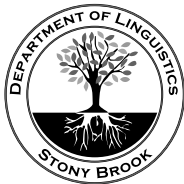


Formal and Substantive Universals Across Language Modules

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Surrey Linguistics Circle
January 31, 2023



Take-home message

Descriptive observation: Monotonicity beyond semantics

- ▶ Monotonicity shows up **a lot** across linguistic domains.
- ▶ Monotonicity ties together seemingly unrelated phenomena.

A bigger picture

- ▶ Formal universals can be stated independently of formalism
- ▶ Substantive universals as domain-specific hierarchies

Take-home message

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- ▶ Substantive universals as domain-specific hierarchies

Outline

- 1 Monotonicity: what and why?
- 2 Monotonicity in morphology and morphosyntax
 - Adjectival gradation and person pronoun syncretism
 - Tense syncretism
 - Person Case Constraint & Gender Case Constraint
 - Omnivorous number
- 3 Monotonicity in syntax
 - Expletive negation and 3/4 splits
 - Reference to hybrid nouns
 - Ban against improper movement
 - Corollary: Ban against improper selection
 - Order preservation in Fox & Pesetsky (2005)
 - Freezing effects

Monotonicity

Definition (Monotonicity)

- ▶ Let **A** and **B** be two sets with orders $\leq_{\mathbf{A}}$ and $\leq_{\mathbf{B}}$, respectively.
- ▶ A function **f** from **A** to **B** is **monotonic**(ally increasing) iff

$$x \leq_{\mathbf{A}} y \Rightarrow \mathbf{f}(x) \leq_{\mathbf{B}} \mathbf{f}(y)$$

- ▶ Monotonicity is similar to **No Crossing Branches** constraint.

1	2	3
A	B	C

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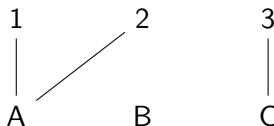
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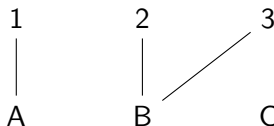
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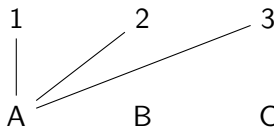
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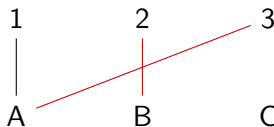
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Monotonicity in cognition

- ▶ Monotonicity shows up quite a bit in cognition.
- ▶ In mathematical learning theory, monotonicity provides safe and efficient inference.
- ▶ Modeling-based work on learning shows similar trend (Carcassi et al. 2021)
- ▶ Monotonicity is related to convexity, which shows up with color terms. (Gärdenfors 2000)

*ABA as a special case of monotonicity

*ABA generalization (Bobaljik 2012)

Given an underlying hierarchy $x < y < z$,
 z cannot pattern with x to the exclusion of y .

Example

- ▶ Adjectival gradation: *good — better — goodest
- ▶ Pronoun paradigm: *I — you — I (cf. Harbour 2015)

Usually explained via

- ▶ containment (Bobaljik 2012)
- ▶ feature combinatorics (Bobaljik and Sauerland 2017)

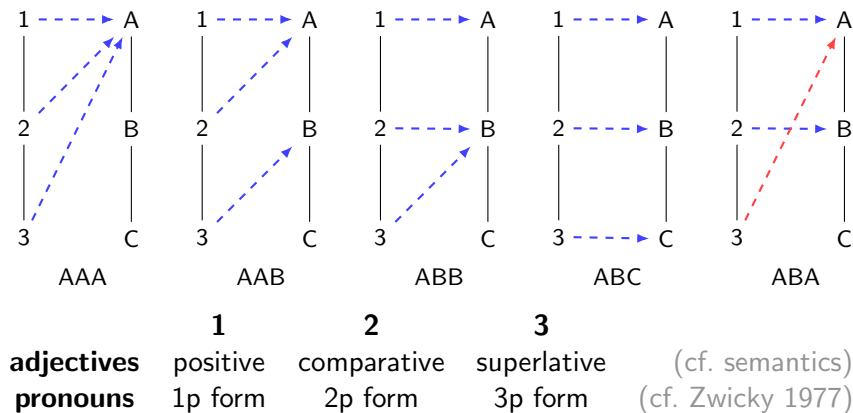
Monotonicity subsumes *ABA

- ▶ Monotonicity provides a high-level account that abstracts away from causal mechanisms.
- ▶ **General recipe**
 - 1 Identify a base hierarchy
(ideally: grounded, non-arbitrary)
 - 2 Map from hierarchy into another structure
(surface forms, well-/ill-formed, ...)
 - 3 Mapping must be monotonic

A corollary of monotonicity

- ▶ If $x \leq y \leq z$, then it cannot hold that $f(x) = f(z) \neq f(y)$.
- ▶ Hence monotonicity enforces *ABA for linear orders.

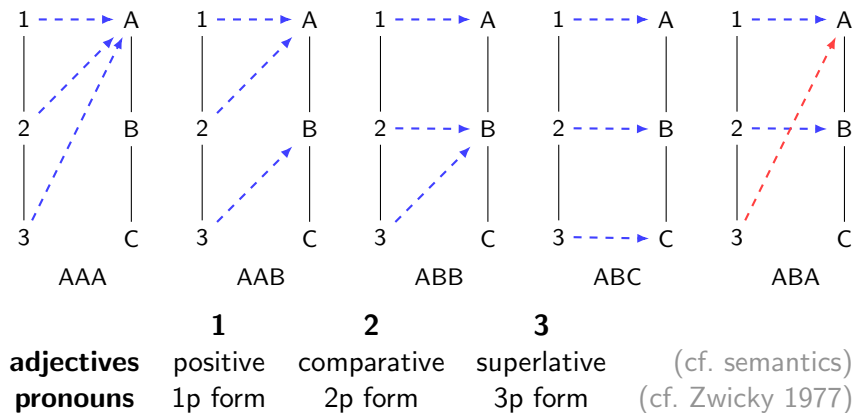
*ABA for adjectives and pronouns



What about *AAB in adjectival gradation?

Monotonicity carves out general space of options,
grammar may not be able to realize all of them.

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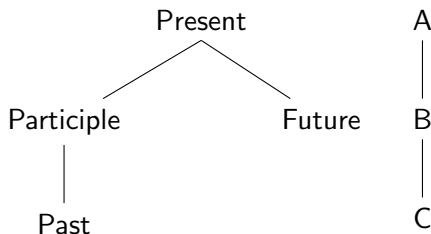
Collateral monotonicity damage in the grammar

- ▶ Suppose the mechanism's of the grammar allow us to build
 - 1 patterns AAA, ABB, ABC via mechanism X,
 - 2 patterns AAB and ABA via mechanism Y.

Mechanism X	Mechanism Y
AAA	AAB
ABB	ABA
ABC	

- ▶ Then monotonicity, by virtue of discriminating against ABA, pushes the grammar away from mechanism Y.
- ▶ The AAB pattern is **collateral damage**.
- ▶ **Disclaimer:** Pure speculation; meant to show how monotonicity approach could integrate with grammar approach

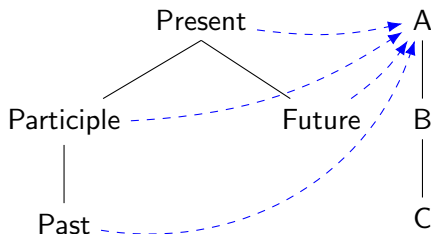
Beyond linear orders: *ABA for tense



**Sophie
Moradi**

- **Forbids:**
present = past $\neq$ participle
- **Allows:**
present = participle $\neq$ future, past
present = future $\neq$ participle = past
present $\neq$ participle = future $\neq$ past
- Hierarchy derived from Reichenbach

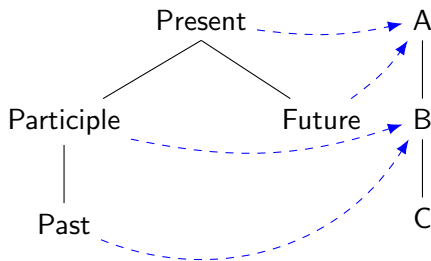
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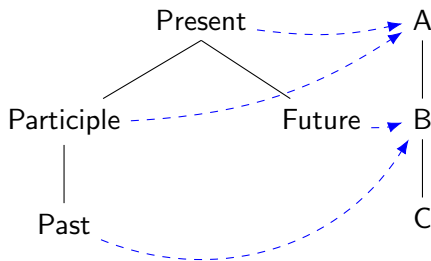
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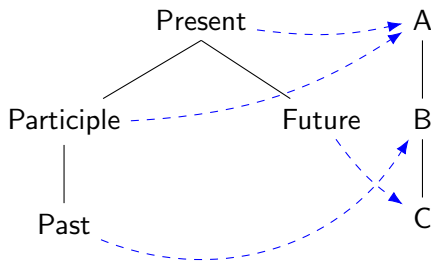
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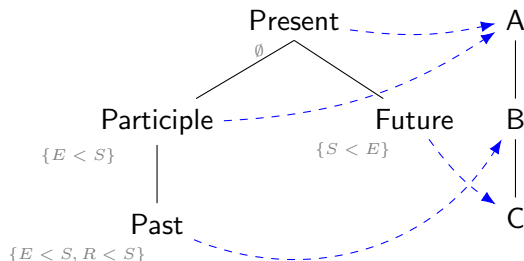
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Person Case Constraint

- ▶ Monotonicity handles the attested PCCs, too. (Graf 2019)

Example: Person Case Constraint (PCC; Bonet 1994)

The well-formedness of clitic combinations is contingent on their person specification.

- (1) Roger *le/*me* *leur* a présenté.
Roger 3SG.ACC/1SG.ACC 3PL.DAT has shown
'Roger has shown me/him to them.'

- ▶ Out of 64 conceivable PCC variants, **only 5 are attested**.
- ▶ Monotonicity provides a (partial) answer.

Building a hierarchy for PCCs

- ▶ PCCs are about person specifications of IO-DO pairs
⇒ start with **Zwicky's person hierarchy**:

$$1 < 2 < 3$$

- ▶ Associate each IO-DO pair with their **person prominence differential**:

Differential	IO-DO combinations
--------------	--------------------

2	1,3
---	-----

1	1,2 2,3
---	---------

0	1,1 2,2 3,3
---	-------------

-1	2,1 3,2
----	---------

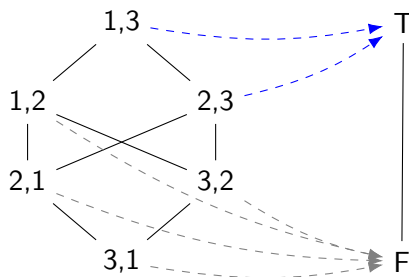
-2	3,1
----	-----

- ▶ Order combinations from greatest differential to lowest.

The PCC mappings

IO↓/DO→	1	2	3
1	NA	*	✓
2	*	NA	✓
3	*	*	NA

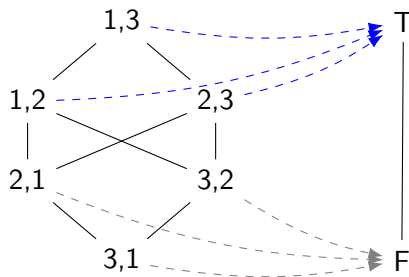
Strong PCC



The PCC mappings

IO↓/DO→	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	*	NA

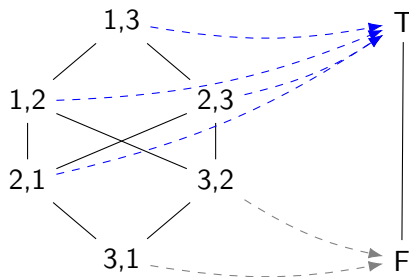
Ultrastrong PCC



The PCC mappings

IO↓/DO→	1	2	3
1	NA	✓	✓
2	✓	NA	✓
3	*	*	NA

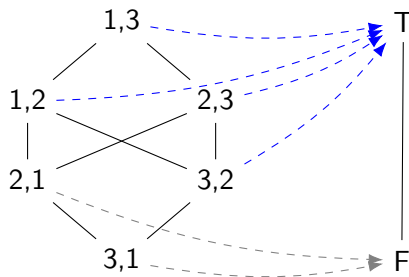
Weak PCC



The PCC mappings

IO↓/DO→	1	2	3
1	NA	✓	✓
2	*	NA	✓
3	*	✓	NA

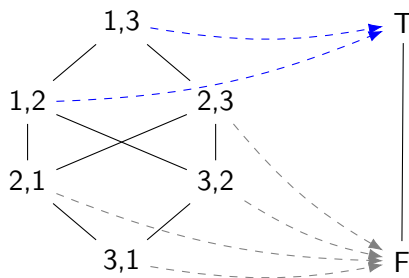
Me-first PCC



The PCC mappings

IO↓/DO→	1	2	3
1	NA	✓	✓
2	*	NA	*
3	*	*	NA

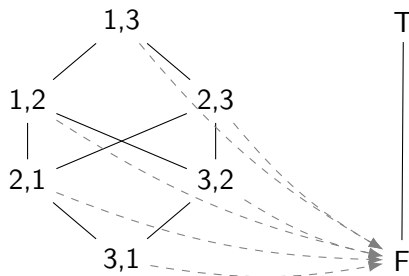
Choctaw PCC (Tyler 2017)



The PCC mappings

IO↓/DO→	1	2	3
1	NA	*	*
2	*	NA	*
3	*	*	NA

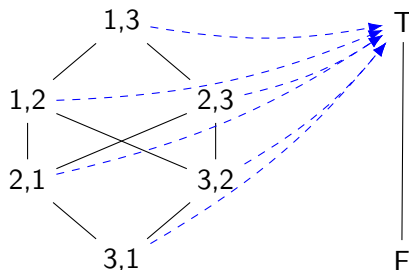
Cairene Arabic (Shlonsky 1997)



The PCC mappings

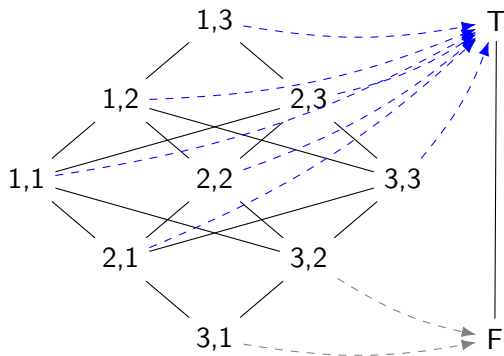
IO↓/DO→	1	2	3
1	NA	✓	✓
2	✓	NA	✓
3	✓	✓	NA

Free combination



Assumed identity constructions in German

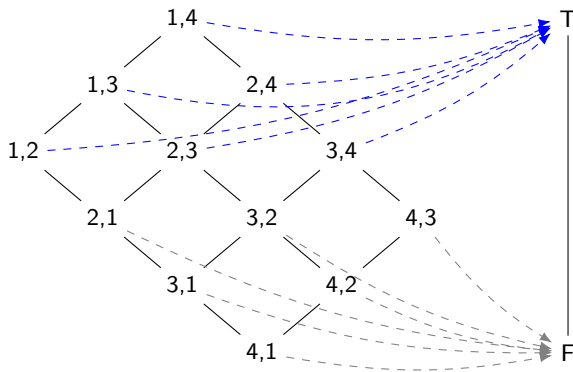
<i>be</i>	Obj1	Obj2	Obj3
Subj1	Ich bin ich	Ich bin du	Ich bin er
Subj2	Du bist ich	Du bist du	Du bist er
Subj3	*Er ist ich	*Er ist du	Er ist er



Gender Case Constraint

IO↓/DO→	1	2	3	4
1	NA	✓	✓	✓
2	*	NA	✓	✓
3	*	*	NA	✓
4	*	*	*	NA

Zapotec GCC (Foley et al. 2017)



Interim summary

General approach

- 1 Pick an underlying hierarchy
 - 2 Map to output values (surface forms, grammaticality, ...)
 - 3 Monotonic?
- ▶ Monotonicity provides a succinct, unified description of seemingly unrelated phenomena.
 - ▶ Let's look at one more case that's odd from the standard perspective.

Omnivorous number (Nevins 2011)

- ▶ In some languages, verbs agree with **subject and object**
- ▶ Some of these languages display **omnivorous number**.

Omnivorous number: √ for agreement

If subject or object is plural, verbal agreement is plural.

S	O	V
sg	sg	sg
sg	pl	pl
pl	sg	pl
pl	pl	pl

(2) g- xedav- t
 2NDOBJ- saw- PL

Georgian (Nevins 2011:950)

1 I saw y'all

2 We saw you

3 We saw y'all

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Georgian (Nevins 2011:950)

- 1 I saw y'all
- 2 We saw you
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A curious typological gap...

Unattested: $\wedge$ for agreement

If subject or object is singular, verbal agreement is singular.

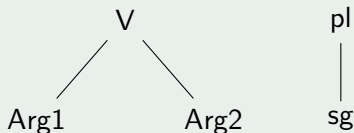
S	O	V
sg	sg	sg
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- Syntactic explanations of this fact exist.
- They make omnivorous number look special.

The monotonicity perspective

- ▶ both arguments must receive number before V does
- ▶ but number values of arguments are independent of each other

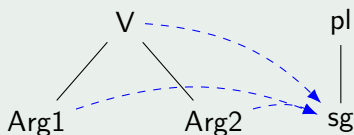
Monotonicity + agreement order = Omnivorous number



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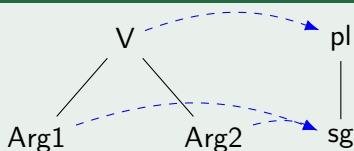


Uniform agreement

The monotonicity perspective

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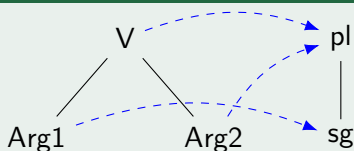


Unattested?

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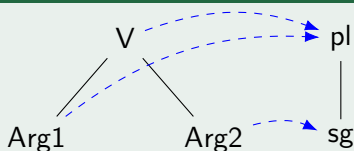


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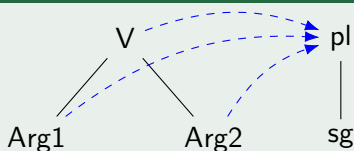


Omnivorous number

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Monotonicity + agreement order = Omnivorous number



Uniform agreement

But what if...?

- ▶ We could have used the **dual** of one of those hierarchies.
- ▶ We could we have replaced monotonicity with **antitonicity**.
- ▶ Either one allows for $\wedge$ -agreement.

What this approach is about

- ▶ Correct, we could have done things differently.
- ▶ The point is not that $\vee$ -agreement is more natural than $\wedge$ -agreement.
- ▶ But monotonicity predicts that it is impossible to have both.
- ▶ Since $\vee$ -agreement exists, $\wedge$ -agreement is ruled out.

Venturing into syntax: Expletive negation and 3/4 splits

- ▶ Typology often reveals **3/4 splits**:
out of 4 conceivable options, only 3 are found.
- ▶ Those could all be instances of monotonicity.

Expletive negation

- (3) Bevor die Lage sich **nicht** entspannt, können wir
before the situation SE not improves, can we
nicht reisen.
not travel
'We can't travel until the situation improves.'

Languages may allow expletive negation

- 1 not at all,
- 2 only with T[+fin],
- 3 with T[+fin] and T[-fin].

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T[+fin]

|

T[-fin]

T

|

F

Venturing into syntax: Expletive negation and 3/4 splits

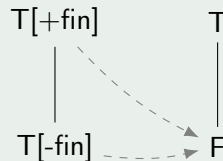
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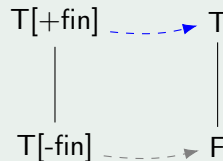
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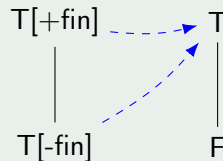
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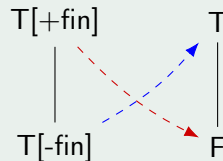
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German *Mädchen* 'girl' and pronouns

- ▶ *Mädchen* is grammatically neuter but semantically neuter.
- ▶ Once a coreferent pronoun agrees with semantic gender, all subsequent coreferent pronouns must also agree with semantic gender

⇒ **once semantic, always semantic**

- (4)
- a. Das Mädchen_i bittet **seine**_i Mutter **es**_i zu küssen.
the girl asks **its** mother **it** to kiss
 - b. Das Mädchen_i bittet **ihre**_i Mutter **sie**_i zu küssen.
the girl asks **her** mother **her** to kiss
 - c. Das Mädchen_i bittet **seine**_i Mutter **sie**_i zu küssen.
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A monotonicity account

- 1 sort coreferent pronouns by the order in which they occur
- 2 Gender type hierarchy: grammatical gender $<$ semantic gender
- 3 Mapping from coreferent pronouns to gender type hierarchy must be monotonic.

Monotonic pronoun reference

Gender type hierarchy: grammatical $<$ semantic

Coreferent pronouns:

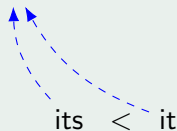
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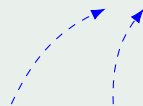
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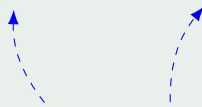
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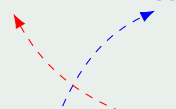
Monotonic pronoun reference

Gender type hierarchy:

grammatical < semantic

Coreferent pronouns:

her < its



Disclaimer: there are exceptions

- ▶ An example from an Austrian pop song
(*Cinderella* by EAV)

(5) Es lebte einst ein junges Mädel, Cinderella war **ihr**
there lived once a young girl, Cinderella was **her**
Nam'. Und **es** wartete vergebens auf den Prinz, der
name. And **it** waited in vain for the prince who
niemals kam.
never came

- ▶ But monotonicity could be a markedness condition.

A-movement and A'-movement

► A-movement phenomena

- (6) a. John was attacked *t*.
b. John seems *t* to have *t* cut the carrot.

► A'-movement phenomena

- (7) a. This girl, John thinks that Mary likes *t*.
b. Who does John think *t* might *t* cut the carrot?

Ban Against Improper Movement

Once a phrase undergoes A'-movement,
it can no longer undergo A-movement.

(But: possible exception in Brazilian Portuguese; Kobayashi 2020)

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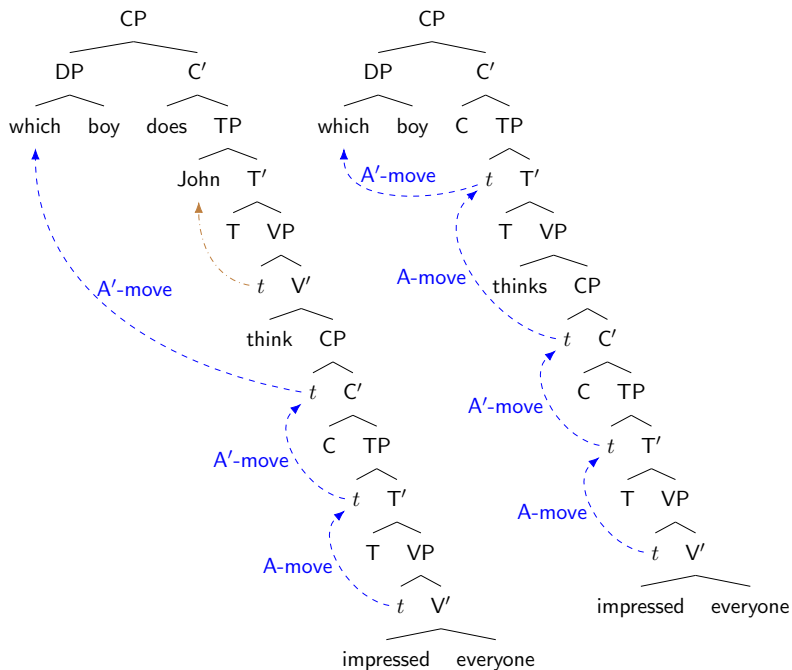
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Why should there be a ban against improper movement?

- ▶ Formalisms vary in how they derive this ban.
- ▶ They usually require extra stipulations.
- ▶ We can derive it from monotonicity.

Monotonicity + locality = Ban Against Improper Movement

Locality hierarchy: A-move < A'-move

Derivation:

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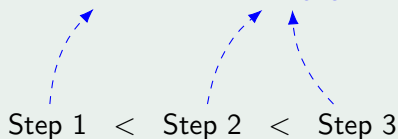
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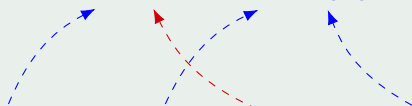
Monotonicity + locality = Ban Against Improper Movement

Locality hierarchy:

A-move < A'-move

Derivation:

Step 1 < Step 2 < Step 3 < Step 4



A welcome corollary: Ban Against Improper Selection

- ▶ Selection combines heads with their arguments.
- ▶ Selection is even more local than A-movement:

Select < A-move < A'-move

- ▶ **Corollary:**
Once a phrase undergoes any movement, it can no longer select an argument or be selected as an argument.
- ▶ This is widely considered to be the case.
(But: Late Merge of arguments; Takahashi and Hulsey 2009; Stanton 2016)

Williams Cycle

General definition (paraphrasing Williams 1974)

- ▶ Assume some fixed order $<$ of heads. For example:

$$V < v < T < C$$

- ▶ If a phrase resides in in Spec,**X**P, then it cannot move to any Spec,**Y**P such that **Y** $<$ **X**.

Monotonicity + head order = Williams Cycle

Head hierarchy: $V < v < T < C$

Derivation:

Williams Cycle

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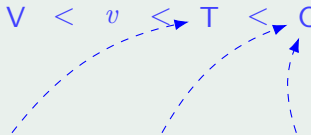
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$$V < v \leq T < C$$

Derivation:

$$\text{Step 1} < \text{Step 2} < \text{Step 3}$$



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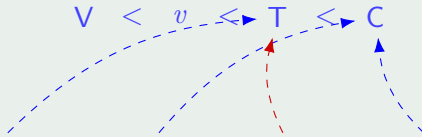
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Derivation:

Step 1 < Step 2 < Step 3 < Step 4



Ban Against Improper Case

A constraint on Dependent Case Theory (Poole 2018)

- ▶ Assume some fixed order $<$ of syntactic positions.
- ▶ NP in position **X** cannot license case on NP in position **Y** if there is some position **Z** such that
 - 1 **Z** occurs between **X** and **Y**, and
 - 2 **X** $<$ **Z**

Example

(8) $[_{TP} \text{ John } [_{vP} \text{ told } [_{VP} \text{ Mary } [_{CP} \text{ that } [_{TP} \text{ Bill had left}]]]]]$.

- 1 *Mary* licensed by *John*: $V < v < T$
- 2 **Bill* licensed by *Mary*: $T < C < V$

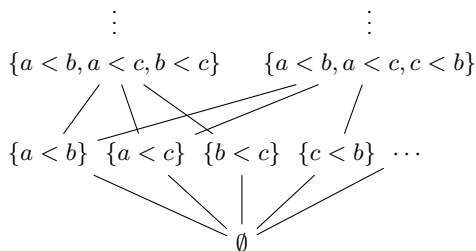
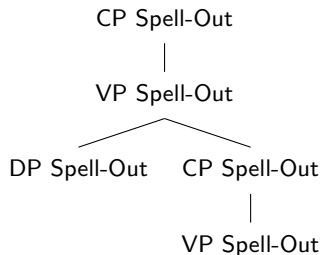
Order preservation in Fox and Pesetsky (2005)

System in a nutshell

- 1 When phase completed, determine ordering statements ($a < b$) between nodes
- 2 New ordering statements must not contradict old ones.

Formally:

Monotonic map from Spell-Outs to sets of ordering statements



Freezing effects

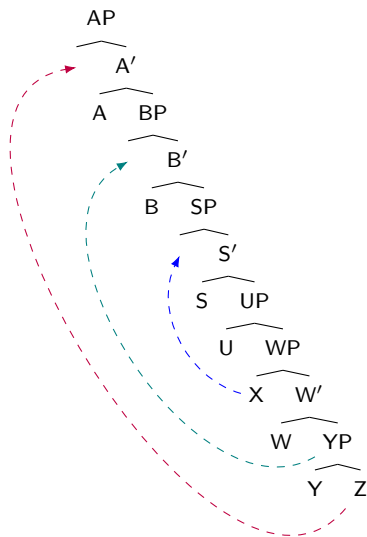
General observation

- ▶ A phrase cannot be extracted from a containing phrase that has already undergone movement.
- ▶ **But:** you can escape by moving out first.

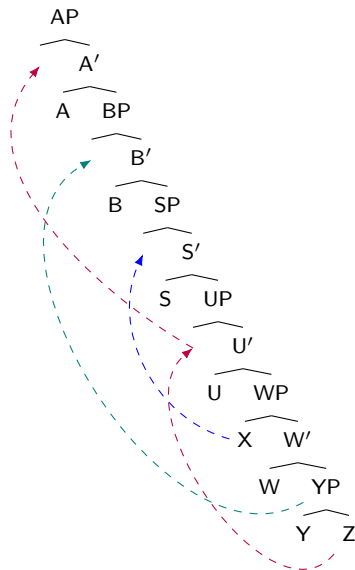
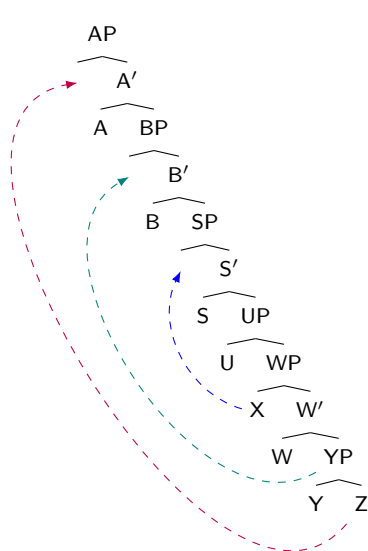
Intuitive solution

- ▶ Two phases in “life” of a head/phrase
 - 1 Merge phase
 - 2 Move phase
- ▶ Two orderings connected via monotonicity:
 - 1 relative prominence established by Merge
 - 2 relative order in which heads transition into Move phase

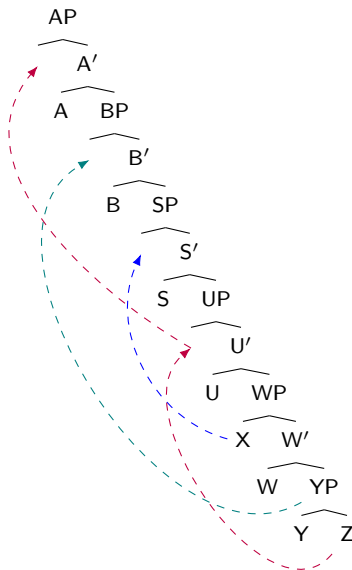
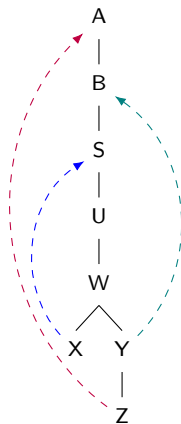
An abstract freezing example



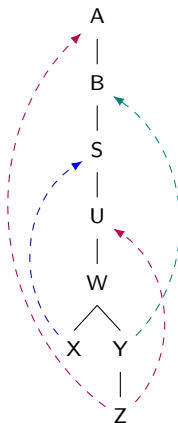
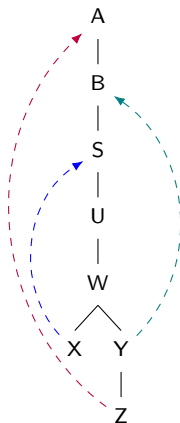
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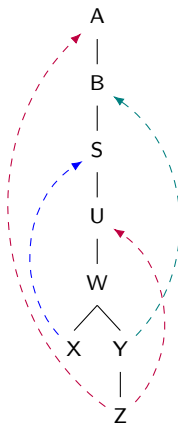
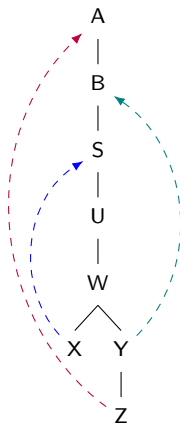
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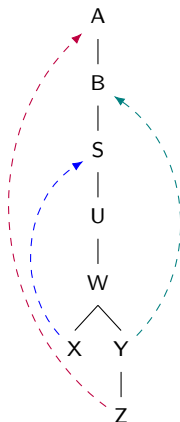


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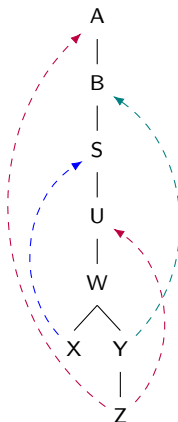


Move transition: $X < Y < Z$

An abstract freezing example



Move transition: $X < Y < Z$



Move transition: $Z < X < Y$

Monotonicity in morphology

- ▶ Adjectival gradation (Graf 2019)
- ▶ Pronoun syncretism (Graf 2019)
- ▶ Case syncretism (Graf 2019)
- ▶ Case stem syncretism (Graf 2019)
- ▶ Tense syncretism (Sophie Moradi's thesis)
- ▶ Resolved gender agreement (Sophie Moradi's thesis)
- ▶ Person-number syncretism (Sophie Moradi's thesis)
- ▶ Inverse marking (possibly, needs more work)

Monotonicity in syntax

- ▶ Person Case Constraint (Graf 2019)
- ▶ Gender Case Constraint (Graf 2019)
- ▶ Assumed identity constructions (this talk)
- ▶ Reference to hybrid nouns (this talk)
- ▶ Ban Against Improper Movement/Selection (Graf 2020)
- ▶ Williams Cycle (Graf 2020)
- ▶ Ban Against Improper Case (Graf 2020)
- ▶ Omnivorous number (Graf 2020)
- ▶ Adjunct Island Constraint (Graf 2013)
- ▶ Coordinate Structure Constraint (same as AIC)
- ▶ Keenan-Comrie hierarchy (by definition)
- ▶ Freezing effects (this talk)

Conclusion

- ▶ Monotonicity goes beyond semantics
- ▶ Unified perspective on seemingly unrelated phenomena

The general approach

plausible hierarchies	+	monotonicity	= bingo
substantive universal	+	formal universal	= bingo

The road ahead: From cute idea to research program

- ▶ proper theory of what is a possible hierarchy
- ▶ hard constraint or markedness?
- ▶ phenomena that do not care about monotonicity at all

Acknowledgments

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