



Tiers and Relativized Locality Across Language Modules

Thomas Graf Aniello De Santo Jon Rawski Alëna Aksënova Hossep Dolatian Sedigheh Moradi Hyunah Baek Suji Yang Jeffrey Heinz

Stony Brook University aniello.desanto@stonybrook.edu https://aniellodesanto.github.io/

Parallels Between Phonology & Syntax Amsterdam, July 9, 2018

The Subregular Group @ SBU



Jeff Heinz



Thomas Graf



Alëna Aksënova



Sedigheh Moradi



Hyunah Baek



Jon Rawski



Hossep Dolatian



Suji Yang

The Elevator Pitch

Parallels between phonology and syntax?

What would a computational linguist tell you? Well, it depends!

What will I show you today? They are fundamentally similar!

The Take-Home Message

- Two kind of dependencies: local and non-local
- The core mechanisms are the same cross-domain, over the respective structural representations.
- Relativized locality plays a major role

The Elevator Pitch

Parallels between phonology and syntax?

What would a computational linguist tell you? Well, it depends!

What will I show you today? They are fundamentally similar!

The Take-Home Message

- Two kind of dependencies: local and non-local
- The core mechanisms are the same cross-domain, over the respective structural representations.
- Relativized locality plays a major role

The Elevator Pitch

Parallels between phonology and syntax?

What would a computational linguist tell you? Well, it depends!

What will I show you today? They are fundamentally similar!

The Take-Home Message

- **Two kind of dependencies**: local and non-local
- The core mechanisms are the same cross-domain, over the respective structural representations.
- Relativized locality plays a major role

Outline

1 Local Dependencies

- In Phonology
- In Syntax

2 Non-local Dependencies

- In Phonology
- In Syntax

A methodological note:

- Only phonotactics considered (no input-output mappings)
- Minimalist Grammars (Stabler 1997) as a model of syntax
- Formal language theory as a tool to assess parallelisms

Outline

1 Local Dependencies

- In Phonology
- In Syntax

2 Non-local Dependencies

- In Phonology
- In Syntax

A methodological note:

- Only phonotactics considered (no input-output mappings)
- Minimalist Grammars (Stabler 1997) as a model of syntax
- Formal language theory as a tool to assess parallelisms

Local Dependencies in Phonology

1 Word-final devoicing

Forbid voiced segments at the end of a word

- (1) a. * rad
 - b. rat

1 Intervocalic voicing

Forbid voiceless segments in between two vowels

- (2) a. * faser
 - b. fazer

These patters can be described by strictly local (SL) constraints.

Local Dependencies in Phonology

1 Word-final devoicing

Forbid voiced segments at the end of a word

- (1) a. * rad
 - b. rat

1 Intervocalic voicing

Forbid voiceless segments in between two vowels

- (2) a. * faser
 - b. fazer

These patters can be described by strictly local (SL) constraints.

Local Dependencies in Phonology are SL

Example: Word-final devoicing

- Forbid voiced segments at the end of a word: *[+voice]\$
- German: *z\$, *v\$,*d\$ (\$ = word edge).

Example: Intervocalic voicing

- Forbid voicess segments in-between two vowels: *V[-voice]V
- German: *ase, *ise, *ese, *isi, ...

Local Dependencies in Phonology are SL

Example: Word-final devoicing

- Forbid voiced segments at the end of a word: *[+voice]\$
- German: *z\$, *v\$,*d\$ (\$ = word edge).

Example: Intervocalic voicing

- Forbid voicess segments in-between two vowels: *V[-voice]V
- German: *ase, *ise, *ese, *isi, ...

Local Dependencies in Phonology are SL

Example: Word-final devoicing

- Forbid voiced segments at the end of a word: *[+voice]\$
- German: *z\$, *v\$,*d\$ (\$ = word edge).

Example: Intervocalic voicing

- Forbid voicess segments in-between two vowels: *V[-voice]V
- German: *ase, *ise, *ese, *isi, ...

What about Syntax?

We need a model for syntax ...

- Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- Operations: Merge and Move
- Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items

Local dependencies in syntax

- Merge is a feature-driven operation: category feature N⁻, D⁻, ... selector feature N⁺, D⁺, ...
- Subcategorization as formalized by Merge is strictly local.

What about Syntax?

We need a model for syntax ...

- Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- Operations: Merge and Move
- Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items

Local dependencies in syntax

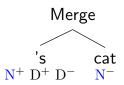
- Merge is a feature-driven operation: category feature N⁻, D⁻, ... selector feature N⁺, D⁺, ...
- Subcategorization as formalized by Merge is strictly local.

- ► category feature N⁻, D⁻, ...
- selector feature N^+ , D^+ , ...

 $s cat N^+ D^+ D^- N^-$

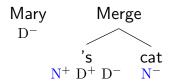
Local Dependencies in Syntax

- ► category feature N⁻, D⁻, ...
- \blacktriangleright selector feature N⁺, D⁺, ...



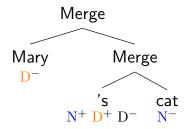
Local Dependencies in Syntax

- ▶ category feature N^- , D^- , ...
- selector feature N^+ , D^+ , ...

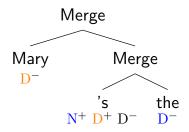


Local Dependencies in Syntax

- \blacktriangleright category feature N⁻, D⁻, ...
- ▶ selector feature N^+ , D^+ , ...

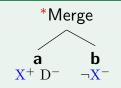


Merge is SL (Graf 2012a)

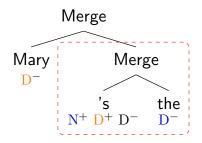


SL constraints on Merge

- We lift constraints from string *n*-grams to tree *n*-grams
- We get SL constraints over subtrees.

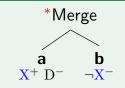


Merge is SL (Graf 2012a)



SL constraints on Merge

- We lift constraints from string *n*-grams to tree *n*-grams
- We get SL constraints over subtrees.



Interim Summary

	Local	Data Structure
Phonology	?	?
Syntax	?	?

Local phenomena modeled by *n*-grams of bounded size:

- computationally very simple
- learnable from positive examples of strings/trees
- plausible cognitive requirements

Interim Summary

	Local	Data Structure
Phonology	SL	Strings
Syntax	SL	Trees

Local phenomena modeled by *n*-grams of bounded size:

- computationally very simple
- learnable from positive examples of strings/trees
- plausible cognitive requirements

Interim Summary

	Local	Non-local	Data Structure
Phonology	SL	?	Strings
Syntax	SL	?	Trees

Local phenomena modeled by *n*-grams of bounded size:

- computationally very simple
- learnable from positive examples of strings/trees
- plausible cognitive requirements

Unbounded Dependencies in Phonology

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (3) a. *hasxintilawa∫
 - b. * ha**∫**xintilawa<mark>s</mark>
 - c. hafxintilawaf
- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (4) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. ha∫xintilawa∫

Example: Samala

```
*$hasxintilawa∫$
```

\$ha∫xintilawa∫\$

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. ha∫xintilawa∫

Example: Samala

```
*$hasxintilawa∫$
```

\$ha∫xintilawa∫\$

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf

Example: Samala

```
*$ha<mark>s</mark>xintilawa<mark>∫</mark>$
```

\$ha∫xintilawa∫\$

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf

Example: Samala

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. ha∫xintilawa∫

Example: Samala

But: Sibilants can be arbitrarily far away from each other!

*\$**s**tajanowonwa**∫**\$

- Samala Sibilant Harmony
 Sibilants must not disagree in anteriority. (Applegate 1972)
 - (5) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. ha∫xintilawa∫

Example: Samala

But: Sibilants can be arbitrarily far away from each other!

Locality Over Tiers

*\$<mark>¦s</mark>tajanowonwa∫¦\$

- Sibilants can be arbitrarily far away from each other!
- **Problem**: SL limited to locality domains of size *n*;

Tier-based Strictly Local (TSL) Grammars (Heinz et al. 2011)

- Projection of selected segments on a tier T;
- Strictly local constraints over T determine wellformedness;
- Unbounded dependencies are local over tiers.

Locality Over Tiers

*\$<mark>s</mark>tajanowonwa**∫**\$

- Sibilants can be arbitrarily far away from each other!
- **Problem**: SL limited to locality domains of size *n*;

Tier-based Strictly Local (TSL) Grammars (Heinz et al. 2011)

- Projection of selected segments on a tier T;
- Strictly local constraints over T determine wellformedness;
- Unbounded dependencies are local over tiers.

Let's revisit Samala Sibilant Harmony

- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]

Example: TSL Samala

Let's revisit Samala Sibilant Harmony

- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]

Example: TSL Samala

^{*}§hasxintilaw∫\$

^{ok}\$ha∫xintilaw∫\$

Let's revisit Samala Sibilant Harmony

- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]

Example: TSL Samala

^{ok}\$ha∫xintilaw∫\$

Let's revisit Samala Sibilant Harmony

- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]

Example: TSL Samala

*\$h<mark>as</mark>xintilaw**∫**\$

^{ok}\$ha∫xintilaw∫\$

- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant]



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant] I.E. *sſ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant] I.E. *sſ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant] I.E. *sſ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz



- (6) a. *hasxintilawa∫
 - b. *ha∫xintilawa<mark>s</mark>
 - c. hafxintilawaf
- What do we need to project? [+strident]
- What do we need to ban? *[+ant][-ant],*[-ant][+ant] I.E. *sſ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz



- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (7) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

Example

- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (7) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

Example

- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (7) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

Example

*LHLLHL

TSL Phonology: Accounting for Context

- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (7) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

Example

LHLLHL

*LHLLHL

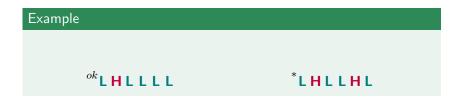
TSL Phonology: Accounting for Context

- Unbounded Tone Plateauing in Luganda (UTP) No L may occur within an interval spanned by H. (Hyman 2011)
 - (7) a. LHLLLL
 - b. LLLLHL
 - c. * LHLLHL
 - d. LHHHHL

Example



- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH



- Most non-local dependencies in phonology are TSL
- What about syntax?

- Project every H; project L iff immediately follows H
- ► Ban: HLH

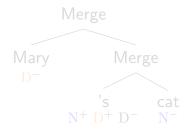


- Most non-local dependencies in phonology are TSL
- What about syntax?

Non-Local Dependencies in Syntax

Let's stick to core operations:

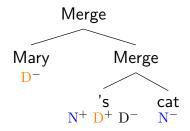
- Move
- Merge?



Non-Local Dependencies in Syntax

Let's stick to core operations:

- Move
- Merge?

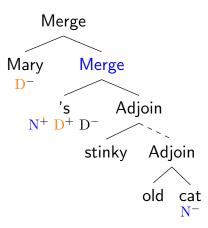


Non-Local Dependencies in Syntax

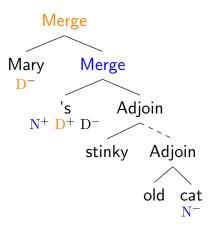
Let's stick to core operations:

- Move
- Merge: Unbounded adjunction

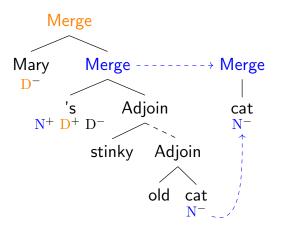
Frey and Gärtner (2002); Graf (2017b)



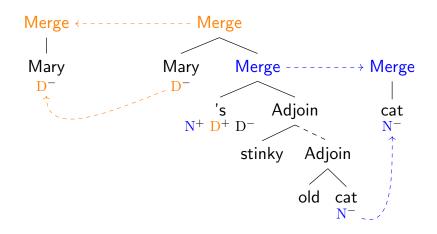
TSL over Trees: Projecting Tiers

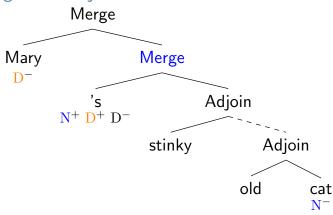


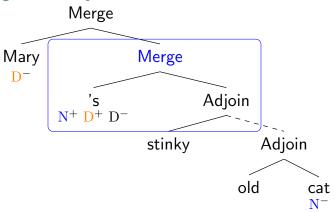
TSL over Trees: Projecting Tiers



TSL over Trees: Projecting Tiers

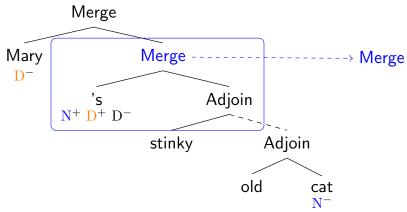






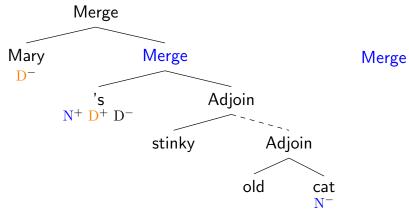
A TSL grammar for Merge

1 Project Merge iff a child has X^+ (e.g. X = N)

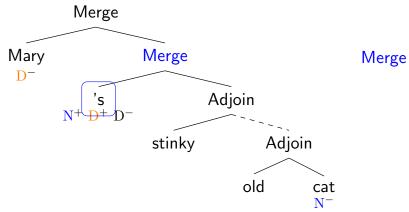


A TSL grammar for Merge

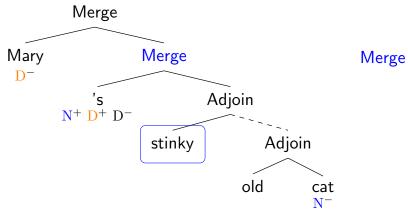
1 Project **Merge** iff a child has X^+ (e.g. X = N)



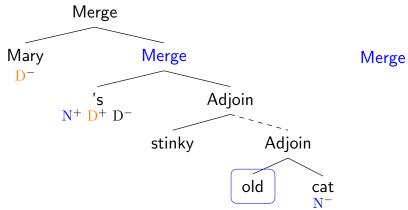
- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



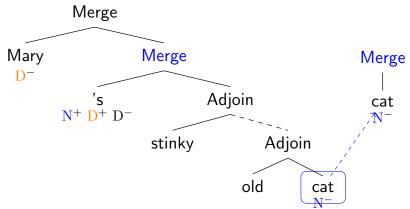
- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



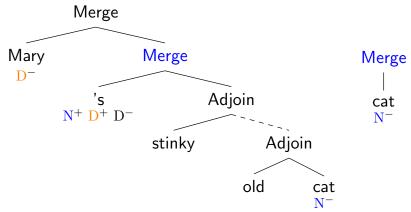
- 1 Project Merge iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



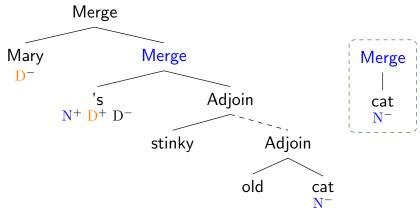
- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



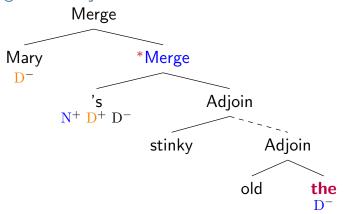
- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



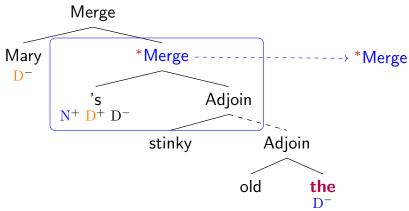
- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)



- **1** Project **Merge** iff a child has X^+ (e.g. X = N)
- 2 Project any node which has X^- (e.g. X = N)
- **3** No Merge without exactly one LI among its daughters.

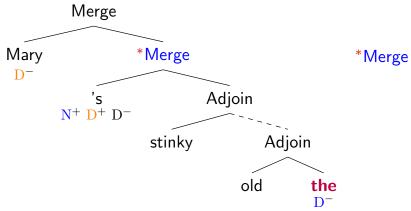


- 1 Project Merge iff a child has X^+ (e.g. X = V)
- 2 Project any node which has X^- (e.g. X = V)
- **3** No Merge without exactly one LI among its daughters.



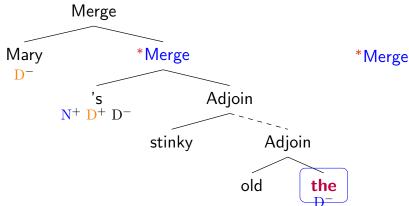
- **1** Project **Merge** iff a child has X^+ (e.g. X = V)
- 2 Project any node which has X^- (e.g. X = V)
- **3** No Merge without exactly one LI among its daughters.



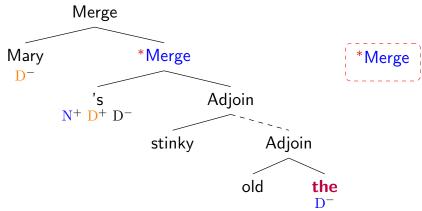


- **1** Project **Merge** iff a child has X^- (e.g. X = V)
- **2** Project any node which has X^+ (e.g. X = V)
- **3** No Merge without exactly one LI among its daughters.





- **1** Project **Merge** iff a child has X^- (e.g. X = V)
- **2** Project any node which has X^+ (e.g. X = V)
- **3** No Merge without exactly one LI among its daughters.



- **1** Project **Merge** iff a child has X^- (e.g. X = V)
- **2** Project any node which has X^+ (e.g. X = V)
- **3** No Merge without exactly one LI among its daughters.

	Local	Non-local	
Phonology	?	?	
Syntax	?	?	

Relativized Locality:

Non-local dependencies are local over a simple relativization domain.

Strong Cognitive Parallelism Hypothesis

	Local	Non-local	
Phonology	SL	?	
Syntax	SL	?	

Relativized Locality:

Non-local dependencies are local over a simple relativization domain.

Strong Cognitive Parallelism Hypothesis

	Local	Non-local
Phonology	SL	TSL
Syntax	SL	TSL

Relativized Locality:

Non-local dependencies are local over a simple relativization domain.

Strong Cognitive Parallelism Hypothesis

	Local	Non-local	Data Structure
Phonology	SL	TSL	Strings
Syntax	SL	TSL	Trees

Relativized Locality:

Non-local dependencies are local over a simple relativization domain.

Strong Cognitive Parallelism Hypothesis

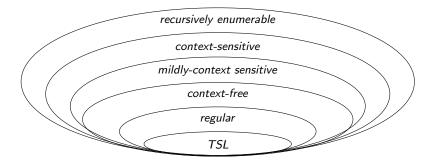
	Local	Non-local	Data Structure
Phonology	SL	TSL	Strings
Syntax	SL	TSL	Trees

Relativized Locality:

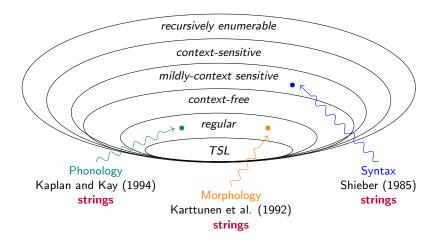
Non-local dependencies are local over a simple relativization domain.

Strong Cognitive Parallelism Hypothesis

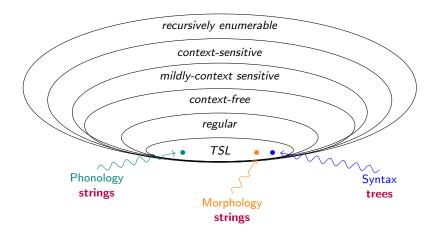
A Bird's-Eye View of the Framework



A Bird's-Eye View of the Framework



A Bird's-Eye View of the Framework



Strong Cognitive Parallelism Hypothesis

Phonology, (morphology), and syntax have the **same subregular complexity** over their respective **structural representations**.

We gain a unified perspective on:

typology

- learnability
- cognition

Strong Cognitive Parallelism Hypothesis

Phonology, (morphology), and syntax have the **same subregular complexity** over their respective **structural representations**.

We gain a unified perspective on:

typology

 \times Intervocalic Voicing iff applied an even times in the string

- \times Have a CP iff it dominates $\geq 3~{\rm TPs}$
- learnability

cognition

Strong Cognitive Parallelism Hypothesis

Phonology, (morphology), and syntax have the **same subregular complexity** over their respective **structural representations**.

We gain a unified perspective on:

typology

 \times Intervocalic Voicing iff applied an even times in the string

 \times Have a CP iff it dominates $\geq 3~{\rm TPs}$

learnability

Learnable from positive examples of strings/trees.

cognition

Strong Cognitive Parallelism Hypothesis

Phonology, (morphology), and syntax have the **same subregular complexity** over their respective **structural representations**.

We gain a unified perspective on:

typology

 \times Intervocalic Voicing iff applied an even times in the string

 \times Have a CP iff it dominates $\geq 3~{\rm TPs}$

learnability

Learnable from positive examples of strings/trees.

cognition

Finite, flat memory

Future Work

We are just getting started:

- autosegmental structures (Jardine 2017:i.a)
- morphological derivations (Chandlee 2017; Aksënova and De Santo 2017)
- mappings (Chandlee 2014; Chandlee and Heinz 2018:i.a.)
- syntax beyond Merge and Move (Graf 2017b; Vu 2018)

Join the Enterprise!

- typological universals/gaps
- TSL-analyses of phenomena/counterexamples
- artificial language learning experiments
- new formal results
- and much more ...

References I

- Aksënova, Alëna, and Aniello De Santo. 2017. Strict locality in morphological derivations. In *Proceedings of the 53rd Meeting of the Chicago Linguistic Society* (*CLS53*). (to appear).
- Aksënova, Alëna, Thomas Graf, and Sedigheh Moradi. 2016. Morphotactics as tier-based strictly local dependencies. In *Proceedings of SIGMorPhon 2016*. To appear.
- Applegate, R.B. 1972. *Ineseno chumash grammar*. Doctoral Dissertation, University of California, Berkeley.
- Chandlee, Jane. 2014. Strictly local phonological processes. Doctoral Dissertation, University of Delaware. URL http://udspace.udel.edu/handle/19716/13374.
- Chandlee, Jane. 2017. Computational locality in morphological maps. *Morphology* 27:599–641.
- Chandlee, Jane, and Jeffrey Heinz. 2018. Strict locality and phonological maps. *Linguistic Inquiry* 49:23–60.
- De Santo, Aniello, and Thomas Graf. 2017. Structure sensitive tier projection: Applications and formal properties. Ms., Stony Brook University.
- Epstein, Samuel D., Erich M. Groat, Ruriko Kawashima, and Hisatsugu Kitahara. 1998. *A derivational approach to syntactic relations*. Oxford: Oxford University Press.

References II

- Fowlie, Meaghan. 2013. Order and optionality: Minimalist grammars with adjunction. In Proceedings of the 13th Meeting on the Mathematics of Language (MoL 13), ed. András Kornai and Marco Kuhlmann, 12–20.
- Frey, Werner, and Hans-martin Gärtner. 2002. On the treatment of scrambling and adjunction in minimalist grammars. In *In Proceedings, Formal Grammar?02*. Citeseer.
- Gärtner, Hans-Martin, and Jens Michaelis. 2010. On the treatment of multiple-wh-interrogatives in Minimalist grammars. In *Language and logos*, ed. Thomas Hanneforth and Gisbert Fanselow, 339–366. Berlin: Akademie Verlag.
- Graf, Thomas. 2012a. Locality and the complexity of Minimalist derivation tree languages. In *Formal Grammar 2010/2011*, ed. Philippe de Groot and Mark-Jan Nederhof, volume 7395 of *Lecture Notes in Computer Science*, 208–227. Heidelberg: Springer. URL http://dx.doi.org/10.1007/978-3-642-32024-8_14.
- Graf, Thomas. 2012b. Movement-generalized Minimalist grammars. In LACL 2012, ed. Denis Béchet and Alexander J. Dikovsky, volume 7351 of Lecture Notes in Computer Science, 58–73. URL http://dx.doi.org/10.1007/978-3-642-31262-5_4.
- Graf, Thomas. 2012c. Tree adjunction as Minimalist lowering. In *Proceedings of the* 11th International Workshop on Tree Adjoining Grammars and Related Formalisms (TAG+11), 19–27.

References III

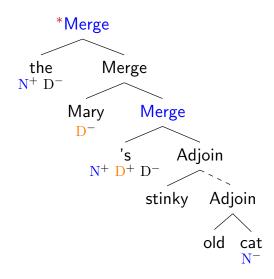
- Graf, Thomas. 2013. Local and transderivational constraints in syntax and semantics. Doctoral Dissertation, UCLA. URL http://thomasgraf.net/doc/papers/PhDThesis_RollingRelease.pdf.
- Graf, Thomas. 2014a. Late merge as lowering movement in Minimalist grammars. In *LACL 2014*, ed. Nicholas Asher and Sergei Soloviev, volume 8535 of *Lecture Notes in Computer Science*, 107–121. Heidelberg: Springer.
- Graf, Thomas. 2014b. Models of adjunction in Minimalist grammars. In *Formal Grammar 2014*, ed. Glynn Morrill, Reinhard Muskens, Rainer Osswald, and Frank Richter, volume 8612 of *Lecture Notes in Computer Science*, 52–68. Heidelberg: Springer.
- Graf, Thomas. 2017a. Grammar size and quantitative restrictions on movement. In *Proceedings of the Society for Computation in Linguistics (SCiL) 2018*, 23–33.
- Graf, Thomas. 2017b. Why movement comes for free once you have adjunction. In Proceedings of CLS 53. URL http://ling.auf.net/lingbuzz/003943, (to appear).
- Heinz, Jeffrey, Chetan Rawal, and Herbert G. Tanner. 2011. Tier-based strictly local constraints in phonology. In *Proceedings of the 49th Annual Meeting of the Association for Computational Linguistics*, 58–64. URL http://www.aclweb.org/anthology/P11-2011.
- Hunter, Tim. 2015. Deconstructing merge and move to make room for adjunction. *Syntax* 18:266–319.

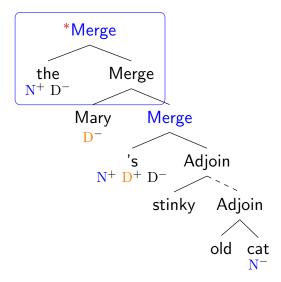
References IV

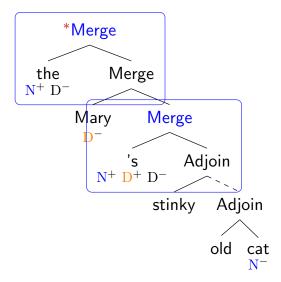
- Hunter, Tim, and Robert Frank. 2014. Eliminating rightward movement: Extraposition as flexible linearization of adjuncts. *Linguistic Inquiry* 45:227–267.
- Hyman, Larry M. 2011. Tone: Is it different? The Handbook of Phonological Theory, Second Edition 197–239.
- Jardine, Adam. 2017. On the logical complexity of autosegmental representations. In *Proceedings of the 15th Meeting on the Mathematics of Language*, ed. Makoto Kanazawa, Philippe de Groote, and Mehrnoosh Sadrzadeh, 22–35. London, UK: Association for Computational Linguistics.
- Kobele, Gregory M. 2006. Generating copies: An investigation into structural identity in language and grammar. Doctoral Dissertation, UCLA. URL http://home.uchicago.edu/~gkobele/files/Kobele06GeneratingCopies.pdf.
- Kobele, Gregory M. 2008. Across-the-board extraction and Minimalist grammars. In Proceedings of the Ninth International Workshop on Tree Adjoining Grammars and Related Frameworks.
- Kobele, Gregory M. 2010. On late adjunction in Minimalist grammars. Slides for a talk given at MCFG+ 2010.
- Kobele, Gregory M. 2011. Minimalist tree languages are closed under intersection with recognizable tree languages. In *LACL 2011*, ed. Sylvain Pogodalla and Jean-Philippe Prost, volume 6736 of *Lecture Notes in Artificial Intelligence*, 129–144.

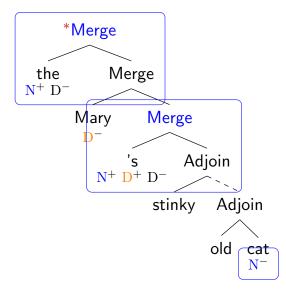
References V

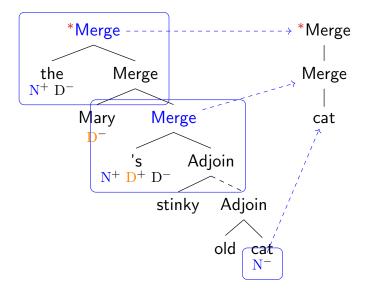
- Kobele, Gregory M., Sabrina Gerth, and John T. Hale. 2012. Memory resource allocation in top-down Minimalist parsing. In *Proceedings of Formal Grammar* 2012.
- McMullin, Kevin. 2016. Tier-based locality in long-distance phonotactics: Learnability and typology. Doctoral Dissertation, Uniersity of British Columbia.
- Pasternak, Robert. 2016. Memory usage and scope ambiguity resolution. Qualifying paper, Stony Brook University.
- Stabler, Edward P. 1997. Derivational Minimalism. In Logical aspects of computational linguistics, ed. Christian Retoré, volume 1328 of Lecture Notes in Computer Science, 68–95. Berlin: Springer.
- Stabler, Edward P. 2006. Sidewards without copying. In Formal Grammar '06, Proceedings of the Conference, ed. Gerald Penn, Giorgio Satta, and Shuly Wintner, 133–146. Stanford: CSLI.
- Stabler, Edward P. 2011. Computational perspectives on Minimalism. In Oxford handbook of linguistic Minimalism, ed. Cedric Boeckx, 617–643. Oxford: Oxford University Press.
- Stabler, Edward P. 2013. Two models of minimalist, incremental syntactic analysis. *Topics in Cognitive Science* 5:611–633.
- Vu, Mai Ha. 2018. Towards a formal description of npi-licensing patterns. Proceedings of the Society for Computation in Linguistics (SCiL) 2018 154–163.

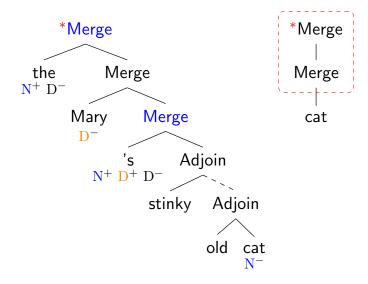












Tier-Based Strictly Local Morphology







- ▶ Work by Alëna Aksënova, Thomas Graf, and Sophie Moradi.
- It seems that morphology is also TSL. (Aksënova et al. 2016)
- ▶ We are unaware of any non-TSL patterns in this realm.
- Tight typology, explains gaps

Example: Circumfixation in Indonesian

- Indonesian has circumfixation with no upper bound on the distance between the two parts of the circumfix.
- (8) maha siswa
 (9) *(ke-) maha siswa *(-an)
 big pupil
 'student'
 'student affairs'
 - Requirements: exactly one ke- and exactly one -an

Tier ₁	contains all NMN affixes	\$ an			ke	ke	\$
Tier ₀	contains all morphemes						
n-grams	\$an, ke\$, keke, anan	\$ an	m	S	ke	ke	\$

Example: Circumfixation in Indonesian

- Indonesian has circumfixation with no upper bound on the distance between the two parts of the circumfix.
- (8) maha siswa
 (9) *(ke-) maha siswa *(-an)
 big pupil
 'student'
 'student affairs'
 - Requirements: exactly one ke- and exactly one -an

$Tier_1$	contains all NMN affixes	\$ an			ke	ke	\$
$Tier_0$	contains all morphemes						
<i>n</i> -grams	\$an, ke\$, keke, anan	\$ an	m	S	ke	ke	\$

Example: Swahili vyo

Swahili *vyo* is **either a prefix or a suffix**, depending on presence of negation. (?)

(10) a. a- vi- soma -vyo SBJ:CL.1- OBJ:CL.8- read -REL:CL.8 'reads'

> b. a- si- vyo- vi- soma SBJ:CL.1- NEG- REL:CL.8- read -OBJ:CL.8 'doesn't read'

Example: Swahili vyo [cont.]

- (11) a. * a- **vyo-** vi- **soma** SBJ:CL.1- REL:CL.8- OBJ:CL.8- read
 - b. * a- vyo- vi- soma -vyo SBJ:CL.1- REL:CL.8- OBJ:CL.8- read -REL:CL.8
 - c. * a- si- vyo- vi- soma SBJ:CL.1- NEG- REL:CL.8- OBJ:CL.8- read -vyo REL:CL.8-
 - d. * a- si- vi- soma -vyo SBJ:CL.1- NEG- OBJ:CL.8- read REL:CL.8-

Example: Swahili vyo [cont.]

Generalizations About vyo

- may occur at most once
- must follow negation prefix si- if present
- ▶ is a prefix iff *si* is present

Tier ₁	contains vyo, si, and stem edges $\#$				
Tier ₀	contains all morphem	nes			
<i>n</i> -grams	vyovyo, vyo##vyo	"at most one <i>vyo</i> "			
	vyosi, vyo##si	" <i>vyo</i> follows <i>si</i> "			
	si##vyo, \$vyo##	" <i>vyo</i> is prefix iff <i>si</i> present"			

Explaining Typological Gaps

Restriction to TSL can also explain some typological gaps.

General Strategy

- Attested patterns A and B are TSL.
- ▶ But combined pattern **A**+**B** is not attested.
- Show that **A**+**B** is not TSL.

Example: Compounding Markers

- Russian has an infix -o- that may occur between parts of compounds.
- Turkish has a single suffix -si that occurs at end of compounds.
- (12) vod **-o-** voz **-o-** voz water -COMP- carry -COMP- carry 'carrier of water-carriers'
- (13) türk bahçe kapı -sı (*-sı) turkish garden gate -COMP (*-COMP)
 'Turkish garden gate'

New Universal

If a language allows unboundedly many compound affixes, they are **infixes**.

Example: Compounding Markers [cont.]

Russian and Turkish are TSL.

Tier1COMP affix and stem edges #Russian n-gramsoo, \$o, o\$Turkish n-gramssisi, \$si, si#

- ▶ The combined pattern would yield Ruskish: stemⁿ⁺¹-siⁿ
- This pattern is not regular and hence **not TSL either**.

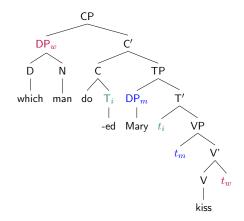
Interim Summary: Morphology

- While we know less about morphology than phonology at this point, it also seems to be TSL.
- Even complex patterns like Swahili vyo can be captured.
- At the same time, we get new universals:

Bounded Circumfixation No recursive process can be realized via circumfixation.

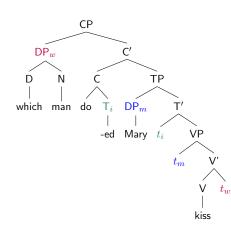
- We can reuse tools and techniques from TSL phonology, including learning algorithms.
- The cognitive resource requirements are also comparable.

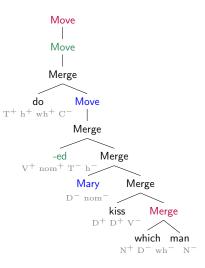
MGs & Derivation Trees



Phrase Structure Tree

MGs & Derivation Trees





Phrase Structure Tree

Derivation Tree

Constraints on Move

What about Move?

Suppose our MG is in **single movement normal form**, i.e. every phrase moves at most once. Then movement is regulated by two constraints. (Graf 2012

Constraints on Movement

- Move Every head with a negative Move feature is dominated by a matching Move node.
- SMC Every Move node is a closest dominating match for exactly one head.

Constraints on Move

What about Move?

Suppose our MG is in single movement normal form,

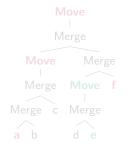
i.e. every phrase moves at most once.

Then movement is regulated by two constraints. (Graf 2012a)

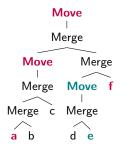
Constraints on Movement

- Move Every head with a negative Move feature is dominated by a matching Move node.
- SMC Every Move node is a closest dominating match for exactly one head.

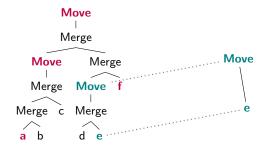
- There is no upper bound on the distance between a lexical item and its matching Move node.
- Consequently, Move dependencies are not local.
- What if every movement type (wh, topic, ...) induces its own tier? Would that make Move dependencies local?



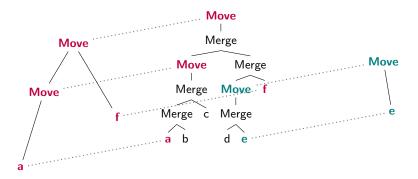
- There is no upper bound on the distance between a lexical item and its matching Move node.
- Consequently, Move dependencies are not local.
- What if every movement type (wh, topic, ...) induces its own tier? Would that make Move dependencies local?



- There is no upper bound on the distance between a lexical item and its matching Move node.
- Consequently, Move dependencies are not local.
- What if every movement type (wh, topic, ...) induces its own tier? Would that make Move dependencies local?



- There is no upper bound on the distance between a lexical item and its matching Move node.
- Consequently, Move dependencies are not local.
- What if every movement type (wh, topic, ...) induces its own tier? Would that make Move dependencies local?



Move Constraints over Tiers

Original

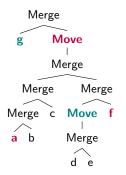
- **Move** Every head with a negative Move feature is dominated by a matching Move node.
- **SMC** Every Move node is a closest dominating match for exactly one head.

Tier

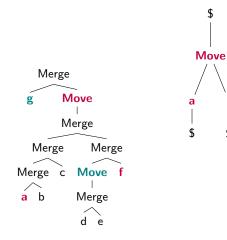
Every lexical item has a **mother** labeled Move.

Exactly one of a Move node's **daughters** is a lexical item.

Tree <i>n</i> -gram Templates						
	Move	SMC1	SMC2			
	\$	Move	Move			
-	$\geq 1 \text{ LI}$	no LI	≥ 2 Lls			

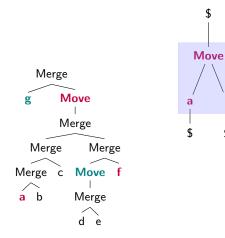




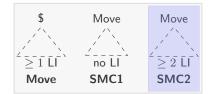


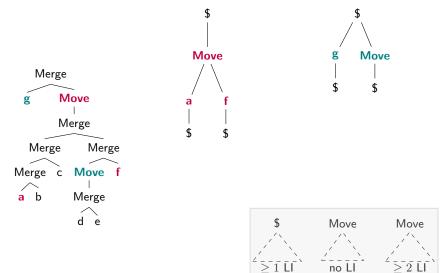
\$





\$

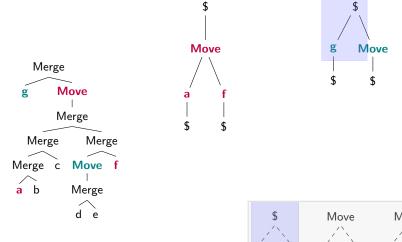




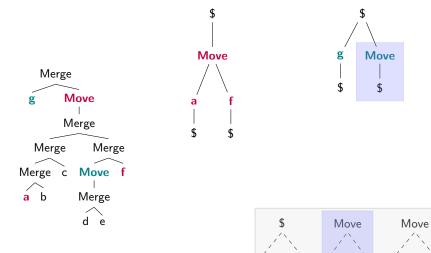
SMC1

Move

SMC2







 ≥ 1 LI

Move

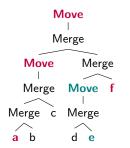
no Ll

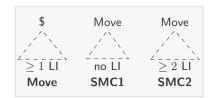
SMC1

 $\geq 2 \overline{\text{LI}}$

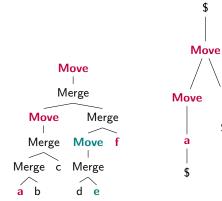
SMC2

Example of Well-Formed Derivation





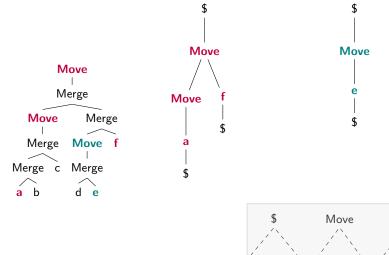
Example of Well-Formed Derivation



S



Example of Well-Formed Derivation



> 1 LI

Move



no Ll

SMC1

Remarks on Single Movement Normal Form

- Single Movement Normal Form seems unrealistic.
- But: does not rule out multiple movement steps, only says there is single feature trigger in derivation
- Intermediate landing sites can be part of structure built from the derivation tree.

A Conjecture on Movement Restrictions (Graf 2017a)

- Conversion of an MG into single movement normal form causes large blow-up in size of lexicon.
- Blow-up varies a lot: from 0 to hundred times the original size
- ► The more fixed the position of movers, the smaller the blow-up ⇒ island constraints as a means to limit lexical blow-up?

Remarks on Single Movement Normal Form

- Single Movement Normal Form seems unrealistic.
- But: does not rule out multiple movement steps, only says there is single feature trigger in derivation
- Intermediate landing sites can be part of structure built from the derivation tree.

A Conjecture on Movement Restrictions (Graf 2017a)

- Conversion of an MG into single movement normal form causes large blow-up in size of lexicon.
- Blow-up varies a lot: from 0 to hundred times the original size
- ► The more fixed the position of movers, the smaller the blow-up ⇒ island constraints as a means to limit lexical blow-up?

The Central Role of Derivation Trees

- Derivation trees are rarely considered in generative syntax. (but see Epstein et al. 1998)
- satisfy Chomsky's structural desiderata:
 - no linear order
 - Iabel-free
 - extension condition
 - inclusiveness condition
- contain all information to produce phrase structure trees
 central data structure of Minimalist syntax

Psychological Reality of Derivation Trees

Central role of derivation trees backed up by processing data:

- Derivation trees can be parsed top-down (Stabler 2013)
- Parsing models update Derivational Theory of Complexity, make correct processing predictions for
 - right < center embedding (Kobele et al. 2012)</p>
 - crossing < nested dependencies (Kobele et al. 2012)
 - ► SC-RC < RC-SC (?)</p>
 - SRC < ORC in English (?)</p>
 - SRC < ORC in East-Asian (?)</p>
 - quantifier scope preferences (Pasternak 2016)

Technical Fertility of Derivation Trees

Derivation trees made it easy for MGs to accommodate the full syntactic toolbox:

- sidewards movement (Stabler 2006; Graf 2013)
- affix hopping (Graf 2012b, 2013)
- clustering movement (Gärtner and Michaelis 2010)
- tucking in (Graf 2013)
- ATB movement (Kobele 2008)
- copy movement (Kobele 2006)
- extraposition (Hunter and Frank 2014)
- Late Merge (Kobele 2010; Graf 2014a)
- Agree (Kobele 2011; Graf 2012a)
- adjunction (Fowlie 2013; Graf 2014b; Hunter 2015)
- ► TAG-style adjunction (Graf 2012c)

Samala (Revisited)

Sibilant Harmony in SAMALA (McMullin 2016)

- 1) Unbounded sibilant harmony
- a. /k-su-∫ojin/ k∫u∫ojin "I darken it" b. /k-su-k'ili-mekeken-∫/ k∫uk'ilimekeket∫ "I straighten up"

2) /s/ \rightarrow [J] when preceding (adjacent) [t, n, l]

- a. /s-lok'in/ ∫lok'in "he cuts it" b. /s-tepu?/ ∫tepu? "he gambles"
- 3) Long-distance agreement overrides local disagreement
- a. /s-i∫t-i∫ti-jep-us/ sististijepus b. /s-net-us/ snetus

"they show him" "he does it to him"

Samala (Revisited)

Sibilant Harmony in SAMALA (McMullin 2016)

- 1) Unbounded sibilant harmony
- a. /k-su-∫ojin/ k∫u∫ojin "I darken it" b. /k-su-k'ili-mekeken-∫/ k∫uk'ilimekeket∫ "I straighten up"

2) /s/ \rightarrow [J] when preceding (adjacent) [t, n, l]

- a. /s-lok'in/\$\int_cuts it''b. /s-tepu?/\$\int_tepu?"he gambles"
- 3) Long-distance agreement overrides local disagreement
- a. /s-i∫t-i∫ti-jep-us/ sististijepu b. /s-net-us/ snetus

"they show him" "he does it to him"

Samala (Revisited)

Sibilant Harmony in SAMALA (McMullin 2016)

- 1) Unbounded sibilant harmony
- a. /k-su-∫ojin/ k∫u∫ojin "I darken it"
 b. /k-su-k'ili-mekeken-∫/ k∫uk'ilimekeket∫ "I straighten up"

2) /s/ \rightarrow [J] when preceding (adjacent) [t, n, l]

- a. /s-lok'in/ flok'in "he cuts it" b. /s-tepu?/ ftepu? "he gambles"
- 3) Long-distance agreement overrides local disagreement
- a. /s-iʃt-iʃti-jep-us/ sististijepus "they show him" b. /s-net-us/ snetus "he does it to him"

SAMALA Sibilant Harmony (Revisited)

- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization

snetus

SAMALA Sibilant Harmony (Revisited)

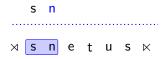
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization

🛪 s n e t u s 🖂

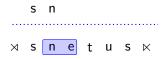
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



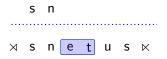
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



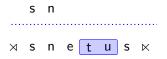
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



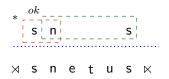
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



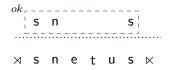
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



SAMALA Sibilant Harmony (Revisited)

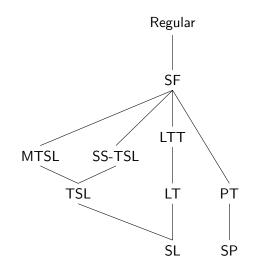
- anticipatory sibilant harmony
- palatalization to avoid local restrictions
- sibilant harmony overrides palatalization



Grammar

$$\begin{aligned} \mathsf{T} &= \{ \ \sigma : \sigma \in \{\mathsf{s}, \ J\} \lor (\sigma \in \{ \ \mathsf{n}, \ \mathsf{t}, \ I \ \} \land \ \mathsf{s} \prec^+ \sigma) \} \\ \mathsf{S} &= \{ *\mathsf{s}\mathsf{f}, \ *\mathsf{s}\mathsf{f}, \ *\mathsf{sn}(\neg\mathsf{s}), \ *\mathsf{st}(\neg\mathsf{s}), \ *\mathsf{sl}(\neg\mathsf{s}) \} \end{aligned}$$

SS -TSL: Relations to other Classes



The TSL Neighborhood: a Plethora of Combinations

