# Grammar Size and Quantitative Restrictions on Movement 

## Thomas Graf

Stony Brook University<br>mail@thomasgraf.net<br>http://thomasgraf.net

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## Outline

1 Movement in Minimalist Grammars

- Merge and Move
- Intermediate Movement

2 Single Movement Normal Form

3 Movement Constraints and Grammar Size: A Curious Conspiracy

## Minimalist Grammars (MGs)



- Minimalist grammars (MGs) are a formalization of Chomskyan syntax (Stabler 1997, 2011)
- Succinct formalism for defining MCFGs
- Operations: Merge and Move
- Grammar is just a finite list of feature-annotated lexical items (LIs)

| Chemistry | Syntax |
| :---: | :---: |
| atoms | words |
| electrons | features |
| molecules | sentences |

## Merge

Merge combines subtrees to encode head-argument dependencies.
category feature $\mathrm{N}^{-}, \mathrm{V}^{-}, \ldots$
selector feature $\mathrm{N}^{+}, \mathrm{V}^{+}, \ldots$
$\frac{\text { the }}{\mathrm{N}^{+} \mathrm{D}^{-}} \frac{\text { men }}{\mathrm{N}^{-}} \frac{\text { like }}{\mathrm{D}^{+} \mathrm{D}^{+} \mathrm{V}^{-}} \frac{\text { which }}{\mathrm{N}^{+} \mathrm{D}^{-}} \frac{\text { men }}{\mathrm{N}^{-}}$

- the and men have matching features, triggering Merge
- same steps for which men
- like merged with which men
- like merged with the men


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## Merge in Derivation Trees



Derived Tree


## Move

Move displaces subtrees to derive the correct linear order.
licensee feature wh $^{-}$, top $^{-}, \ldots$ licensor feature $\mathrm{wh}^{+}$, top $^{+}, \ldots$


- Merge do
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## Move in Derivation Trees



## Move in Derivation Trees



## Intermediate Movement

Intermediate movement is possible, but has no effect on output.


## An Issue with Intermediate Movement

Minimalist analyses posit an unbounded number of intermediate landing sites.
(1) Who does John think $t$ that Mary believes $t$ that Sue said $t$ that ... $t$ that Bill hates $t$ ?

But every LI can only carry finitely many features!


## Derivational Solution (Kobele 2006)

- Only final landing site has feature.
- Intermediate movement is inserted by mapping to phrase structure trees


## Recipe for Successive Cyclic Movement

Add trace in every crossed Spec,CP.


## Generalization: No Intermediate Movement (Graf et al. 2016)



Alëna Aksënova


Aniello De Santo

- Kobele's solution can be generalized.
- Intermediate movement never needs to be feature triggered.
- It is derivationally redundant.

Definition (Single Movement Normal Form)
An MG is in single movement normal form (SMNF) iff every LI has at most one licensee feature.

## Theorem

For every MG there is a strongly equivalent $M G$ that is in SMNF.

## An Annoying Complication

MGs have one central locality restriction on Move.

## Shortest Move Constraint (SMC)

If two LIs in a tree both have a licensee feature as their first currently unchecked feature, then these features must be distinct.


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## A Work-Around with Subscripts

## Feature Subscripting

- For every LI $l$, only keep its last licensee feature.
- Add subscripts to licensee features to avoid SMC violations.



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## Lexical Blow-Up

- SMNF translation induces linear lexical blow-up
- Effect varies a lot depending on movement configurations:
lower bound linear size reduction(!),
1:1 for non-redundant grammars
upper bound large linear blow-up

$$
\sum_{\mathbf{l} \in \mathrm{Lex}} \mu^{\gamma(1)+\delta(1)}
$$

$\mu \ldots$ maximum number of required indices
$\gamma(1) \ldots$ number of licensor features of $\mathrm{LI} l$ in original grammar
$\delta(1) \ldots 1$ if $l$ has licensee features, 0 otherwise

## Abstract Example (Sketch)



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## Abstract Example (the Math)

- The original grammar contains a single LI.

$$
\mathrm{c}:: \mathrm{C}^{+} \mathrm{g}^{+} \mathrm{f}^{+} \mathrm{C}^{+} \mathrm{g}^{+} \mathrm{f}^{+} \mathrm{C}^{-} \mathrm{g}^{-} \mathrm{f}^{-}
$$

- The SMNF grammar contains 8 variants.

$$
\begin{array}{lll}
\mathrm{c}:: \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{-} \mathrm{f}_{0}^{-} & \mathrm{c}:: \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{-} \mathrm{f}_{1}^{-} \\
\mathrm{c}:: \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{+} \mathrm{f}_{1}^{+} \mathrm{C}^{-} \mathrm{f}_{0}^{-} & \mathrm{c}:: \mathrm{C}^{+} \mathrm{f}_{0}^{+} \mathrm{C}^{+} \mathrm{f}_{1}^{+} \mathrm{C}^{-} \mathrm{f}_{1}^{-} \\
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\end{array}
$$

- We can get n variants of the LI by changing the phonetic exponent, so the grammar size increases at least by 8 n .
- But we can keep increasing number $m$ of arguments:

$$
2^{m+1} \times n
$$

## Interim Summary

- Every MG is a finite set of LIs.
- The more LIs, the larger the grammar.
- Derivation trees are the primary data structure.
- Intermediate movement is derivationally redundant and costly:
- complicates proofs
- increases computational complexity (Graf and Heinz 2015)
- at odds with MG processing models (Graf et al. 2017)
- But SMNF MGs may be much larger, which is bad for
- parsing
- learning
- explanatory adequacy


## A New Empirical Puzzle

Are the movement configurations we find in natural language exactly those that induce little lexical blow-up?

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Are the movement configurations we find in natural language exactly those that induce little lexical blow-up?

## What Produces a Large Blow-Up in Grammar Size?

- Large blow-up occurs whenever there are multiple Lls s.t.

1 they all have the same final movement feature, and
2 they have overlapping movement paths, and
3 their relative configuration is not fixed across derivations.

- That's easy to do with abstract examples, but natural examples are tough.


## The Constraint-Grammar-Size Conspiracy

Patterns that would induce a large blow-up are independently forbidden.

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## Improper Movement



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John wonders who Bill saw.

## Improper Movement



John wonders who Bill saw.

## Improper Movement



## Superraising



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## Freezing Effects

- One could also get overlapping paths by extracting an $f$-mover from within an $f$-mover.
- But this produces freezing effects.
(5) It seems your comment about John annoys Sue.
(6) * John seems your comment about $t$ annoys Sue.
(7) * Who don't you know [which pictures of $t$ ] Mary bought.


## Wh-Islands

- Multiple $\mathrm{A}^{\prime}$-movers of the same type would also be an option.
- But here the wh-island constraint intervenes.
(8) a. What ${ }_{w h}$ did John say Mary gave $t_{w h}$ to Bill?
b. *What ${ }_{w h 0}$ did John say $w h o_{w h 1}$ Mary gave $t_{w h 0}$ to $t_{w h 1}$ ? (Wh-island violation)
c. * What ${ }_{\text {who }}$ did Bill think which $_{w h 1}$ man $t_{w h 1}{\text { says } \text { who }_{w h 1} \text { }}$ Mary gave $t_{w h o}$ to $t_{w h 1}$ ?
d. * What ${ }_{w h 0}$ did Sue claim who ${ }_{w h 1}$ Bill thinks which ${ }_{w h 2}$ man $t_{w h 2}$ says Mary gave $t_{w h 0}$ to $t_{w h 1}$ ?


## Taking Stock

- MGs are all about two structure-building operations: Merge and Move.
- Intermediate movement complicates formalism
- SMNF simplifies MGs, but at the risk of larger lexicons.
- Realistic grammars block the truly dangerous configurations.
- Unclear whether this is coincidence or conspiracy


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