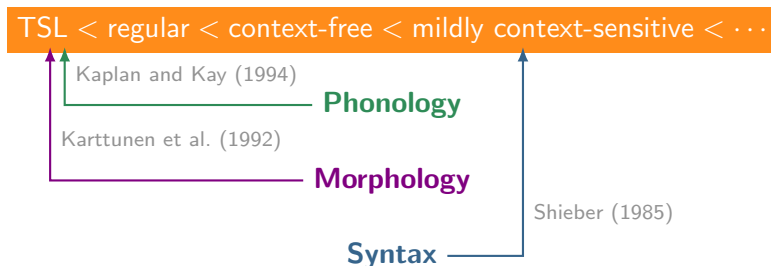


**Sophie
Moradi**

Why is TSL Relevant?

- ▶ Linguistically natural
- ▶ Captures wide range of phonotactic dependencies
- ▶ Correct and efficient learning algorithms
(I/O-TSL work in progress)
(Jardine and McMullin 2017)
- ▶ Low resource demand
 - ▶ remember the last n symbols of a specific type
 - ▶ requires little working memory
 - ▶ no complex memory architecture
- ▶ Rules out unattested patterns
 - ▶ center embedding
 - ▶ harmony only if separated by even number of segments

Could Syntax Also be Subregular?



- ▶ Syntax seems even more like an outlier...
- ▶ Don't look at strings!
What about **syntactic dependencies**?

Nazila Shafiei

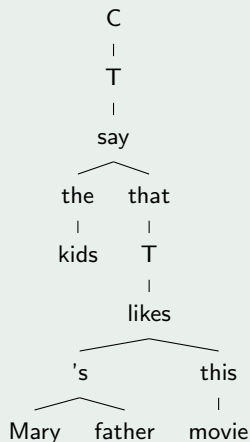
c-Strings

Command-Strings

The **c[ommand]-string** of a node n contains

- ▶ n and
 - ▶ every node that commands n .
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- ▶ easily computed from dependency trees
 - ▶ c-command constraints seem to be largely **IOTSL over c-strings**

Example



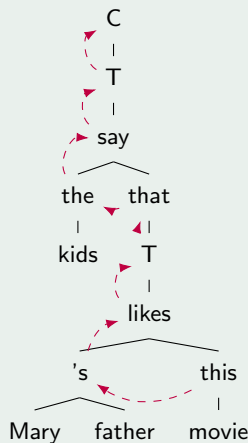
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Example



this 's likes T that the say T C

Principle A

Principle A (as a distributional constraint)

Every reflexive must be c-commanded by a DP in the same TP.

Equivalent c-String Constraint

If the c-string starts with a reflexive,
then at least one D must occur before the first T.

TSL Strategy for Principle A

- 1 Always project first symbol (ITSL)
- 2 Project D/T if previous symbol is Refl (OTSL)
- 3 Constraint: ***Refl** **T** (bigram)

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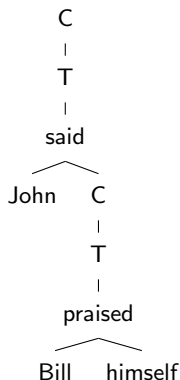
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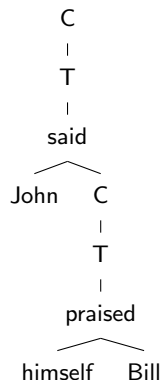
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- | | | |
|---|--|----------|
| 1 | Always project first symbol | (ITSL) |
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Example of Principle A as a TSL Constraint

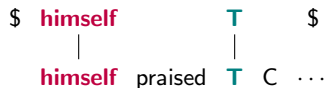
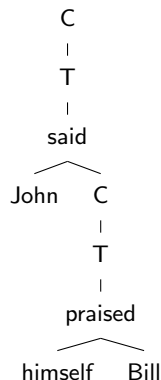
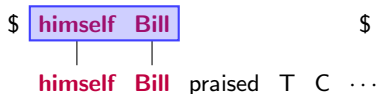
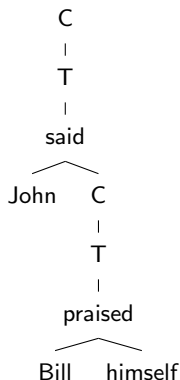


\$ **himself** **Bill** \$
 | |
himself **Bill** praised T C ...

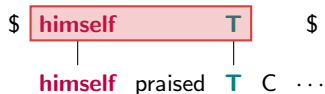
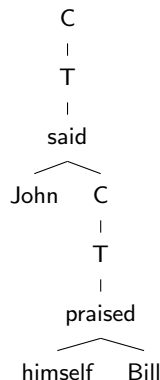
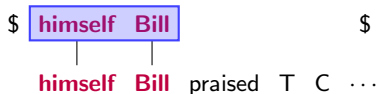
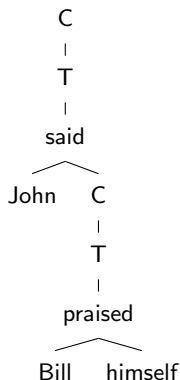


\$ **himself** T \$
 | |
himself praised T C ...

Example of Principle A as a TSL Constraint



Example of Principle A as a TSL Constraint



Another Example: Swedish *sig*

- Swedish *sig* must be non-locally bound.

- (1) a. John said Bill praised *sig*.
 b. * Bill praised *sig*.

TSL Strategy for *sig*

- 1 Always project first symbol (ITSL)
- 2 Project T if previous symbol is *sig* (OTSL)
- 3 Project D if previous symbol is T (OTSL)
- 4 Constraint: ***sig T \$** (trigram)

\$ **sig** **T** **John** \$
 | | |
sig Bill praised **T** C **John** ...

\$ **sig** **T** \$
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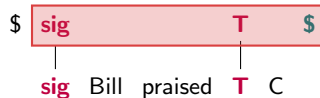
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Comparison to Phonology and Morphology

Similarities

- ▶ mostly bigram and trigram constraints
- ▶ simple structural contexts
- ▶ dependencies in phonology are also c-command-like (Graf 2018a)

Differences

- ▶ OTSL seems more common in syntax

A Typological Prediction

Formal typology of syntactic constraints should mirror phonology and morphology.

Connection to Parsing

- ▶ A tree is well-formed only if each node has a well-formed c-string.
- ▶ verifiable by deterministic top-down tree automaton with finite look-ahead
 - ⇒ **efficient incremental parsing**

An Intriguing Hypothesis

- ▶ Why c-command (rather than, say, precedence)?
 - ▶ Because it allows for more efficient processing!
-
- ▶ But syntax isn't just c-command.
There's also displacement/movement. . .

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Minimalist Grammars

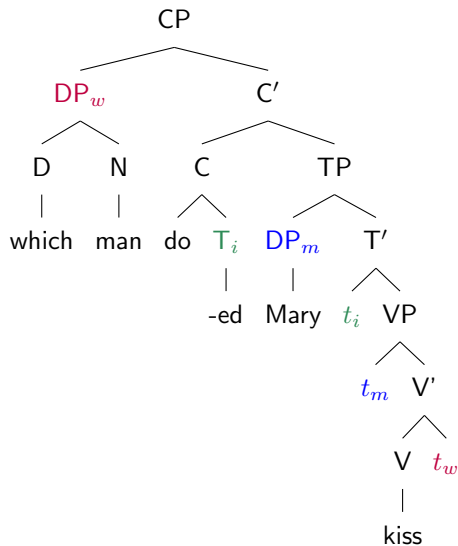


Ed Stabler

- ▶ Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- ▶ Operations: **Merge** and **Move**
- ▶ Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items

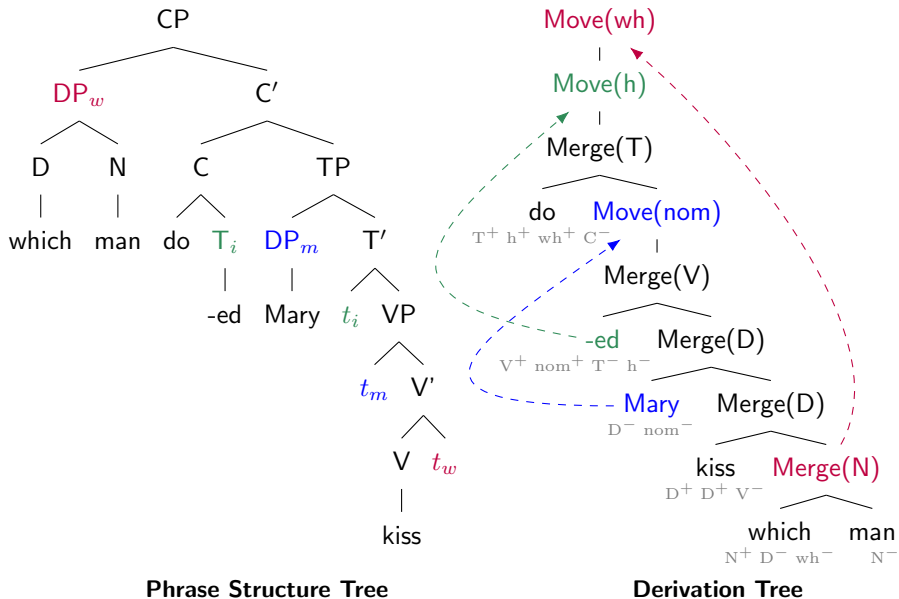
Chemistry	Syntax
atoms	words
electrons	features
molecules	sentences

MG Syntax in Action



Phrase Structure Tree

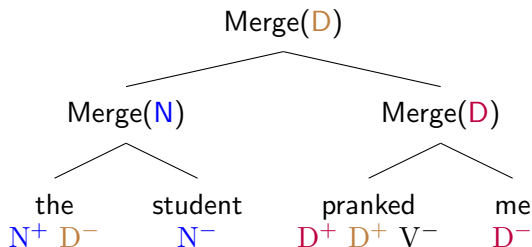
MG Syntax in Action



The Central Role of Derivation Trees

- ▶ Derivation trees are rarely considered in generative syntax.
(but see Epstein et al. 1998)
- ▶ Satisfy Chomsky's structural desiderata:
 - ▶ no linear order
 - ▶ label-free
 - ▶ extension condition
 - ▶ inclusiveness condition
- ▶ Contain all information to produce phrase structure trees
⇒ **central data structure** of Minimalist syntax

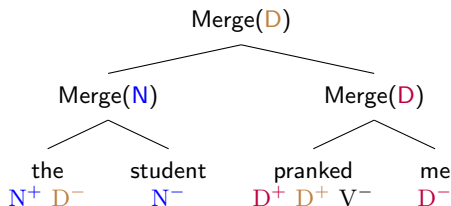
Merge is TSL



- ▶ The selector features of the head have to match the category features of the arguments.
- ▶ 1-to-1 match between selector features and category features.
- ▶ This is naturally expressed as **TSL over trees**.

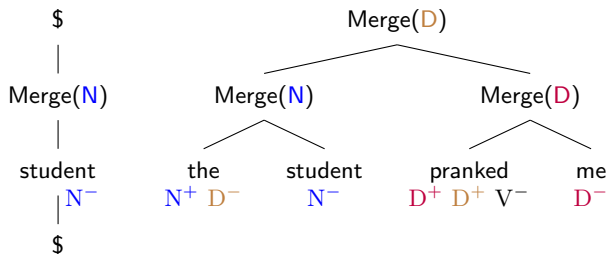
Category Tiers for Merge

- ▶ Project tree tier for each category X .
- ▶ Every X^- has a Merge node as its mother.
- ▶ Every Merge node has exactly one X^- among its daughters.



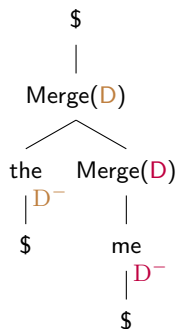
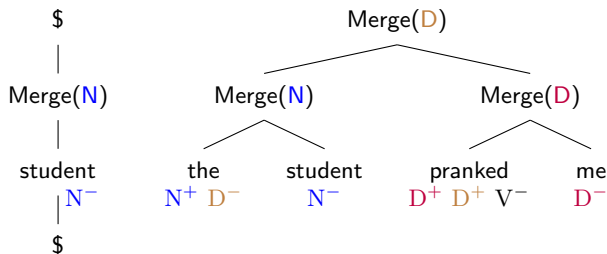
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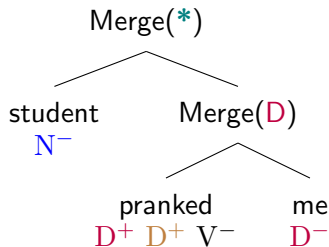


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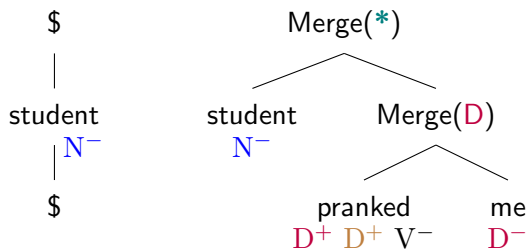


Illicit Merge Yields Ill-Formed Tiers



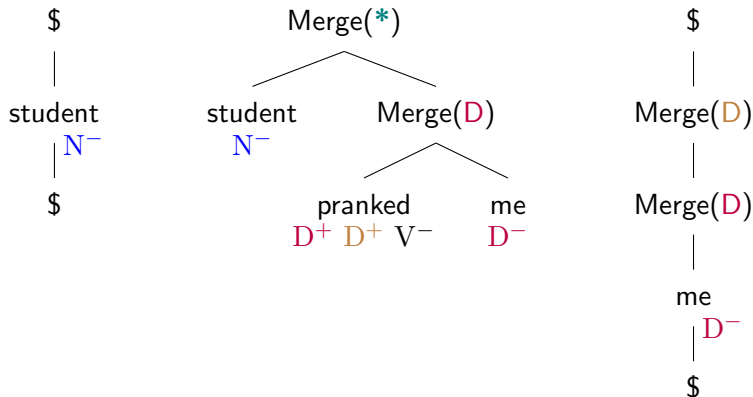
- ▶ This handles Merge.
- ▶ Moving on to Move...

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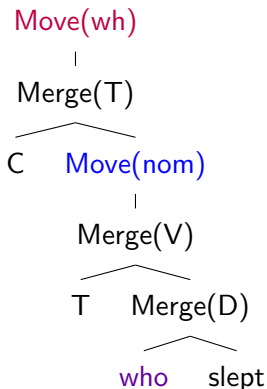
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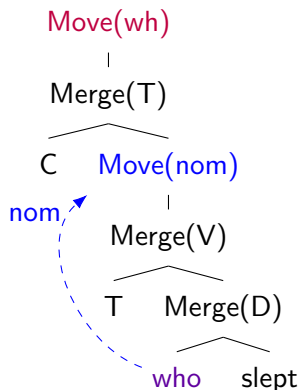
Move: Single Movement Normal Form

- ▶ **Assumption:** every phrase at most one movement feature
- ▶ Intermediate landing sites not feature-triggered
(Graf et al. 2016)



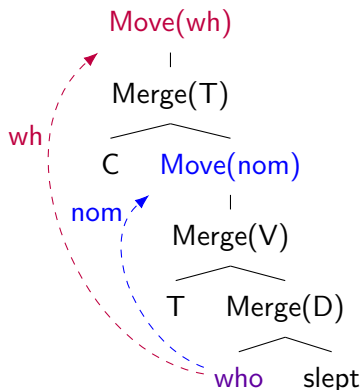
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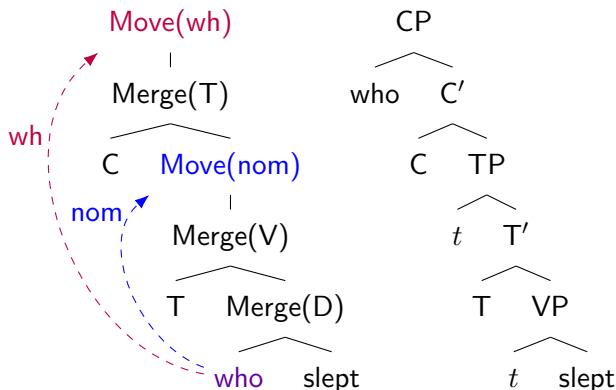
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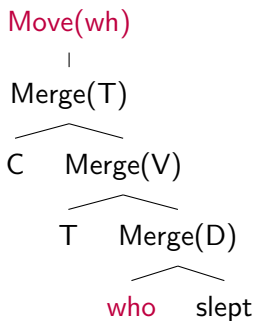
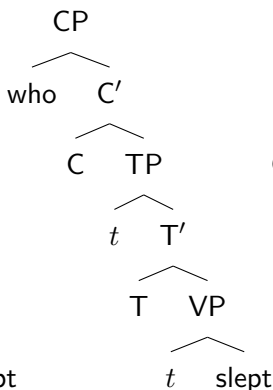
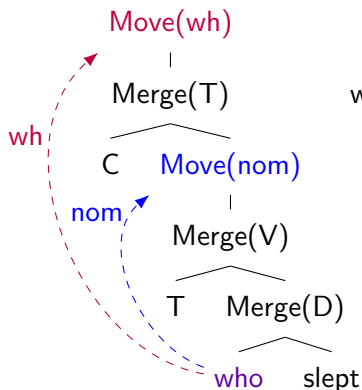
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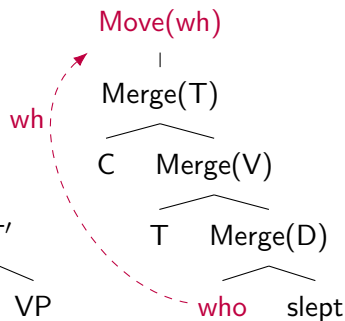
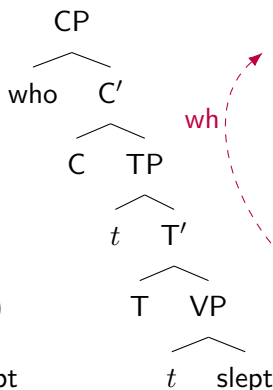
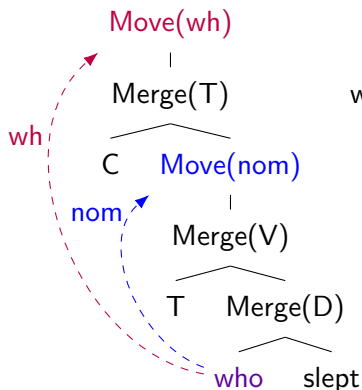
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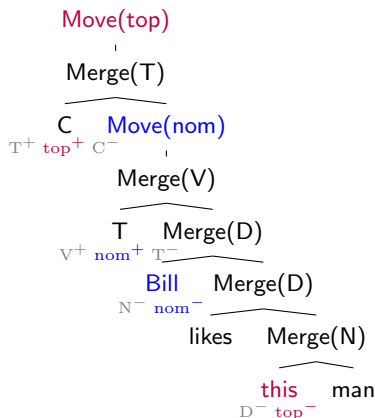
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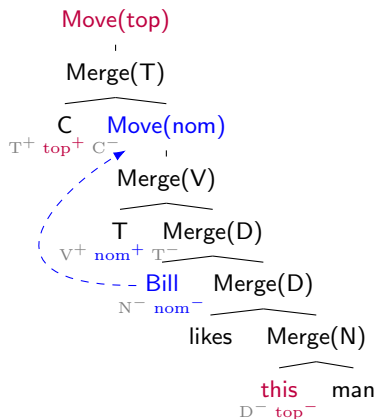
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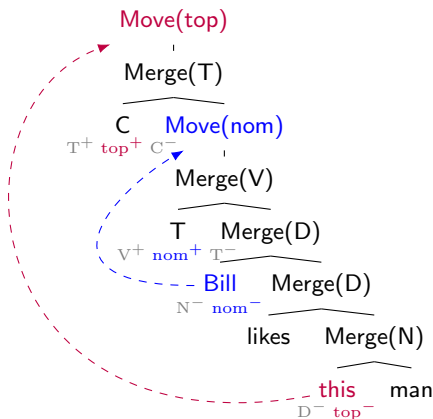
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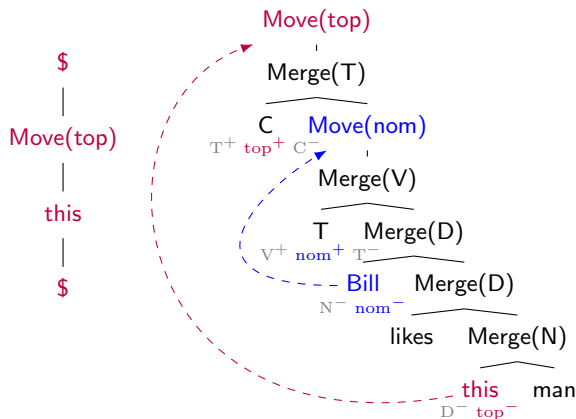
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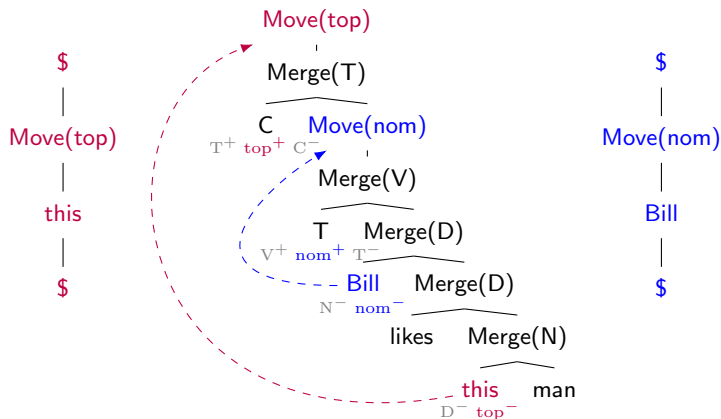
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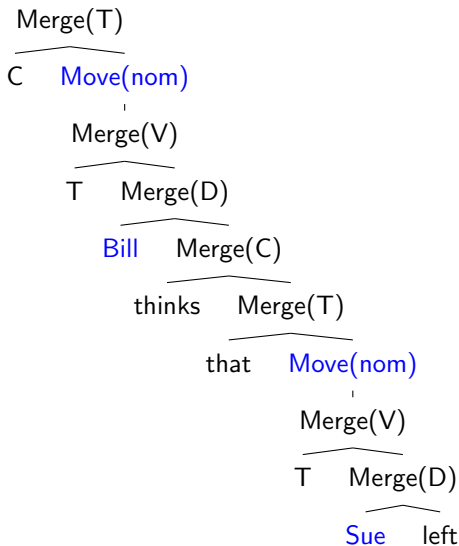


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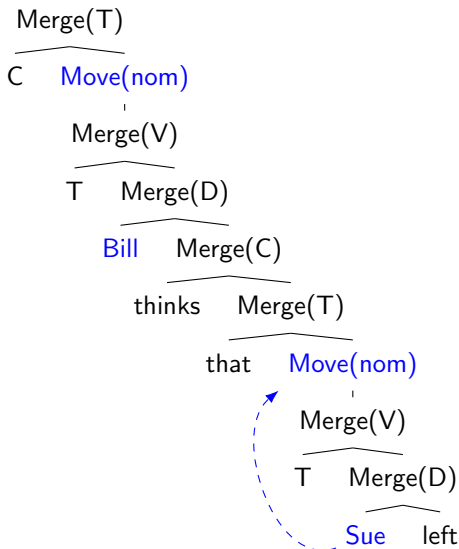
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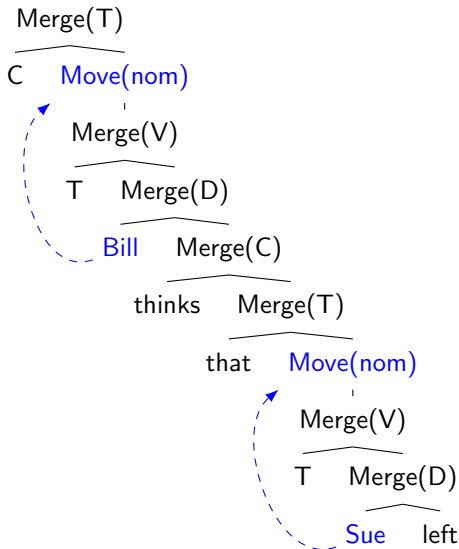
A Tier With Multiple Movers



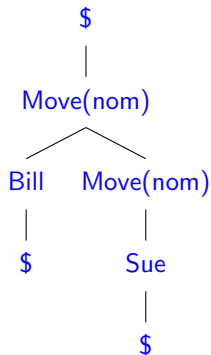
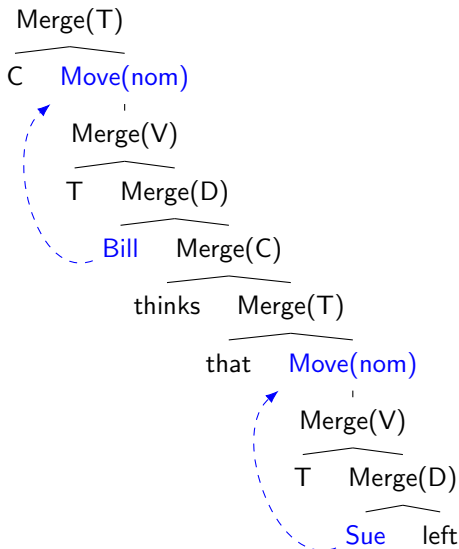
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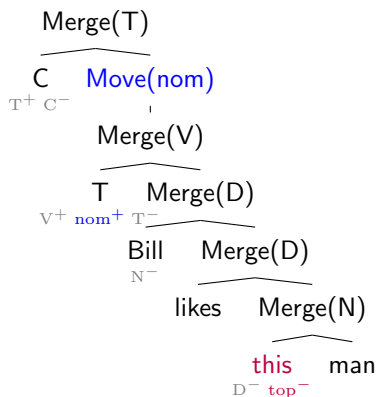
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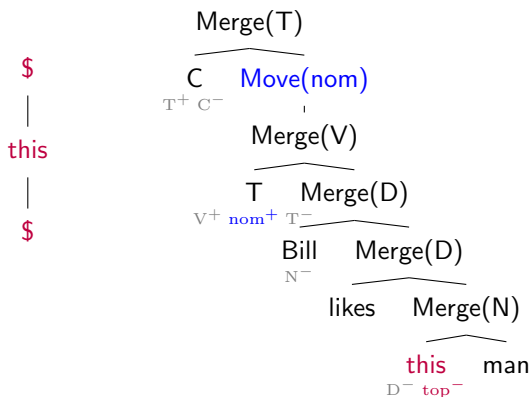
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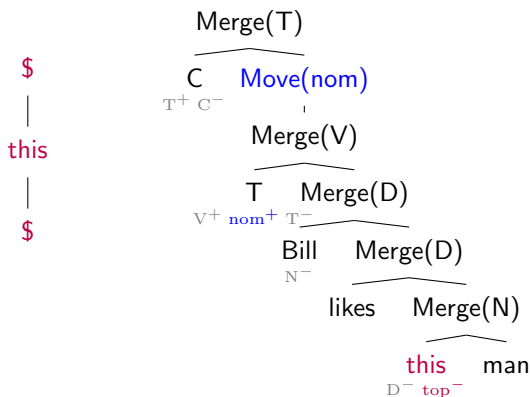
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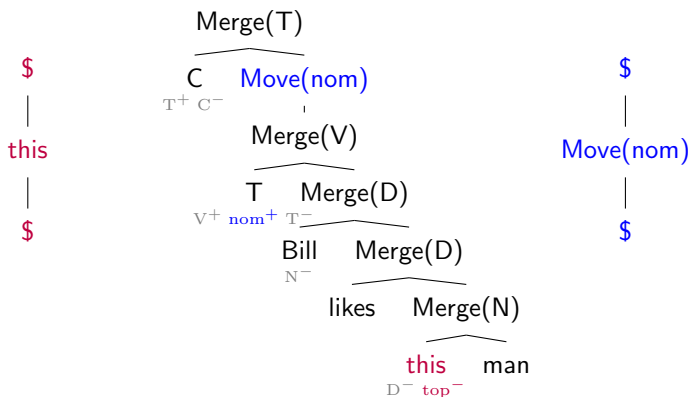
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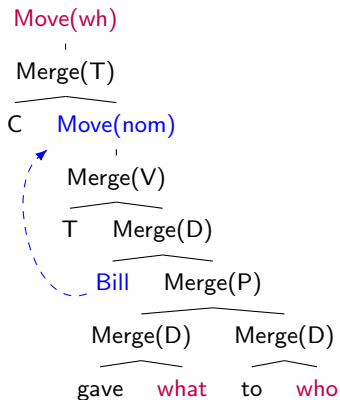
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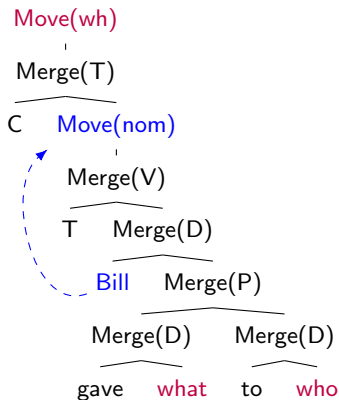
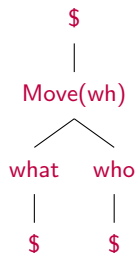
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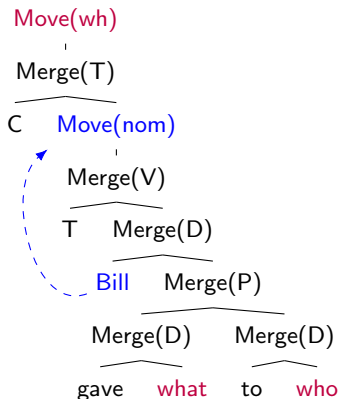
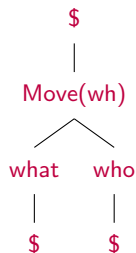
Blocking Many-to-One Movement



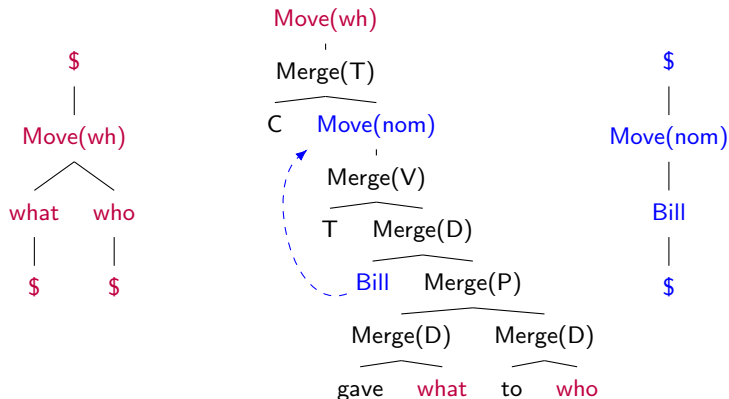
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Blocking Many-to-One Movement



Blocking Many-to-One Movement



The Common Core of Merge and Move

TSL Strategy for Merge

- ▶ Project tree tier for each **category** X .
- ▶ Every X^- has a **Merge** node as its mother.
- ▶ Every **Merge** node has exactly one X^- among its daughters.

TSL Strategy for Move

- ▶ Project tree tier for each **movement type** x .
- ▶ Every x^- has a **Move** node as its mother.
- ▶ Every **Move** node has exactly one x^- among its daughters.

Note: constraints again **highly local**

Summary

- ▶ Syntax looks like a complex outlier.
- ▶ But not if we choose appropriate representations:
 - ▶ c-command dependencies are TSL over c-strings
 - ▶ Merge and Move are TSL over derivation trees
- ▶ **Computational parallelism:**
 - ▶ phonology is TSL
 - ▶ morphology is TSL
 - ▶ syntax is TSL

Work In Progress

► **Movement**

- Interaction of movement and c-command
- Complexity without Single Movement Normal Form

► **Empirical work**

- limits of c-string constraints
- unified treatment of island constraints
- modeling specific phenomena
(e.g. case assignment)

► **Processing & Learning**

- compiling c-string constraints into MG parser
- learning via semantic bootstrapping

Open Issues

- ▶ experimental evidence for computational parallelism
- ▶ even tighter subclasses of TSL
- ▶ full predicted typology
- ▶ model concrete aspects of acquisition

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Join the program!

Resources and Readings

- 1 **Survey papers:** Pullum and Rogers (2006); Heinz (2011a,b, 2018); Rogers and Pullum (2011); Chandlee and Heinz (2016)
- 2 **TSL and its extensions:** Heinz et al. (2011); McMullin (2016); Baek (2017); De Santo (2017); De Santo and Graf (2017); Graf (2017c); Graf and Mayer (2018); Mayer and Major (2018); Yang (2018)
- 3 **TSL morphology:** Aksënova et al. (2016); Graf (2017b)
- 4 **TSL morpho-semantics:** Graf (2017d)
- 5 **TSL syntax:** Graf (2012a, 2018b); Graf and Shafiei (2019); Vu (2018); Vu et al. (2019)
- 6 **Mappings:** Courcelle and Engelfriet (2012); Chandlee (2014, 2017); Jardine (2016)
- 7 **Learnability:** Heinz (2010); Kasprzik and Kötzing (2010); Heinz et al. (2012); Jardine et al. (2014); Lai (2015); Jardine and Heinz (2016); Jardine and McMullin (2017)

Appendix

Psychological Reality of Derivation Trees

Central role of derivation trees backed up by **processing data**:

- ▶ Derivation trees can be parsed top-down (Stabler 2013)
- ▶ Parsing models update Derivational Theory of Complexity, make correct processing predictions for
 - ▶ right < center embedding (Kobele et al. 2013)
 - ▶ crossing < nested dependencies (Kobele et al. 2013)
 - ▶ SC-RC < RC-SC (Graf et al. 2017)
 - ▶ SRC < ORC in English (Graf et al. 2017)
 - ▶ SRC < ORC in East-Asian (Graf et al. 2017)
 - ▶ quantifier scope preferences (Pasternak 2016)
 - ▶ stacked relative clauses (Zhang 2017)
 - ▶ Korean attachment ambiguities

Technical Fertility of Derivation Trees

Derivation trees made it easy for MGs to accommodate the full syntactic toolbox:

- ▶ sideways movement (Stabler 2006; Graf 2013)
- ▶ affix hopping (Graf 2012b, 2013)
- ▶ clustering movement (Gärtner and Michaelis 2010)
- ▶ tucking in (Graf 2013)
- ▶ ATB movement (Kobele 2008)
- ▶ copy movement (Kobele 2006)
- ▶ extraposition (Hunter and Frank 2014)
- ▶ Late Merge (Kobele 2010; Graf 2014a)
- ▶ Agree (Kobele 2011; Graf 2012a)
- ▶ adjunction (Fowlie 2013; Graf 2014b; Hunter 2015)
- ▶ TAG-style adjunction (Graf 2012c)

Even More MG Extensions

- ▶ local and global constraints (Kobele 2011; Graf 2012a, 2017a)
- ▶ transderivational constraints (Graf 2010, 2013)
- ▶ Principle A and B (Graf and Abner 2012)
- ▶ GPSG-style feature percolation (Kobele 2008)
- ▶ idioms (Kobele 2012)
- ▶ grafts (multi-rooted multi-dominance trees) (Graf in progress)

Long Story Short

Derivation trees are a more useful and fertile data structure than phrase structure trees.

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References I

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